

Please write clearly in block capitals.

Centre number

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I declare this is my own work.

# A-level FURTHER MATHEMATICS

## Paper 3 Statistics

Time allowed: 2 hours

### Materials

- You must have the AQA Formulae and statistical tables booklet for A-level Mathematics and A-level Further Mathematics.
- You should have a scientific calculator that meets the requirements of the specification. (You may use a graphical calculator.)
- You must ensure you have the other optional Question Paper/Answer Book for which you are entered (**either** Discrete **or** Mechanics). You will have 2 hours to complete **both** papers.

### Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- You must answer each question in the space provided for that question. If you require extra space for your answer(s), use the lined pages at the end of this book. Write the question number against your answer(s).
- Do **not** write outside the box around each page or on blank pages.
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work you do not want to be marked.

### Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 50.

### Advice

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
- You do not necessarily need to use all the space provided.

For Examiner's Use	
Question	Mark
1	
2	
3	
4	
5	
6	
7	
8	
<b>TOTAL</b>	



Answer **all** questions in the spaces provided.

**1** The discrete uniform distribution  $X$  can take values 1, 2, 3, ..., 10

Find  $P(X \geq 7)$

Circle your answer.

[1 mark]

0.3

0.4

0.6

0.7

**2** The random variable  $X$  has variance  $\text{Var}(X)$

Which of the following expressions is equal to  $\text{Var}(aX + b)$ , where  $a$  and  $b$  are non-zero constants?

Circle your answer.

[1 mark]

$a \text{Var}(X)$

$a \text{Var}(X) + b$

$a^2 \text{Var}(X)$

$a^2 \text{Var}(X) + b$



**3** In a game, it is only possible to score 10, 20 or 30 points.  
The probability of scoring 20 points is twice the probability of scoring 30 points.  
The probability of scoring 20 points is half the probability of scoring 10 points.

**3 (a)** Find the mean points scored when the game is played once, giving your answer to two decimal places.

**[3 marks]**

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**3 (b)** Mina plays the game.  
Her father, Michael, tells her that he will multiply her score by 5 and then subtract 10  
He will then give her the value he has calculated in pence rounded to the nearest penny.  
Calculate the expected value in pence that Mina receives.

**[2 marks]**

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**Turn over ►**



**4** Oscar is studying the daily maximum temperature in °C in a village during the month of June.

He constructs a 95% confidence interval of width 0.8 °C using a random sample of 150 days.

He assumes that the daily maximum temperature has a normal distribution.

**4 (a)** Find the standard deviation of Oscar's sample, giving your answer to three significant figures.

**[3 marks]**

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**4 (b)** Oscar calculates the mean of his sample to be 25.3 °C

He claims that the population mean is 26.0 °C

Explain whether or not his confidence interval supports his claim.

**[2 marks]**

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**4 (c)** Explain how Oscar could reduce the width of his 95% confidence interval.

**[1 mark]**

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**Turn over for the next question**

**Turn over ►**



**5** The continuous random variable  $X$  has cumulative distribution function

$$F(x) = \begin{cases} 0 & x \leq 1 \\ \frac{1}{10}x - \frac{1}{10} & 1 < x \leq 6 \\ \frac{1}{90}x^2 + \frac{1}{10} & 6 < x \leq 9 \\ 1 & x > 9 \end{cases}$$

**5 (a)** Find the probability density function  $f(x)$

**[2 marks]**

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**5 (b)** Show that  $\text{Var}(X) = \frac{6737}{1200}$

**[4 marks]**

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**6** Danai is investigating the number of speeding offences in different towns in a country. She carries out a hypothesis test to test for association between town and number of speeding offences per year.

**6 (a)** State the hypotheses for this test.

[1 mark]

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**6 (b)** The observed frequencies,  $O$ , have been collected and the expected frequencies,  $E$ , have been calculated in an  $n \times m$  contingency table, where  $n > 3$  and  $m > 3$

One of the values of  $E$  is less than 5

**6 (b) (i)** Explain what steps Danai should take before calculating the test statistic.

[2 marks]

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**6 (b) (ii)** State an expression for the test statistic Danai should calculate.

[1 mark]

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**6 (c)** Danai correctly calculates the value of the test statistic to be 45.22

The number of degrees of freedom for the test is 25

Determine the outcome of Danai's test, using the 1% level of significance.

**[3 marks]**

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**Turn over for the next question**

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7 The random variable  $X$  has an exponential distribution with parameter  $\lambda$

7 (a) Prove that  $E(X) = \frac{1}{\lambda}$

[4 marks]

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- 8** A company records the number of complaints,  $X$ , that it receives over 60 months. The summarised results are

$$\sum x = 102 \quad \text{and} \quad \sum (x - \bar{x})^2 = 103.25$$

- 8 (a)** Using this data, explain why it may be appropriate to model the number of complaints received by the company per month by a Poisson distribution with mean 1.7

**[3 marks]**

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**8 (c)** It is later found that the mean total number of complaints and enquiries received per month is 6.1

Find the power of the test carried out in part (b), giving your answer to four decimal places.

**[4 marks]**

Blank answer lines for calculation.

**END OF QUESTIONS**



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Question number	Additional page, if required. Write the question numbers in the left-hand margin.







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