- ¹. The acceleration of a particle *P* moving in a straight line is (t 9t + 18) ms⁻², where *t* is the time in seconds.
 - i. Find the values of *t* for which the acceleration is zero.

[2]

[4]

[2]

- ii. It is given that when t = 3 the velocity of P is 9 ms⁻¹. Find the velocity of P when t = 0.
- iii. Show that the direction of motion of *P* changes before t = 1.
- 2. A particle *P* moves in a straight line. The displacement of *P* from a fixed point on the line is $(t^4 2t^8 + 5)m$, where *t* is the time in seconds. Show that, when t = 1.5,
 - i. Pis at instantaneous rest,
 - ii. the acceleration of P is 9 m s⁻².
- **3.** A particle *P* moves in a straight line. At time *t* s after passing through a point *O* of the line, the displacement of *P* from *O* is *x* m. Given that $x = 0.06t^8 0.45t^2 0.24t$, find
 - i. the velocity and the acceleration of P when t = 0,
 - ii. the value of x when P has its minimum velocity, and the speed of P at this instant,
 - iii. the positive value of t when the direction of motion of P changes.

[3]

[3]

[6]

[5]

[3]

[1]

[4]

[3]

[4]

[4]

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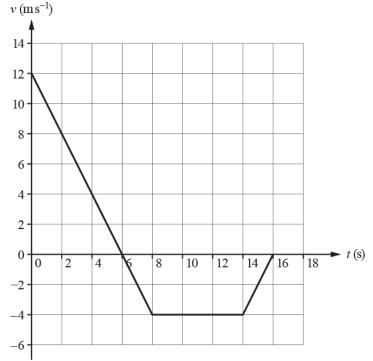
- 4. A particle *P* travels in a straight line. The velocity of *P* at time *t* seconds after it passes through a fixed point *A* is given by $(0.6t^2 + 3)$ ms⁻¹. Find
 - i. the velocity of *P* when it passes through *A*,
 - ii. the displacement of P from A when t = 1.5,
 - iii. the velocity of P when it has acceleration 6 ms⁻².
- 5. A particle *P* moves in a straight line on a horizontal surface. *P* passes through a fixed point *O* on the line with velocity 2 m s⁻¹. At time *t*s after passing through *O*, the acceleration of *P* is $(4 + 12t) \text{ m s}^{-2}$.
 - i. Calculate the velocity of P when t = 3.
 - ii. Find the distance *OP* when t = 3.

A second particle Q, having the same mass as P, moves along the same straight line. The displacement of Q from O is $(k - 2\ell)$ m, where k is a constant. When t = 3 the particles collide and coalesce.

- iii. Find the value of *k*.
- iv. Find the common velocity of the particles immediately after their collision.

[5]

[1]



A particle is moving along a straight line. The motion of the particle is modelled by the velocity-time graph shown above, where $\nu m s^{-1}$ is the velocity of the particle at time *t* s after it passes through a point *A*.

- (a) Describe the motion of the particle between times t = 0 and t = 8. [2]
- (b) Calculate the acceleration of the particle at time t = 3.
- (c) Find the displacement of the particle from A at time t = 16.

A second model for the motion of the particle is given by $v = at^2 + bt + 12$, where *a* and *b* are constants. It is given that the two models agree on the value of *v* at times t = 0, t = 6 and t = 16.

- (d) Find the values of *a* and *b*.
- (e) Hence find, according to this second model,
 - an expression in terms of *t* for the displacement of the particle from *A*,
 - the distance travelled by the particle from its position when t = 0 to its position when $t_{[5]} = 16$.
- (f) Calculate the time when the two models agree on the acceleration of the particle in the interval $0 \le t \le 8$. [2]

[1]

[3]

[2]

7. A particle moves in a straight line on a horizontal surface. At time t s after being released from rest at a point O on the line, the particle has a velocity v m s⁻¹ and a displacement from O of x m. It is given that

$$v = 0.8t^3 - 4t^2 + 5.6t.$$

Find the positive values of t at which the particle has its maximum and minimum velocities, and calculate the values of these velocities.

Express x in terms of t, and hence find the distance travelled by the particle while it is [6] decelerating.

