



## Cambridge International AS & A Level

CANDIDATE  
NAME

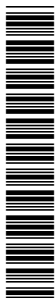
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**MATHEMATICS**

**9709/12**

Paper 1 Pure Mathematics 1

**October/November 2023**

**1 hour 50 minutes**

You must answer on the question paper.

You will need: List of formulae (MF19)

### INSTRUCTIONS

- Answer **all** questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

### INFORMATION

- The total mark for this paper is 75.
- The number of marks for each question or part question is shown in brackets [ ].

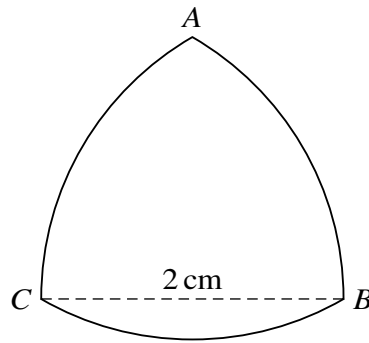
This document has **20** pages.







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The diagram shows the shape of a coin. The three arcs  $AB$ ,  $BC$  and  $CA$  are parts of circles with centres  $C$ ,  $A$  and  $B$  respectively.  $ABC$  is an equilateral triangle with sides of length 2 cm.

(a) Find the perimeter of the coin. [2]

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(b) Find the area of the face  $ABC$  of the coin, giving the answer in terms of  $\pi$  and  $\sqrt{3}$ . [4]

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6 The equation of a curve is  $y = x^2 - 8x + 5$ .

(a) Find the coordinates of the minimum point of the curve. [2]

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The curve is stretched by a factor of 2 parallel to the y-axis and then translated by  $\begin{pmatrix} 4 \\ 1 \end{pmatrix}$ .

(b) Find the coordinates of the minimum point of the transformed curve. [2]

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(c) Find the equation of the transformed curve. Give the answer in the form  $y = ax^2 + bx + c$ , where  $a$ ,  $b$  and  $c$  are integers to be found. [4]

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7 (a) Verify the identity  $(2x - 1)(4x^2 + 2x - 1) \equiv 8x^3 - 4x + 1$ . [1]

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(b) Prove the identity  $\frac{\tan^2 \theta + 1}{\tan^2 \theta - 1} \equiv \frac{1}{1 - 2 \cos^2 \theta}$ . [3]

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8 Functions  $f$  and  $g$  are defined by

$$f(x) = (x + a)^2 - a \text{ for } x \leq -a,$$

$$g(x) = 2x - 1 \text{ for } x \in \mathbb{R},$$

where  $a$  is a positive constant.

(a) Find an expression for  $f^{-1}(x)$ . [3]

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(b) (i) State the domain of the function  $f^{-1}$ . [1]

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(ii) State the range of the function  $f^{-1}$ . [1]

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- (c) Given that  $a = \frac{7}{2}$ , solve the equation  $gf(x) = 0$ . [3]

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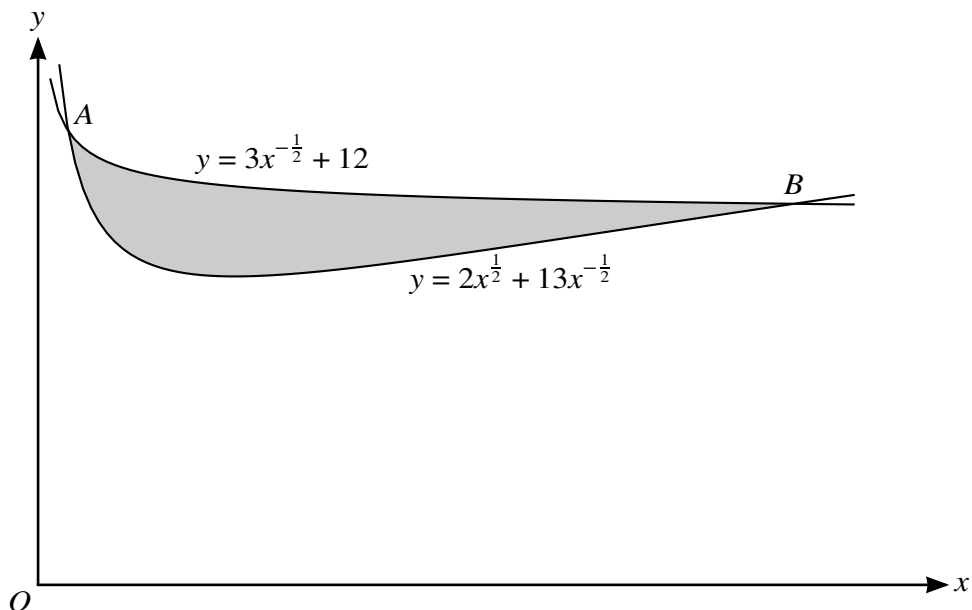
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The diagram shows curves with equations  $y = 2x^{\frac{1}{2}} + 13x^{-\frac{1}{2}}$  and  $y = 3x^{-\frac{1}{2}} + 12$ . The curves intersect at points A and B.

(a) Find the coordinates of A and B. [4]

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(b) State the set of values for which the function  $f$  is increasing. [1]

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**11** The coordinates of points *A*, *B* and *C* are (6, 4), (*p*, 7) and (14, 18) respectively, where *p* is a constant. The line *AB* is perpendicular to the line *BC*.

(a) Given that  $p < 10$ , find the value of  $p$ . [4]

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A circle passes through the points  $A$ ,  $B$  and  $C$ .

- (b) Find the equation of the circle. [3]

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- (c) Find the equation of the tangent to the circle at  $C$ , giving the answer in the form  $dx + ey + f = 0$ , where  $d$ ,  $e$  and  $f$  are integers. [3]

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**Additional Page**

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