

#### **Cambridge Assessment International Education**

Cambridge International Advanced Subsidiary and Advanced Level

MATHEMATICS
Paper 1
MARK SCHEME
Maximum Mark: 75
Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge International will not enter into discussions about these mark schemes.

Cambridge International is publishing the mark schemes for the May/June 2018 series for most Cambridge IGCSE™, Cambridge International A and AS Level and Cambridge Pre-U components, and some Cambridge O Level components.

IGCSE™ is a registered trademark.



#### Cambridge International AS/A Level – Mark Scheme

#### PUBLISHED

#### **Generic Marking Principles**

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptors for a question. Each question paper and mark scheme will also comply with these marking principles.

#### **GENERIC MARKING PRINCIPLE 1:**

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

#### **GENERIC MARKING PRINCIPLE 2:**

Marks awarded are always whole marks (not half marks, or other fractions).

#### **GENERIC MARKING PRINCIPLE 3:**

Marks must be awarded positively:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- · marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

#### **GENERIC MARKING PRINCIPLE 4:**

Rules must be applied consistently e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

© UCLES 2018 Page 2 of 15

### Cambridge International AS/A Level – Mark Scheme **PUBLISHED**

#### **GENERIC MARKING PRINCIPLE 5:**

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

#### **GENERIC MARKING PRINCIPLE 6:**

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

© UCLES 2018 Page 3 of 15

#### Mark Scheme Notes

Marks are of the following three types:

- M Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.
- A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).
- B Mark for a correct result or statement independent of method marks.
- When a part of a question has two or more 'method' steps, the M marks are generally independent unless the scheme specifically says
  otherwise; and similarly when there are several B marks allocated. The notation DM or DB (or dep\*) is used to indicate that a particular M or B
  mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier
  marks are implied and full credit is given.
- The symbol FT implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise,
  A or B marks are given for correct work only. A and B marks are not given for fortuitously 'correct' answers or results obtained from incorrect
  working.
  - Note: B2 or A2 means that the candidate can earn 2 or 0.
     B2/1/0 means that the candidate can earn anything from 0 to 2.

The marks indicated in the scheme may not be subdivided. If there is genuine doubt whether a candidate has earned a mark, allow the candidate the benefit of the doubt. Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored.

- Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise.
- For a numerical answer, allow the A or B mark if a value is obtained which is correct to 3 s.f., or which would be correct to 3 s.f. if rounded (1 d.p. in the case of an angle). As stated above, an A or B mark is not given if a correct numerical answer arises fortuitously from incorrect working. For Mechanics questions, allow A or B marks for correct answers which arise from taking *g* equal to 9.8 or 9.81 instead of 10.

© UCLES 2018 Page 4 of 15

### Cambridge International AS/A Level – Mark Scheme PUBLISHED

May/June 2018

The following abbreviations may be used in a mark scheme or used on the scripts:

AEF/OE Any Equivalent Form (of answer is equally acceptable) / Or Equivalent

, ,	,
AG	Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)
CAO	Correct Answer Only (emphasising that no 'follow through' from a previous error is allowed)

CWO Correct Working Only – often written by a 'fortuitous' answer

ISW Ignore Subsequent Working

SOI Seen or implied

SR Special Ruling (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the light of a particular circumstance)

#### **Penalties**

- MR –1 A penalty of MR –1 is deducted from A or B marks when the data of a question or part question are genuinely misread and the object and difficulty of the question remain unaltered. In this case all A and B marks then become 'follow through' marks. MR is not applied when the candidate misreads his own figures this is regarded as an error in accuracy. An MR –2 penalty may be applied in particular cases if agreed at the coordination meeting.
- PA –1 This is deducted from A or B marks in the case of premature approximation. The PA –1 penalty is usually discussed at the meeting.

© UCLES 2018 Page 5 of 15

## Cambridge International AS/A Level – Mark Scheme **PUBLISHED**

Question	Answer	Marks	Guidance
1(i)	$(1-2x)^5 = 1-10x + 40x^2 $ (no penalty for extra terms)	B2,1	Loses a mark for each incorrect term. Treat $-32x^5 + 80x^4 - 80x^3$ as MR -1
		2	
1(ii)	$\to (1 + ax + 2x^2)(1 - 10x + 40x^2)$		
	3 terms in $x^2 \to 40 - 10a + 2$	M1 A1FT	Selects 3 terms in $x^2$ . FT from (i)
	Equate with $12 \rightarrow a = 3$	A1	CAO
		3	