 $v(m s^{-1})$ B 9 U 5 0 15 16 t(s)

The diagram shows the (t, v) graphs for two particles A and B which move on the same straight line. The units of v and t are m s⁻¹ and s respectively. Both particles are at the point S on the line when t = 0. The particle A is initially at rest, and moves with acceleration 0.18t m s⁻² until the two particles collide when t = 16. The initial velocity of B is U m s⁻¹ and B has variable acceleration for the first five seconds of its motion. For the next ten seconds of its motion B has a constant velocity of 9 m s⁻¹; finally B moves with constant deceleration for one second before it collides with A.

i. Calculate the value of t at which the two particles have the same velocity.

[4]

[5]

For $0 \le t \le 5$ the distance of *B* from *S* is $(Ut + 0.08t^8)$ m.

- ii. Calculate U and verify that when t = 5, B is 25 m from S.
- iii. Calculate the velocity of *B* when t = 16.

8.

[5]

[4]

A particle *P* is moving along a straight line with constant acceleration. Initially the particle is at *O*. After 9 s, *P* is at a point *A*, where OA = 18 m (see diagram) and the velocity of *P* at *A* is 8 ms⁻¹ in the direction \overrightarrow{OA} .

(a) (i)	Show that the initial speed of P is 4 ms ⁻¹ .	[2]

(ii) Find the acceleration of *P*.

B is a point on the line such that OB = 10 m, as shown in the diagram.

(b) Show that *P* is never at point *B*.

A second particle Q moves along the same straight line, but has variable acceleration. Initially Q is at O, and the displacement of Q from O at time t seconds is given by

$$x = at^{\beta} + bt^{2} + ct,$$

where *a*, *b* and *c* are constants.

It is given that

9.

- the velocity and acceleration of Q at the point O are the same as those of P at O,
- *Q* reaches the point *A* when t = 6.

(c) Find the velocity of Q at A.

- 10. The velocity $v \,\mathrm{m} \,\mathrm{s}^{-1}$ of a car at time *t s*, during the first 20 s of its journey, is given by $v = kt + 0.03t^2$, where k is a constant. When t = 20 the acceleration of the car is 1.3 m s⁻². For *t* > 20 the car continues its journey with constant acceleration 1.3 m s⁻² until its speed reaches 25 m s⁻¹.
 - (a) Find the value of *k*.
 - (b) Find the total distance the car has travelled when its speed reaches 25 m s^{-1} . [7]

[3]

[2]

[4]

Non-Uniform Acceleration 11. A particle *P* moves along the *x*-axis. At time *t* seconds the velocity of *P* is ν ms⁻¹, where $\nu = 2t^4 + kt^2 - 4$.

The acceleration of P when t = 2 is 28ms^{-2} . (a) Show that k = -9.

(b) Show that the velocity of *P* has its minimum value when t = 1.5.

When t = 1, *P* is at the point (-6.4125, 0).

(c) Find the distance of *P* from the origin *O* when *P* is moving with minimum velocity. [4]

END OF QUESTION paper

[3]

[3]

Mark scheme

a	Question		Answer/Indicative content	Marks	Part marks and guidance
1		i	(t-3)(t-6) = 0	M1	Solve 3 term QE, 2 correct coefficients if factorising, or using formula 9 +/– $\sqrt{9}$ /2
					"By inspection" both values M1A1, one value M0A0
		i	<i>t</i> = 3, 6	A1	Examiner's Comments
					Nearly all candidates gained both marks, getting their answers via factorisation.
		ii	$\nu = \int (t^2 - 9t + 18) \mathrm{d}t$	M1*	Attempts integration of <i>a</i> (<i>t</i>)d <i>t</i> , maximum one wrong term
		ii	$v = f^2/3 - 9f^2/2 + 18f(+ c)$	A1	Accept omission of + c
		ii	$3^{3}/3 - 9 \times 3^{2}/2 + 18 \times 3 + c = 9$	D*M1	Uses v(3) = 9
					Must be negative, and goes beyond $c = -13.5$
		ii	$(\nu =) -13.5 \text{ m s}^{-1}$	A 1	Examiner's Comments
		11	(v =) = 10.5 m s	A1	Attempts to use constant acceleration were rare. Nearly all candidates, correctly, went beyond their value of the integration constant, explicitly finding ν at time zero.
		iii	v(1) = 1/3 - 9/2 + 18 - 13.5 = 0.333	M1	Finds v(1) (= 1/3)
					Accurate values (v(0) = -13.5 , v(0.5) = -5.58 , v(0.9) = -0.702)
		iii	Changed sign so direction of motion has changed	A1	Examiner's Comments
					While most candidates started well, many did not make explicit the link between the change of sign for ν and a change in direction of

