



Cambridge International AS & A Level

MATHEMATICS**9709/13**

Paper 1 Pure Mathematics 1

October/November 2022

MARK SCHEME

Maximum Mark: 75

Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge International will not enter into discussions about these mark schemes.

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This document consists of **14** printed pages.

PUBLISHED**Generic Marking Principles**

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptors for a question. Each question paper and mark scheme will also comply with these marking principles.

GENERIC MARKING PRINCIPLE 1:

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

GENERIC MARKING PRINCIPLE 2:

Marks awarded are always **whole marks** (not half marks, or other fractions).

GENERIC MARKING PRINCIPLE 3:

Marks must be awarded **positively**:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:

Rules must be applied consistently, e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

GENERIC MARKING PRINCIPLE 5:

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

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Mathematics Specific Marking Principles	
1	Unless a particular method has been specified in the question, full marks may be awarded for any correct method. However, if a calculation is required then no marks will be awarded for a scale drawing.
2	Unless specified in the question, answers may be given as fractions, decimals or in standard form. Ignore superfluous zeros, provided that the degree of accuracy is not affected.
3	Allow alternative conventions for notation if used consistently throughout the paper, e.g. commas being used as decimal points.
4	Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored (isw).
5	Where a candidate has misread a number in the question and used that value consistently throughout, provided that number does not alter the difficulty or the method required, award all marks earned and deduct just 1 mark for the misread.
6	Recovery within working is allowed, e.g. a notation error in the working where the following line of working makes the candidate's intent clear.

PUBLISHED**Mark Scheme Notes**

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

Types of mark

- M** Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.
- A** Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).
- B** Mark for a correct result or statement independent of method marks.
- DM or DB** When a part of a question has two or more ‘method’ steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly, when there are several B marks allocated. The notation DM or DB is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
- FT** Implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only.
- A or B marks are given for correct work only (not for results obtained from incorrect working) unless follow through is allowed (see abbreviation FT above).
 - For a numerical answer, allow the A or B mark if the answer is correct to 3 significant figures or would be correct to 3 significant figures if rounded (1 decimal place for angles in degrees).
 - The total number of marks available for each question is shown at the bottom of the Marks column.
 - Wrong or missing units in an answer should not result in loss of marks unless the guidance indicates otherwise.
 - Square brackets [] around text or numbers show extra information not needed for the mark to be awarded.

PUBLISHED**Abbreviations**

AEF/OE	Any Equivalent Form (of answer is equally acceptable) / Or Equivalent
AG	Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)
CAO	Correct Answer Only (emphasising that no ‘follow through’ from a previous error is allowed)
CWO	Correct Working Only
ISW	Ignore Subsequent Working
SOI	Seen Or Implied
SC	Special Case (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the light of a particular circumstance)
WWW	Without Wrong Working
AWRT	Answer Which Rounds To

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Question	Answer	Marks	Guidance
1	$8(1 - \cos^2 \theta) + 6 \cos \theta + 1 = 0$	M1	Expect $8 \cos^2 \theta - 6 \cos \theta - 9 = 0$.
	$(4 \cos \theta + 3)(2 \cos \theta - 3) = 0$	A1	Factors or formula or completing square must be shown.
	$[\rightarrow \cos \theta = -0.75 \rightarrow \theta =] 138.6^\circ$ only,	A1	AWRT, ignore solutions outside the given range, answer in radians A0.
		3	

Question	Answer	Marks	Guidance
2(a)	$[f(x)] = \{-2(x+2)^2\} - \{5\}$	B1 B1	
		2	
2(b)	$[f(x)] < -7$	B1	Allow $y < -7, < -7, (-\infty, -7)$ or less than -7 $-\infty < f(x) < -7, -7 < f(x) < -\infty, f < -7$
		1	
2(c)	$y = -2(x+2)^2 - 5 \rightarrow (x+2)^2 = \frac{-(y+5)}{2}$	M1	Operations correct. Allow sign errors. FT <i>their</i> quadratic from (a).
	$x = [\pm] \sqrt{\frac{-(y+5)}{2}} - 2$	M1	Operations correct. Allow sign errors. FT <i>their</i> quadratic from (a).
	$[f^{-1}(x)] = -2 - \sqrt{\frac{-(x+5)}{2}}$ or $-2 - \sqrt{\frac{(x+5)}{2}}$	A1	Allow $[f^{-1}(x)] = -2 - \sqrt{\frac{x+5}{-2}}$.
		3	

