



## Cambridge International AS & A Level

CANDIDATE  
NAME

CENTRE  
NUMBER

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NUMBER

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### FURTHER MATHEMATICS

9231/21

Paper 2 Further Pure Mathematics 2

October/November 2022

2 hours

You must answer on the question paper.

You will need: List of formulae (MF19)

### INSTRUCTIONS

- Answer **all** questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

### INFORMATION

- The total mark for this paper is 75.
- The number of marks for each question or part question is shown in brackets [ ].

This document has **16** pages. Any blank pages are indicated.

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- 2 (a) Show that the system of equations

$$x - y + 2z = 4,$$

$$x - y - 3z = a,$$

$$x - y + 7z = 13,$$

where  $a$  is a constant, does not have a unique solution.

[2]

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- (b) Given that  $a = -5$ , show that the system of equations in part (a) is consistent. Interpret this situation geometrically. [3]

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- (c) Given instead that  $a \neq -5$ , show that the system of equations in part (a) is inconsistent. Interpret this situation geometrically. [2]

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- (c) Sketch the graph of  $y = \operatorname{sech} x$ , stating the equation of the asymptote. [2]

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- (d) By considering a suitable set of  $n$  rectangles of unit width, use your sketch to show that

$$\sum_{r=1}^n \operatorname{sech} r < \tan^{-1}(\sinh n). \quad [3]$$

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- (e) Hence state an upper bound, in terms of  $\pi$ , for  $\sum_{r=1}^{\infty} \operatorname{sech} r$ . [1]

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