



## Cambridge International AS & A Level

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**MATHEMATICS**

**9709/31**

Paper 3 Pure Mathematics 3

**October/November 2020**

**1 hour 50 minutes**

You must answer on the question paper.

You will need: List of formulae (MF19)

### INSTRUCTIONS

- Answer **all** questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

### INFORMATION

- The total mark for this paper is 75.
- The number of marks for each question or part question is shown in brackets [ ].

This document has **20** pages. Blank pages are indicated.



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- 2 On a sketch of an Argand diagram, shade the region whose points represent complex numbers  $z$  satisfying the inequalities  $|z| \geq 2$  and  $|z - 1 + i| \leq 1$ . [4]















(b) Find the other roots of this equation.

[4]

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8 The coordinates  $(x, y)$  of a general point of a curve satisfy the differential equation

$$x \frac{dy}{dx} = (1 - 2x^2)y,$$

for  $x > 0$ . It is given that  $y = 1$  when  $x = 1$ .

Solve the differential equation, obtaining an expression for  $y$  in terms of  $x$ . [6]

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9 Let  $f(x) = \frac{8 + 5x + 12x^2}{(1 - x)(2 + 3x)^2}$ .

(a) Express  $f(x)$  in partial fractions. [5]

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(b) Hence obtain the expansion of  $f(x)$  in ascending powers of  $x$ , up to and including the term in  $x^2$ . [5]

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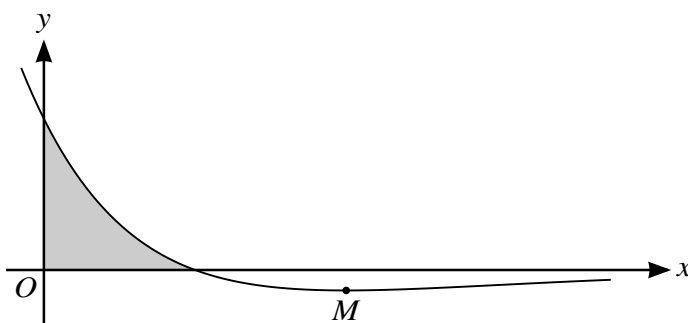
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The diagram shows the curve  $y = (2 - x)e^{-\frac{1}{2}x}$ , and its minimum point  $M$ .

(a) Find the exact coordinates of  $M$ .

[5]

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- 11 Two lines have equations  $\mathbf{r} = \mathbf{i} + 2\mathbf{j} + \mathbf{k} + \lambda(a\mathbf{i} + 2\mathbf{j} - \mathbf{k})$  and  $\mathbf{r} = 2\mathbf{i} + \mathbf{j} - \mathbf{k} + \mu(2\mathbf{i} - \mathbf{j} + \mathbf{k})$ , where  $a$  is a constant.
- (a) Given that the two lines intersect, find the value of  $a$  and the position vector of the point of intersection. [5]

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