Question	Answer	Marks	Guidance
2	$y = 2x + \frac{5}{x}$ $\rightarrow \frac{dy}{dx} = 2 - \frac{5}{x^2} = -3$ (may be implied) when $x = 1$ .	M1 A1	Reasonable attempt at differentiation CAO (-3)
	$\frac{\mathrm{d}y}{\mathrm{d}t} = \frac{\mathrm{d}y}{\mathrm{d}x} \times \frac{\mathrm{d}x}{\mathrm{d}t}  \to  -0.06$	M1 A1	Ignore notation, but needs to multiply $\frac{dy}{dx}$ by 0.02.
		4	

© UCLES 2018 Page 6 of 15

## Cambridge International AS/A Level – Mark Scheme **PUBLISHED**

Question	Answer	Marks	Guidance
3	$\frac{dy}{dx} = \frac{12}{(2x+1)^2} \to y = \frac{-12}{2x+1} \div 2 \ (+c)$	B1 B1	Correct without " $\div$ 2". For " $\div$ 2". Ignore " $c$ ".
	Uses $(1, 1) \rightarrow c = 3 \ ( \rightarrow y = \frac{-6}{2x+1} + 3)$	M1 A1	Finding "c" following integration. CAO
	Sets y to 0 and attempts to solve for $x \to x = \frac{1}{2} \to ((\frac{1}{2}, 0))$	DM1 A1	Sets y to 0. $x = \frac{1}{2}$ is sufficient for A1.
		6	

Question	Answer	Marks	Guidance
4(i)	$(\sin\theta + \cos\theta)(1 - \sin\theta\cos\theta) \equiv \sin^3\theta + \cos^3\theta.$		Accept abbreviations s and c
	$LHS = \sin\theta + \cos\theta - \sin^2\theta \cos\theta - \sin\theta \cos^2\theta$	M1	Expansion
	$= \sin\theta(1 - \cos^2\theta) + \cos\theta(1 - \sin^2\theta) \text{ or } (s + c - c(1 - c^2) - s(1 - s^2))$	M1A1	Uses identity twice. Everything correct. AG
	Uses $\sin^2\theta + \cos^2\theta = 1 \rightarrow \sin^3\theta + \cos^3\theta$ (RHS)		or from RHS: M1 for use of trig ID twice
	Or		
	LHS = $(\sin \theta + \cos \theta)(\sin^2 \theta + \cos^2 \theta - \sin \theta \cos \theta)$	M1	M1 for factorisation
	$= \sin^3\theta + \sin\theta\cos^2\theta - \sin^2\theta\cos\theta + \cos\theta\sin^2\theta + \cos^3\theta - \sin\theta\cos^2\theta = \sin^3\theta + \cos^3\theta$	M1A1	
		3	

© UCLES 2018 Page 7 of 15

## Cambridge International AS/A Level – Mark Scheme **PUBLISHED**

Question	Answer	Marks	Guidance
4(ii)	$(\sin\theta + \cos\theta)(1 - \sin\theta\cos\theta) = 3\cos^3\theta \rightarrow \sin^3\theta = 2\cos^3\theta$	M1	
	$\rightarrow \tan^3 \theta = 2 \rightarrow \theta = 51.6^{\circ} \text{ or } 231.6^{\circ} \text{ (only)}$	A1A1FT	Uses $\tan^3 = \sin^3 \div \cos^3$ . A1 CAO. A1FT, 180 + their acute angle. $\tan^3 \theta = 0$ gets M0
		3	

Question	Answer	Marks	Guidance
5(i)	Eqn of $AC$ $y = -\frac{1}{2}x + 4$ (gradient must be $\Delta y / \Delta x$ )	M1A1	Uses gradient and a given point for equa. CAO
	Gradient of $OB = 2 \rightarrow y = 2x$ (If y missing only penalise once)	M1 A1	Use of $m_1m_2 = -1$ , answers only ok.
		4	

© UCLES 2018 Page 8 of 15

## Cambridge International AS/A Level – Mark Scheme **PUBLISHED**

Question	Answer	Marks	Guidance
5(ii)	Simultaneous equations $\rightarrow$ ((1.6, 3.2))	M1	Equate and solve for M1 and reach ≥1 solution
	This is mid-point of $OB. \rightarrow B \ (3.2, 6.4)$	M1 A1	Uses mid-point. CAO
	or		
	Let coordinates of $B$ $(h, k)$ $OA = AB \rightarrow h^2 = 8k - k^2$ $OC = BC \rightarrow k^2 = 16h - h^2 \rightarrow (3.2, 6.4)$		M1 for both equations, M1 for solving with $y = 2x$
	or		
	gradients $(\frac{k-4}{h} \times \frac{k}{h-8} = -1)$		M1 for gradient product as $-1$ , M1 solving with $y = 2x$
	or		
	Pythagoras: $h^2 + (k-4)^2 + (h-8)^2 + k^2 = 4^2 + 8^2$		M1 for complete equation, M1 solving with $y = 2x$
		3	