				motion. Finding a value of t when ν was zero was not regarded as showing a change of direction.
		Total	8	
2	i	$v = d(t^4 - 2t^6 + 5)/dt$	M1*	Differentiates displacement, one wrong term max, ignore +c
	i	$\nu = 4 \times 1.5^3 - 6 \times 1.5^2$	D*M1	Substitutes $t = 1.5$ in $v(t)$ OR solves $4t^{0} - 6t^{2} = 0$ for a +ve root
				0 + c is A0 unless c is discarded
	i	<i>v</i> = 0 AG	A1	Examiner's Comments
				This question was very well done, with constant acceleration formulae almost entirely absent.
	ii	$a = d(4t^{\beta} - 6t^{\beta})/dt$	M1*	Differentiates velocity, one wrong term max, ignore +c
	ii	$a(1.5) = 12 \times 1.5^2 - 12 \times 1.5$	D*M1	Substitutes $t = 1.5$ in $a(t)$ OR solves $12\ell - 12t = 9$ for a +ve root
				9 + c is A0 unless c is discarded
	ii	$a = 9 \text{ m s}^{-2}$ AG	A1	Examiner's Comments
				Again this was done well, with nearly all candidates demonstrating the appropriate substitution.
		Total	6	
3	i	$V = a(0.06t^3 - 0.45t^2 - 0.24t)/dt$	M1	Differentiates displacement
	i	$V = 0.18t^2 - 0.9t - 0.24$	A1	Accept with +c, unsimplified coefficients
	i	$A = d(0.18\ell - 0.9t - 0.24)/dt$	M1	Differentiates velocity
	i	A = 0.36t - 0.9	A1	Accept with +c, unsimplified coefficients
	i	$\mathcal{V}(0) = -0.24 \text{ m s}^{-1}$	A1	cao, if coeffs in <i>V</i> (<i>t</i>) wrong A0

			ft cv(–0.9), the constant in expression for A . Tolerate wrong coeff t
i	$A(0) = -0.9 \text{ m s}^{-2}$	A1ft	Examiner's Comments
·			Nearly all candidates adopted the correct methods, differentiating twice. Loss of marks mostly arose from leaving out the negative signs
			when giving the velocity and the acceleration for $t = 0$.
ii	Solves $A = 0$ for t	M1	Not if $A(1)$ includes + c in this section
ii	0.36t - 0.9 = 0	A1	
ii	<i>t</i> = 2.5	A1	
ii	x(2.5) = -2.475	A1	Final answer must be negative. Accept –2.47 and –2.48.
			Final answer must be positive. Accept 1.36 or 1.37.
			Examiner's Comments
			About half of all candidates based their answer for minimum velocity
			on $\nu = 0$. Candidates who correctly used $a = 0$ to find the correct value of <i>t</i> might sometimes mis-calculate the corresponding value of
			<i>x</i> , but were more likely than not to give the corresponding velocity,
			instead of the speed as requested. There were also a significant
			proportion of scripts where only one of the two required quantities
ii	Speed = $ u(2.5) = 1.365 \text{ m s}^{-1}$	A1	was found. (Some mark-worthy responses were based on
			candidates finding two values of t which had the same value of v .
			Candidates would then find the average these two values. As v is a quadratic function of t , the method was valid, and was marked as
			such.) About 10% of scripts contained a fully correct solution to
			Q6(ii).
			The value of t for the minimum velocity may be found by completing the square, M1.
			$0.18(t^2 - 5t - 4/3)$ gives $(t - 2.5)^2 \text{ A1}[-91/12]$ hence $t = 2.5 \text{ A1}$.
			Candidates can either return to the formula for $u(t)$ or calculate $ 0.18x $
			-91/12 .