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Question	Answer	Marks	Guidance
3(a)	$1+10x+40x^2$ May be part of a complete expansion	B2, 1, 0	1^5 must be simplified to 1, allow if the '1' is seen in a more complete expansion but not the final answer. Mis-reads not condoned in this question.
		2	
3(b)	$1-12x+54x^2$ May be part of a complete expansion	B2, 1, 0	1^4 must be simplified to 1, allow if the '1' is seen in a more complete expansion but not the final answer. Mis-reads not condoned in this question.
		2	
3(c)	$54-120+40$	M1	Forming exactly 3 products correctly using their terms.
	-26	A1	Allow $-26x^2$ If in a list with other terms it must be clear this is the required term otherwise A0.
		2	

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Question	Answer	Marks	Guidance
4	$\left[\frac{dv}{dx} \right] = (9-x)^2$	B1	Allow unsimplified forms. Allow any or no notation
	Substitute $x = 4$ into <i>their</i> differentiated V,	*M1	Expect 25.
	$\frac{dx}{dt} = \frac{1}{\text{their derivative}} \times 3.6$ (accept $\frac{dt}{dx} = \frac{\text{their derivative}}{3.6}$)	M1	Correct use of the chain rule, ignore incorrect conversions at this point. Expect 0.144
	$= \frac{1}{\text{their numerical derivative}} \times 3.6 \times \frac{100}{60}$	DM1	Correct use of the conversion factors.
	$= \frac{1}{25} \times 3.6 \times \frac{100}{60} = 0.24$	A1	
		5	

Question	Answer	Marks	Guidance
5(a)	3	B1	Ignore any description.
		1	
5(b)	2	B1	Ignore any description.
		1	
5(c)	(8, 2)	B1 B1	Ignore any description. Allow vector notation and absence of brackets.
		2	

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Question	Answer	Marks	Guidance
5(d)	(1, 5)	B1 FT	FT each coordinate, (<i>their</i> 8 – 7, <i>their</i> 2 + 3) Allow vector notation and absence of brackets.
		B1 FT	
		2	

Question	Answer	Marks	Guidance
6	Use of $\sin^2\alpha + \cos^2\alpha = 1$ eg $\sin\alpha = [\pm]\sqrt{1 - \left(\frac{8}{17}\right)^2}$	*M1	Or Pythagoras seen (may quote 8, 15, 17 triple).
	$\sin\alpha = \frac{15}{17}$	A1	
	$\tan\alpha = \frac{15}{8}$	A1	
	$\frac{1}{\sin\alpha} + \frac{1}{\tan\alpha} = \frac{17}{15} + \frac{8}{15}$	DM1	Dealing with reciprocals and addition of fractions correctly.
	$= \frac{5}{3}$ oe	A1	Correct answer with no working shown scores 0. Extra answers from $\sin\alpha = -\frac{15}{17}$ are allowed.
		5	

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Question	Answer	Marks	Guidance
7(a)	$\frac{-3}{(a+2)^4} = -\frac{16}{27} \rightarrow \text{e.g. } 16(a+2)^4 = 81$	M1	Equate first derivative and $-\frac{16}{27}$ and move term in a (or x) into the numerator.
	$\rightarrow (a+2)^2 = \frac{9}{4} \rightarrow a+2 = [\pm]\frac{3}{2}$	M1	Solve for $(a+2)$ or $(x+2)$
	$a = -\frac{1}{2}$ or $-\frac{7}{2}$	A1 A1	Allow 'x ='
		4	
7(b)	$[f(x)] = \frac{1}{(x+2)^3} [+c]$	B1	Allow unsimplified form and 'y ='
	$5 = 1 + c$	M1	Sub $x = -1$, $y = 5$ into an integral.
	$[f(x)] = \frac{1}{(x+2)^3} + 4$	A1	Allow 'y ='
		3	

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Question	Answer	Marks	Guidance
8(a)	$APQ = \cos^{-1} \frac{\frac{5}{6}r}{r} \left[= \cos^{-1} \frac{5}{6} \right]$	*M1	May use cosine rule to find APB. Stating APQ or APB as an incorrect multiple of π is M0.
	$= 0.5857$	A1	Accept 0.586 or 33.6° or APB (1.171 or 67.1°).
	Perimeter $= 4 \times r \times \text{their } 0.5857 = 2.34r$ or $0.745\pi r$ or $(293/125)r$	DM1 A1	Must use a numerical value of <i>their</i> angle.
		4	
8(b)	Use of sector formula: Sector APB $= \frac{1}{2}r^2 \times (2 \times \text{their } 0.5857)$ or Sector APC (C is on PQ so PC = r) $= \frac{1}{2}r^2 \times (\text{their } 0.5857)$	M1	Any sector with <i>their</i> appropriate angle. It must be clear the appropriate numerical angle is being used.
	Use of appropriate formula for area of triangle and correct combination with the sector to find the area of a half segment, one segment or both segments	M1	e.g. Area APB $= \frac{1}{2}r^2 \times \sin(2 \times \text{their } 0.5857)$.
	Shaded area $[= 2 \times 0.1250r^2] = 0.250r^2$	A1	or $0.0796\pi r^2$, allow $\frac{1}{4}r^2$ or $0.25 r^2$.
		3	