Question	Answer	Marks	Guidance
6(i)	$(\tan\theta = \frac{AT}{r}) \rightarrow AT = r \tan\theta \text{ or } OT = \frac{r}{\cos\theta} \text{ SOI}$	B1	CAO
	$\to A = \frac{1}{2} r^2 \tan \theta \qquad -\frac{1}{2} r^2 \theta$	B1 B1	B1 for $\frac{1}{2}r^2\tan\theta$ . B1 for " $-\frac{1}{2}r^2\theta$ "  If Pythagoras used may see area of triangle as $\frac{1}{2}r\sqrt{r^2+r^2\tan^2\theta} \text{ or } \frac{1}{2}r\left(\frac{r}{\cos\theta}\right)\sin\theta$
		3	

## Cambridge International AS/A Level – Mark Scheme **PUBLISHED**

Question	Answer	Marks	Guidance
6(ii)	$\tan\theta = \frac{AT}{3} \rightarrow AT = 7.716$	M1	Correct use of trigonometry and radians in rt angle triangle
	Arc length = $r\theta = 3.6$	<b>B</b> 1	Accept 3×1.2
	$OT$ by Pythagoras or $\cos 1.2 = \frac{3}{OT}$ (= 8.279)	M1	Correct method for OT
	Perimeter = $AT$ + arc + $OT$ - radius = 16.6	A1	CAO, www
		4	

Question	Answer	Marks	Guidance
7	$\overrightarrow{OA} = \begin{pmatrix} 1 \\ -3 \\ 2 \end{pmatrix},  \overrightarrow{OB} = \begin{pmatrix} -1 \\ 3 \\ 5 \end{pmatrix} \text{ and } \overrightarrow{OC} = \begin{pmatrix} 3 \\ 1 \\ -2 \end{pmatrix}$		
7(i)	$\overrightarrow{AC} = \begin{pmatrix} 2\\4\\-4 \end{pmatrix}$	B1	B1 for $\overrightarrow{AC}$ .
		1	

© UCLES 2018 Page 10 of 15

## Cambridge International AS/A Level – Mark Scheme **PUBLISHED**

Ma	y/June	2018
----	--------	------

Question	Answer	Marks	Guidance
7(ii)	$\overrightarrow{OM} = \overrightarrow{OA} + \overrightarrow{AM} = \begin{pmatrix} 2 \\ -1 \\ 0 \end{pmatrix} \text{ or } \frac{1}{2} \begin{bmatrix} 1 \\ -3 \\ 2 \end{pmatrix} + \begin{pmatrix} 3 \\ 1 \\ -2 \end{bmatrix} $	M1	M1 for their $\overrightarrow{OM} = \overrightarrow{OA} + \overrightarrow{AM}$ oe
	Unit vector in direction of $\overrightarrow{OM} = \frac{1}{\sqrt{5}} (\overrightarrow{OM})$	M1 A1	M1 for dividing their $\overrightarrow{OM}$ by their modulus
		3	
7(iii)	$\overrightarrow{AB} = \begin{pmatrix} -2\\6\\3 \end{pmatrix}, \text{ Allow } \pm$	B1	
	$ \overrightarrow{AB} =7,  \overrightarrow{AC} =6$ $\begin{pmatrix} -2\\6\\3 \end{pmatrix}. \begin{pmatrix} 2\\4\\-4 \end{pmatrix} = -4 + 24 - 12 = 8$	M1 M1	Product of both moduli, Scalar product of ± their AB and AC
	$7 \times 6 \cos \theta = 8 \rightarrow \theta = 79.(0)^{\circ}$	A1	1.38 radians ok
		4	

© UCLES 2018 Page 11 of 15

# Cambridge International AS/A Level – Mark Scheme **PUBLISHED**

Question	Answer	Marks	Guidance
8(a)	$ar = 12$ and $\frac{a}{1-r} = 54$	B1 B1	CAO, OE CAO, OE
	Eliminates $a$ or $r \to 9r^2 - 9r + 2 = 0$ or $a^2 - 54a + 648 = 0$	M1	Elimination leading to a 3-term quadratic in a or r
	$\rightarrow r = \frac{2}{3} \text{ or } \frac{1}{3} \text{ hence to } a \rightarrow a = 18 \text{ or } 36$	A1	Needs both values.
		4	
8(b)	nth term of a progression is $p + qn$		
8(b)(i)	first term = $p + q$ . Difference = $q$ or last term = $p + qn$	B1	Need first term and, last term or common difference
	$S_n = \frac{n}{2} (2(p+q) + (n-1)q)$ or $\frac{n}{2} (2p+q+nq)$	M1A1	Use of $S_n$ formula with their $a$ and $d$ . ok unsimplified for A1.
		3	
8(b)(ii)	Hence $2(2p+q+4q) = 40$ and $3(2p+q+6q) = 72$	DM1	Uses their $S_n$ formula from (i)
	Solution $\rightarrow p = 5$ and $q = 2$ [Could use $S_n$ with $a$ and $d \rightarrow a = 7$ , $d = 2 \rightarrow p = 5$ , $q = 2$ .]	A1	Note: answers 7, 2 instead of 5, 2 gets M1A0 – must attempt to solve for M1
		2	