				As $t(t)$ is a quadratic function, finding two values of t giving the same velocity identifies the mean of these t values as the time for the minimum velocity.	form Acceleration
	iii	Uses $v = 0$	M1		
	iii	$0.18\ell - 0.9t - 0.24 = 0$	A1ft	Forms and offers solution of 3 term QE using $cv(\mathcal{N})$	
				Must select +ve answer explicitly. Accept 5.3, not 5.2	
				Examiner's Comments	
		<i>t</i> = 5.25 s	A1	Was frequently left out by candidates who had used $v = 0$ in part (ii), while others simply quoted the value found previously, which (if correct) would gain full marks. A significant number of solutions foundered because candidates could not solve accurately the quadratic equation $0.18f - 0.9t - 0.24 = 0$. If the initial step in a solution was to convert the coefficients to integers, this was likely to yield $18f - 9t - 24 = 0$.	
		Total	14		
4	i	3 ms ⁻¹	B1	Examiner's Comments All three parts of this question were well answered by nearly all candidates.	MR (0.6 <i>i</i> ⁶ + 3), award B1 here
	ij	$x = \int (0.6t^2 + 3) \mathrm{d}t$	M1*	Integrates ν	MR (0.6 <i>t</i> ⁶ + 3)
	ii	$x = 0.6t^{2}/3 + 3t(+ c)$	A1	Accept with / without + c	$0.6t^4/4 + 3t$ is A0
	ii	Substitutes 1.5 in expression for x	D*M1	Needs integration and 2 terms in t	
	ii	<i>x</i> (1.5) = 5.175 m	A1	Only without +c. Accept 5.17, 5.18 Examiner's Comments	MR 5.26 only gets A1ft

				Non-Un	form Acceleration
				This part had an answer of exactly 5.175, which should be left as such, but the answer 5.18 was accepted. Inevitably some answers were based on <i>suvat</i> expressions, more commonly in (ii) where integration was needed than in (iii) which used differentiation.	
	iii	a = d(0.6f + 3)/dt	M1*	Differentiates v	MR (0.6 <i>t</i> ⁶ + 3) gives t = 1.82(57)
	iii	$6 = 2 \times 0.6t$	D*M1	Plus attempt to solve $a(t) = 6$	
		$\nu(5) = 18 \text{ ms}^{-1}$	A1	Examiner's Comments Inevitably some answers were based on <i>suvat</i> expressions, more commonly in (ii) where integration was needed than in (iii) which used differentiation.	v(1.8257) = 6.65 (3 sf)
		Total	8		
5	i	$v = \int 4 + 12t dt$	M1*	Integrates acceleration	Must see one term correct.
	i	$v = 4t + 12t^2/2(+c)$	A1	Award without (+ c)	
	i	(t = 0, v = 2) c = 2 and $v(3) = 4 \times 3 + 12 \times 3^2 / 2 (+ 2)$	D*M1	Evaluates constant	
				Examiner's Comments	
	i	$\nu = 68 \text{ m s}^{-1}$	A1	The variable acceleration and hence the need to use differentiation and integration in this question was well understood with very few cases where the use of <i>suvat</i> equations was thought appropriate. The main cause of lost marks was failure to evaluate the constant of integration. Candidates should be aware that the constant of integration is not always zero.	

ii	$\int 4t + 6\ell (+2) dt$	M1*	Integrates velocity Non-Un	form Acceleration
ii		A1ft D*M1	accept omission of d for all subsequent marks	ft on incorrect (non- zero) c from (i)
ii		A1	Examiner's Comments The variable acceleration and hence the need to use differentiation and integration in this question was well understood with very few cases where the use of suvat equations was thought appropriate. Failure to evaluate the constant of integration affected the accuracy of work in (ii). Candidates should be aware that the constant of integration is not always zero.	
iii	<i>k</i> = 132	B1ft	ft cv(78) + 54 Examiner's Comments This part was not always done correctly; answers were often incorrect because of errors made when solving a simple linear equation or because the displacement of Q was taken to be zero.	
iv	v = d(k - 2f) / dt	M1*	Differentiates displacement	
iv	$v = -2 \times 3\ell$	A1	Award even if <i>k</i> wrong earlier	
iv	$\nu(3) = -6 \times 3^2 (=-54)$	D*M1	Substitutes $t = 3$	
iv	68 <i>m</i> – 54 <i>m</i> = <i>2mv</i>	M1	Conservation of momentum, must have 2 <i>m</i> , cv(68)	No marks if <i>g</i> included, even if apparently cancelled
iv	$\nu = 7 \text{ m s}^{-1}$	A1	Examiner's Comments	

