

Cambridge
International
A Level

Cambridge Assessment International Education
Cambridge International Advanced Level

CANDIDATE
NAME

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CENTRE
NUMBER

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FURTHER MATHEMATICS

9231/21

Paper 2

May/June 2019

3 hours

Candidates answer on the Question Paper.

Additional Materials: List of Formulae (MF10)

READ THESE INSTRUCTIONS FIRST

Write your centre number, candidate number and name in the spaces at the top of this page.

Write in dark blue or black pen.

You may use an HB pencil for any diagrams or graphs.

Do not use staples, paper clips, glue or correction fluid.

DO NOT WRITE IN ANY BARCODES.

Answer **all** the questions in the space provided. If additional space is required, you should use the lined page at the end of this booklet. The question number(s) must be clearly shown.

Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place in the case of angles in degrees, unless a different level of accuracy is specified in the question.

Where a numerical value is necessary, take the acceleration due to gravity to be 10 m s^{-2} .

The use of a calculator is expected, where appropriate.

Results obtained solely from a graphic calculator, without supporting working or reasoning, will not receive credit.

You are reminded of the need for clear presentation in your answers.

At the end of the examination, fasten all your work securely together.

The number of marks is given in brackets [] at the end of each question or part question.

This document consists of **25** printed pages and **3** blank pages.



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3

- 1 A particle P moves along an arc of a circle with centre O and radius 2 m. At time t seconds, the angle POA is θ , where $\theta = 1 - \cos 2t$, and A is a fixed point on the arc of the circle.

- (i) Show that the magnitude of the radial component of the acceleration of P when $t = \frac{1}{6}\pi$ is 6 m s^{-2} . [2]

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- (ii) Find the magnitude of the transverse component of the acceleration of P when $t = \frac{1}{6}\pi$. [2]

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(iii) Find the total kinetic energy lost by the three spheres as a result of the two collisions. [3]

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(ii) Find the value of c . [3]

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(iii) Find the value of the product moment correlation coefficient. [3]

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OR

A farmer grows two different types of cherries, Type *A* and Type *B*. He assumes that the masses of each type are normally distributed. He chooses a random sample of 8 cherries of Type *A*. He finds that the sample mean mass is 15.1 g and that a 95% confidence interval for the population mean mass, μ g, is $13.5 \leq \mu \leq 16.7$.

- (i) Find an unbiased estimate for the population variance of the masses of cherries of Type *A*. [3]

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The farmer now chooses a random sample of 6 cherries of Type *B* and records their masses as follows.

12.2 13.3 16.4 14.0 13.9 15.4

- (ii) Test at the 5% significance level whether the mean mass of cherries of Type *B* is less than the mean mass of cherries of Type *A*. You should assume that the population variances for the two types of cherry are equal. [9]

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