© UCLES 2018 Page 12 of 15

### Cambridge International AS/A Level – Mark Scheme PUBLISHED

Question	Answer	Marks	Guidance
9	$f: x \mapsto \frac{x}{2} - 2,  g: x \mapsto 4 + x - \frac{x^2}{2}$		
9(i)	$4 + x - \frac{x^2}{2} = \frac{x}{2} - 2  \to  x^2 - x - 12 = 0$	M1	Equates and forms 3 term quadratic
	$\rightarrow$ (4, 0) and (-3, -3.5) Trial and improvement, B3 all correct or B0	A1 A1	A1 For both <i>x</i> values or a correct pair. A1 all.
		3	
9(ii)	f(x) > g(x) for $x > 4$ , $x < -3$	B1, B1	B1 for each part. Loses a mark for $\leq$ or $\geq$ .
		2	
9(iii)	$fg(x) = 2 + \frac{x}{2} - \frac{x^2}{4} - 2 \left(= \frac{x}{2} - \frac{x^2}{4}\right)$	B1	CAO, any correct form
	i.e. $-\frac{1}{4}((x-1)^2 - 1)$ or $\frac{dy}{dx} = \frac{1}{2} - \frac{2x}{4} = 0 \rightarrow x = 1$	M1 A1	Completes the square or uses calculus. First A1 is for $x = 1$ or completed square form
	$\rightarrow y = \frac{1}{4} \rightarrow \text{Range of fg} \leqslant \frac{1}{4},$	A1	CAO, OE e.g. $y \leqslant \frac{1}{4}$ , $[-\infty, \frac{1}{4})$ etc.
		4	
9(iv)	Calculus or completing square on 'h' $\rightarrow x = 1$	M1	May use a sketch or $-\frac{b}{2a}$
	$k=1$ (accept $k \geqslant 1$ )	A1	Complete method. CAO
		2	

© UCLES 2018 Page 13 of 15

# Cambridge International AS/A Level – Mark Scheme **PUBLISHED**

Question	Answer	Marks	Guidance
10	$y = x^3 - 2x^2 + 5x$		
10(i)	$\frac{\mathrm{d}y}{\mathrm{d}x} = 3x^2 - 4x + 5$	B1	CAO
	Using $b^2 - 4ac \rightarrow 16 - 60 \rightarrow$ negative $\rightarrow$ some explanation or completed square and explanation	M1 A1	Uses discriminant on equation (set to 0). CAO
		3	
10(ii)	$\frac{dm}{dx} = 6x - 4 (= 0) \text{ (must identify as } \frac{dm}{dx}\text{)}$	B1FT	FT providing differentiation is equivalent
	$ \Rightarrow x = \frac{2}{3}, \ m = \frac{11}{3} \text{ or } \frac{dy}{dx} = \frac{11}{3} $ Alt1: $m = 3\left(x - \frac{2}{3}\right)^2 + \frac{11}{3}, \ m = \frac{11}{3} $ Alt2: $3x^2 - 4x + 5 - m = 0, \ b^2 - 4ac = 0, \ m = \frac{11}{3} $	M1 A1	Sets to 0 and solves. A1 for correct <i>m</i> .  Alt1: B1 for completing square, M1A1 for ans  Alt2: B1 for coefficients, M1A1 for ans
	$\frac{d^2m}{dx^2} = 6 + ve \rightarrow \text{Minimum value or refer to sketch of curve or}$ $\text{check values of } m \text{ either side of } x = \frac{2}{3},$	M1 A1	M1 correct method. A1 (no errors anywhere)
		5	

© UCLES 2018 Page 14 of 15

## Cambridge International AS/A Level – Mark Scheme **PUBLISHED**

May/June	2018
----------	------

Question	Answer	Marks	Guidance
10(iii)	Integrate $\rightarrow \frac{x^4}{4} - \frac{2x^3}{3} + \frac{5x^2}{2}$	B2,1	Loses a mark for each incorrect term
	Uses limits 0 to 6 $\rightarrow$ 270 (may not see use of lower limit)	M1 A1	Use of limits on an integral. CAO Answer only 0/4
		4	

© UCLES 2018 Page 15 of 15