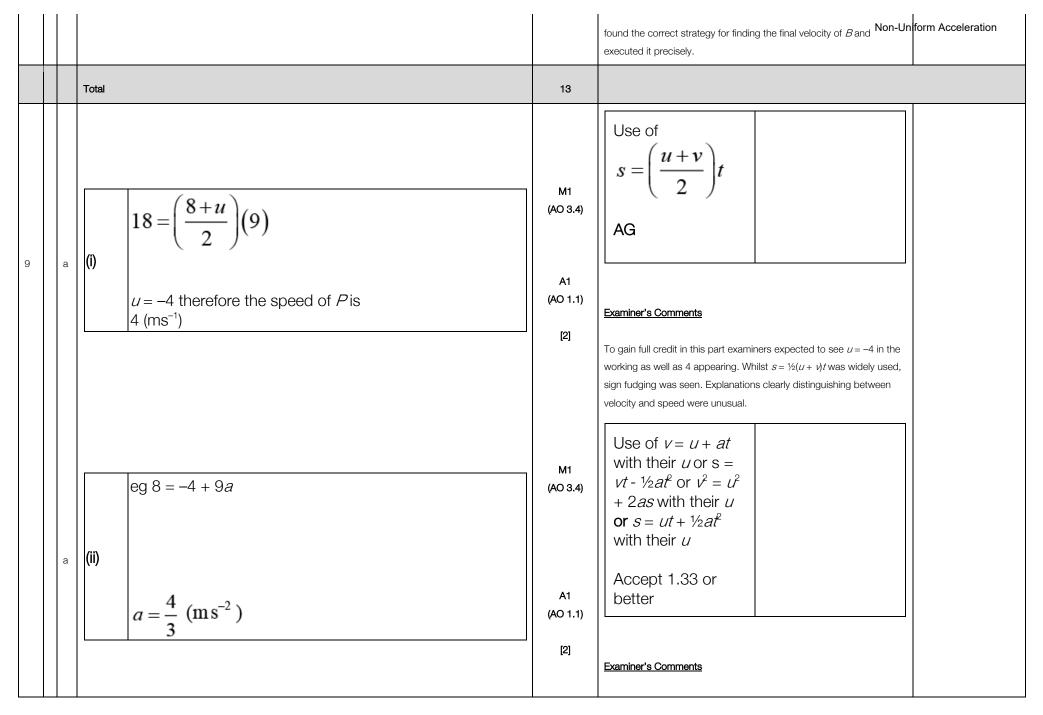
				Non-Unform Acceleration
				The differentiation was usually correct, although some lost the minus sign. The final step, requiring the use of conservation of momentum, was sometimes omitted. The most common error at the final stage was to use a mass of m instead of 2m for the after momentum.
		Total	14	
6	а	Uniform deceleration from 12 m s ⁻¹ to -4 ms ⁻¹ Changes direction after 6 seconds	E1 (AO2.4) E1 (AO2.4) [2]	One relevant comment A second relevant comment
	b	-2 m s ⁻²	B1 (AO1.1) [1]	
		Area of triangle for $0 \le t \le 6$ is $\frac{1}{2} \times 6 \times 12$	M1 (AO3.4)	
	с	Area of trapezium for $6 \le t \le 16$ is $\frac{1}{2}(10+6) \times 4$	M1 (AO1.1) A1 (AO1.1)	
		Displacement = 36 – 32 = 4 m	[3]	
	d	36a + 6b + 12 = 0 and $256a + 16b + 12 = 0$	M1 (AO1.1a)	Substitute (6, 0) and (16, 0) and