Question	Answer	Marks	Guidance
9(a)	$216r^3 = 64 \rightarrow r = 2/3$	B1	Allow decimal to 3sf (AWRT).
	$S_{\infty} = \frac{216}{1 - \text{their } \frac{2}{3}} = 648 \text{ cao}$	M1 A1	M1 depends on <i>their</i> $ r < 1$.
		3	

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Question	Answer	Marks	Guidance
9(b)	$216\left(\frac{2}{3}\right) = 144 \rightarrow 144 = a + d$	B1 FT	SOI, may be implied in the use of $96 = 144 + 3d$ and finding a . Mis-reads not condoned in 9(b) .
	$216\left(\frac{2}{3}\right)^2 = 96 \rightarrow 96 = a + 4d$	B1 FT	SOI, may be implied in the use of $96 = 144 + 3d$ and finding a .
	Solve simultaneously	*M1	No working may be seen.
	$d = -16, a = 160$	A1	Both required.
	$S_{21} = \frac{21}{2}\{320 + 20(-16)\} = 0$	DM1 A1	Or use of $\frac{21}{2}(a + u_{21})$.
			6

Question	Answer	Marks	Guidance
10(a)	$x^2 + (2x-1)^2 - 2 [= 0] \rightarrow 5x^2 - 4x - 1 [= 0]$	*M1 A1	Or $5y^2 + 2y - 7 [= 0]$.
	$(5x+1)(x-1)[= 0]$ or $(5y+7)(y-1)[= 0]$	DM1	May see factors or formula or completing square.
	$x = 1, y = 1$ or $(1, 1)$ only	A1	May be implied on the diagram.
			4

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Question	Answer	Marks	Guidance
10(b)	$(\pi) \int (2 - x^2) dx = (\pi) \left(2x - \frac{x^3}{3} \right)$	*M1 A1	Attempt integration of y^2 , allow $\int (2 - y^2) dy$.
	$(\pi) \left(2\sqrt{2} - \frac{(\sqrt{2})^3}{3} \right) - \left(2 - \frac{1}{3} \right)$	DM1	Apply limits $1 \rightarrow \sqrt{2}$.
	$\frac{\pi}{3} (4\sqrt{2} - 5)$	A1	CAO, allow $\frac{\pi}{3} (2\sqrt{8} - 5)$, must be in given form.
		4	
10(c)	Arc length = $\frac{1}{8} (2\pi\sqrt{2})$ or $\frac{\pi\sqrt{2}}{4}$ oe	B1	Must be exact.
	Perimeter = $\sqrt{2} + \text{their arc length}$	B1 FT	Must be exact, do not allow inverse trig functions.
		2	

Question	Answer	Marks	Guidance
11(a)	$(5 - 2p)^2 + (p + 2)^2 = (10 - 2p)^2 + (3 - p)^2$	M1 A1	Allow one sign error for M mark only.
	$25 - 20p + 4p^2 + p^2 + 4p + 4 = 100 - 40p + 4p^2 + 9 - 6p + p^2$ $30p = 80 \rightarrow p = \frac{8}{3}$ oe	A1	Allow 2.67 AWR T.
		3	

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Question	Answer	Marks	Guidance
11(b)(i)	$m_{AC} = \frac{p+2}{2p-5} \quad m_{BC} = \frac{p-3}{2p-10}$	M1	Allow a sign error.
	$\frac{p+2}{2p-5} \times \frac{p-3}{2p-10} = -1$	M1	Use of $m_1m_2 = -1$ with their m_{AC} and m_{BC} .
	$p^2 - p - 6 = -(4p^2 - 30p + 50) \rightarrow 5p^2 - 31p + 44 (=0)$	A1	
	$p = 4$ (Ignore $p = \frac{11}{5}$)	A1	Factors $(p-4)(5p-11)$, or formula or completing square must be seen.
		4	
11(b)(ii)	Mid-point of $AB = (7\frac{1}{2}, \frac{1}{2})$	B1	SOI
	$r^2 = 2\frac{1}{2}^2 + 2\frac{1}{2}^2 \left[= \frac{50}{4} \right]$ or $r = \sqrt{(2\frac{1}{2}^2 + 2\frac{1}{2}^2)} \left[= \frac{5\sqrt{2}}{2} \right]$	*M1	Or $r^2 = \frac{1}{4}(5^2 + 5^2) \left[= \frac{50}{4} \right]$ etc.
	Equation of circle is $(x - \text{their } 7\frac{1}{2})^2 + (y - \text{their } \frac{1}{2})^2 = \text{their } \frac{50}{4}$	DM1	Must use r^2 not r or d or d^2
	$x^2 + y^2 - 15x - y + 44 = 0$	A1	CAO
		4	