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Centre number

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Candidate number

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Surname

Forename(s)

Candidate signature

A-level FURTHER MATHEMATICS

Paper 2

Thursday 6 June 2019

Afternoon

Time allowed: 2 hours

Materials

- You must have the AQA formulae and statistical tables booklet for A-level Mathematics and A-level Further Mathematics.
- You should have a scientific calculator that meets the requirements of the specification. (You may use a graphical calculator.)

Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- You must answer each question in the space provided for that question. If you require extra space for your answer(s), use the lined pages at the end of this book. Write the question number against your answer(s).
- Do **not** write outside the box around each page.
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work you do not want to be marked.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 100.

Advice

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
- You do not necessarily need to use all the space provided.

For Examiner's Use	
Question	Mark
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Answer **all** questions in the spaces provided.

- 1** Given that z is a complex number, and that z^* is the complex conjugate of z , which of the following statements is **not** always true?

Circle your answer.

[1 mark]

$$(z^*)^* = z \qquad zz^* = |z|^2 \qquad (-z)^* = -(z^*) \qquad z - z^* = z^* - z$$

- 2** Which of the straight lines given below is an asymptote to the curve

$$y = \frac{ax^2}{x-1}$$

where a is a non-zero constant?

Circle your answer.

[1 mark]

$$y = ax + a \qquad y = ax \qquad y = ax - a \qquad y = a$$

- 3** The set \mathcal{A} is defined by $\mathcal{A} = \{x : -\sqrt{2} < x < 0\} \cup \{x : 0 < x < \sqrt{2}\}$

Which of the inequalities given below has \mathcal{A} as its solution?

Circle your answer.

[1 mark]

$$|x^2 - 1| > 1 \qquad |x^2 - 1| \geq 1 \qquad |x^2 - 1| < 1 \qquad |x^2 - 1| \leq 1$$



4 The positive integer k is such that

$$\sum_{r=1}^k (3r - k) = 90$$

Find the value of k .

[3 marks]

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7 The points A , B and C have coordinates $A(4, 5, 2)$, $B(-3, 2, -4)$ and $C(2, 6, 1)$

7 (a) Use a vector product to show that the area of triangle ABC is $\frac{5\sqrt{11}}{2}$

[4 marks]

7 (b) The points A , B and C lie in a plane.

Find a vector equation of the plane in the form $\mathbf{r} \cdot \mathbf{n} = k$

[1 mark]



7 (c) Hence find the exact distance of the plane from the origin.

[1 mark]

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9 (c) Given that $\mathbf{M}^n \rightarrow \mathbf{L}$ as $n \rightarrow \infty$, find the matrix \mathbf{L} .

[4 marks]

9 (d) The transformation represented by \mathbf{L} maps all points onto a line.

Find the equation of this line.

[2 marks]

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1 3

12 Abel and Bonnie are trying to solve this mathematical problem:

$$z = 2 - 3i \text{ is a root of the equation}$$
$$2z^3 + mz^2 + pz + 91 = 0$$

Find the value of m and the value of p .

Abel says he has solved the problem.

Bonnie says there is not enough information to solve the problem.

12 (a) Abel's solution begins as follows:

Since $z = 2 - 3i$ is a root of the equation,
 $z = 2 + 3i$ is another root.

State **one extra** piece of information about m and p which could be added to the problem to make the beginning of Abel's solution correct.

[1 mark]



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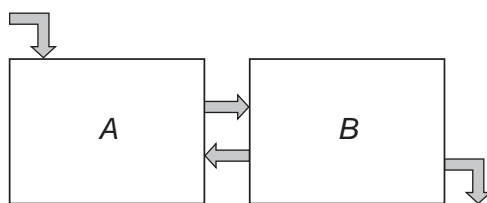
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15

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Two tanks, A and B , each have a capacity of 800 litres.

At time $t = 0$ both tanks are full of pure water.

When $t > 0$, water flows in the following ways:

- Water with a salt concentration of μ grams per litre flows into tank A at a constant rate
- Water flows from tank A to tank B at a rate of 16 litres per minute
- Water flows from tank B to tank A at a rate of r litres per minute
- Water flows out of tank B through a waste pipe
- The amount of water in each tank remains at 800 litres.

At time t minutes ($t \geq 0$) there are x grams of salt in tank A and y grams of salt in tank B .

This system is represented by the coupled differential equations

$$\frac{dx}{dt} = 36 - 0.02x + 0.005y \quad (1)$$

$$\frac{dy}{dt} = 0.02x - 0.02y \quad (2)$$

15 (a) Find the value of r .

[2 marks]



15 (b) Show that $\mu = 3$

[3 marks]

15 (c) Solve the coupled differential equations to find both x and y in terms of t .

[9 marks]

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