	$a = \frac{1}{8}$ and $b = -\frac{11}{4}$	A1 (AO1.1) [2]	Non-Uniform Acceleration attempt to solve resulting simultaneous equations BC
	$s = \int \left(\frac{1}{8}t^2 - \frac{11}{4}t + 12\right) dt = \frac{1}{24}t^3 - \frac{11}{8}t^2 + 12t (+c)$ $t = 0, s = 0 \Rightarrow c = 0$	M1 (AO2.1) A1 (AO1.1) A1 (AO3.4)	Attempt integration of ν (increase powers; but not just multiplication by t) Correct integration (with or without + c)
е	Distance travelled is $2\left(\frac{1}{24}(6)^{3} - \frac{11}{8}(6)^{2} + 12(6)\right) - \left(\frac{1}{24}(16)^{3} - \frac{11}{8}(16)^{2} + 12(16)\right)$ = 52.3 m (3 sf)	M1 (AO3.4) A1 (AO2.2a) [5]	Dependent on M mark but not previous A Dealing with motion both before and after $t = 6$

					Non-Ur	form Acceleration
	$ \int_{f} \frac{\frac{1}{4}t - \frac{11}{4} = -2}{t = 3 s} $	M1 (AO3.4) A1 (AO2.2a) [2]	Differentiate their <i>v</i> and equate to their value from part (b)			
		Total	15			
			M1*			
		Differentiates to find accn	A1			
		dv/dt = 3x0.8f - 2x4t + 5.6	D*M1	3 term QE and		
7	i	Solve $2.4f - 8t + 5.6 = 0$	A1	evidence of method of solution if answer incorrect.		
		<i>t</i> = 1, 2.33(33) (Accept7/3)	A1	OR t=1 and	As there are two values needed for	
		ν = 2.4 m s ⁻¹ , 1.45 m s ⁻¹		<i>v</i> =2.4 m s ⁻¹ A1 <i>OR t</i> =7/3 and	each A1 mark, accept values	
			[5]	<i>v</i> =1.45 m s ^{−1} A1	correct to 2 sig fig.	
		$x = \int 0.8t^{\theta} - 4t^{\theta} + 5.6t \mathrm{d}t$	M1			
	ii	$x = 0.8t^4 / 4 - 4t^6 / 3 + 5.6t^2 / 2 (+c)$	A1			
		$x = 0.2t^4 - 4t^8 / 3 + 2.8t^8$	A1	$x = 0.2t^{4} - 1.33t^{8} + 2.8t^{2}$	Simplified	
					coefficients and c	

				Non-Uniform Acceleration
		$x(2.3333) - x(1) = (0.2 \times 2.3333^4 - 4 \times 2.3333^3 / 3 + 2.8 \times 2.3333^2) - (0.2 \times 1^4 - 4 \times 1^3 / 3 + 2.8 \times 1^2)$	M1*	discarded
		Distance = 2.57 m	D*M1	Evaluates x at two times found from $a = 0$ These are the answers in (i)Subtraction of
			A1	values (4.23–1.67)
			[6]	Examiner's Comments
				This question was well answered by most candidates, who used calculus accurately, and used their answers in (i) to complete part (ii) successfully. The commonest mistakes arose from calculator error, and in (ii) substituting $t = 2.33 - 1 = 1.33$ into the formula for $x(t)$
		Total	11	
8	i	$A: v = \int 0.18t \mathrm{d}t$	M1*	Integration indicated by change in coefficient and
	i	$v = 0.18/2 \ \ell$ (+c)	A1	increase in power
	i	9 = 0.09 <i>f</i>	D*M1	
	i	<i>t</i> = 10	A1	Examiner's Comments Frequently this part of the question was answered correctly, with candidates integrating the acceleration of <i>A</i> .
	ii	<i>B</i> : $v = d(Ut + 0.08t^{e})/dt$	M1*	Differentiation indicated by change in coefficient and
	ii	$v = U + 0.24 f^{2}$ 9 = U + 0.24 × 5 ²	D*M1	reduction in power

ii	U = 3 SB(5) = 3 × 5 + 0.08 × 5 ³	A1	There are instances of solutions in which $SB(5) = 25$ is used to show that $U = 3$, and then demonstrate that
			SB(5) = 25. Such work can gain no marks. u = 3 without any supporting work. MOA0.
			Examiner's Comments
ii	<i>SB</i> (5) = 25 m AG	A1	This part of the question caused a large number of circular solutions to be presented (which gained no marks). Candidates could (and did) deduce that $U = 3$ from the position of <i>B</i> when $t = 5$.
			The substitution of $U = 3$ and $t = 5$ into the distance formula of <i>B</i> was then held to verify the value of 25 m. That said, the correct solution based on differentiation of the distance formula of <i>B</i> was frequently seen.
iii	$A: x = \int 0.09 f' dt x = 0.09 f' /3$	M1*	Integration of V(A)
iii	$x(16) = 0.03 \times 16^3$	D*M1	
iii	x = 122.88 (may be implied by later work)	A1	Accept 123
iii	122.88 = 25 + 10 × 9 + (9 + <i>v</i>)(<i>x</i> 1) /2	M1	
iii	v = 6.76 m s ⁻¹ OR	A1	
iii	122.88 - 25 - 10 × 9 = 9 × 1 +/-a × 1 ² /2 Deceleration = 2.24 m s ⁻² $v = 9 - 2.24 \times 1$	M1	
			$s = ut + -at^{e}/2$
iii	$\nu = 6.76 \text{ m s}^{-1}$	A1	Examiner's Comments
			There were a lot of very good answers to this demand. Candidates



				Once again the necessary methods were widely used, with $v = u + at$ the equation used most. This was often done with $u = 4$, candidates not realising the importance of the minus sign. Those who used the equation $s = vt - \frac{1}{2}at^2$ avoided this consideration here.		
		$0 = -4 + \frac{4}{3}t$	M1 (AO 3.1b)	Use of $v = u + at$ with $v = 0$ and their <i>a</i> and <i>u</i>		
		<i>t</i> = 3	A1 (AO 1.1)			
	$-s_{\max} = -4t + \frac{1}{2}\left(\frac{4}{3}\right)t^{2}$ $S_{\max} = 6 < 10 \text{ so } P \text{ is never at } B$ OR	$-s_{\max} = -4t + \frac{1}{2}\left(\frac{4}{3}\right)t^2$	M1 (AO 3.4)	Use of $s = ut + \frac{1}{2}at^2$		
		A1 (AO 2.2a) [4]	2 with their <i>a</i> , <i>u</i> & <i>t</i> Compare with 10 or suitable comment			
		M1				
		$-10 = -4t + \frac{1}{2} \left(\frac{4}{3}\right) t^2$	A1	Use of $s = ut + \frac{1}{2}at^{2}$ with their <i>u</i> and <i>a</i> and suitable <i>s</i>		
			М1			
			A1	Consider $b^2 - 4ac$ or attempt to solve three term		

	e.g. det = -24 therefore not possible		quadratic in <i>t</i>	Non-Uniform Acceleration
	OR $0 = (\pm 4)^{2} + 2\left(\frac{4}{3}\right)s \text{ or } v^{2} = (\pm 4)^{2} + 2\left(\frac{4}{3}\right)(-10)$	M2	Or 36 – 60 < 0 therefore not possible	
	$v^{2} = -\frac{32}{3}$ (3)	A1 A1	Use of $v^2 = u^2 + 2as$ with their a and u and either $v = 0$ or $s = \pm 10$	
	Suitable conclusion		Dependent on previous A mark	
			Examiner's Comments This part proved to be a challenge and, altho ways of solving the problem, candidates did intentions easy to follow. Were they consider B? Some even appeared to be considering A ½at ^e once again had sign difficulties, with <i>u</i> = quite widely.	not always make their ing the motion from O or A. Those trying $s = ut$ +
	$x = at^{\theta} + bt^{\theta} + ct$			
с	$\dot{x} = 3at^2 + 2bt + c$	M1 (AO 1.1)	Attempt to differentiate once	Two terms differentiated correctly

$\ddot{x} = 6at + 2b$	M1	Attempt to differentiate again and substitute $t = 0$ into both equations and	Non-Uniform A Two terms differentiated	cceleration
$b = \frac{2}{3}$ $18 = a(6)^{3} + \frac{2}{3}(6)^{2} - 4(6) \Longrightarrow a = \frac{1}{12}$ Velocity of $Q = \left(\frac{1}{4}(6)^{2} + \frac{4}{3}(6) - 4\right) = 13 (\text{m s}^{-1})$	(AO 2.1) A1ft (AO 1.1) A1ft (AO 1.1) A1 (AO 1.1) [5]	substitute their acceleration in their second derivative and their u in their first derivative $b = 0.5 \times$ their accel. and $c = \pm 4$ Allow $a = -\frac{5}{36}, -\frac{7}{108}, \frac{1}{108}$ which come from u = 4 cao	correctly following through from their first derivative	
	[6]	Examiner's Comments		
		Few fully correct solutions were seen to this part. Many just earned one mark for differentiating the given displacement equation, seemingly not understanding that $t = 0$ needed to be used in the work to find <i>b</i> and <i>c</i> (not $t = 6$) and then $t = 6$ needed to obtain a. A number of candidates attempted to solve this part using the constant acceleration formulae.		
Total	13			

					Non	Uniform Acceleration
			B1(AO			
		a = k + 0.06t	1.1)E			
			M1(AO			
10			1.1)E	Use of $t = 20$ and		
10	а	k + 0.06(20) = 1.3		<i>a</i> = 1.3 in their <i>a</i>		
			A1(AO 1.1)E			
		k = 1.3 - 1.2 = 0.1	,_	Examiner's Comments		
			[3]	Nearly all candidates correctly diffe correctly obtained the value of <i>k</i> as		
			M1*(AO	Attempt to		
			3.1a) E	integrate – all		
				powers increased		
				by 1 (but not just		
		$s = 0.05t^2 + 0.01t^2(+c)$	A1ft(AO	multiplying by <i>t</i>)		
			1.1)E	$s = \frac{1}{2}kt^2 + 0.01t^3$		
		$t=0, s=0 \Rightarrow c$	B1(AO	2		
			2.1) A	From a correct		
	b	<i>t</i> = 20, <i>v</i> = 14	B1ft(AO	expression for s		
		l = 20, v = 14	1.1)E	12 + 20 <i>k</i>		
			dep*M1(AO		If $c = 0$ stated then must give a reason	
		$s_1 = 0.05(20)^2 + 0.01(20)^3$	3.4) C			
				Finding distance		
				travelled after 20 <i>s</i> (for reference		
		$25^2 = 14^2 + 2(1.3)s_2$	M1(AO	$S_1 = 100$)		
			3.3) A			
				Use of $v^2 = u^2 + 2as$ with $v = 25$		
				2a5 with $V = 20$		

	Total distance = $s_1 + s_2 = 265 \text{ m}$	A1(AO 2.2a)A [7]	and $a = 1.3$ and their u Non-Un form Acceleration All previous marks must have been awarded awarded
			Examiner's Comments This part was answered extremely well with many candidates correctly finding the total distance that car had travelled when its speed had reached 25 ms ⁻¹ . Many correctly realised that they had to use integration to find an expression for the displacement in terms of t which they could then use to find the distance travelled by the car in the first 20 seconds. However, many ignored the constant of integration that would arise from the corresponding indefinite integral; even though this constant was zero it is mathematically incorrect to simply ignore it (and for full marks candidates either had to consider this displacement expressed as a definite integral or explain why the constant was zero). Most candidates then used the SUVAT equations to work out the remaining distance travelled when the speed increased from 14 to 25 and correctly calculated the total distance as 265m.
	Total	10	
11	$\frac{\mathrm{d}v}{\mathrm{d}t} = 8t^3 + 2kt$ $8(2)^3 + 2k(2) = 28$ $4K = 28 - 64 \Rightarrow k = -9$	B1 (AO 1.1) M1 (AOs 1.1) A1 (AO 2.2a) [3]	Correct expression for the accelerationSubstitute $t = 2$ into their a and equate to 28 AG

					Nan II	iform Appolaration
	b	$\frac{\mathrm{d}v}{\mathrm{d}t} = 0 \Longrightarrow 2t(4t^2 - 9) = 0$ $t = 1.5 \text{ (and } t = 0)$	M1 (AO 3.1b) A1 (AO 1.1)	Substituting the correct value of <i>k</i> and equating to zero AG Correctly finding the given	Non-U	n form Acceleration
		E.g. $\frac{d^2 v}{dt^2}\Big _{t=1.5} = 24(1.5)^2 - 18 > 0$ so a	B1 (AO 2.1)	value of <i>t</i> Showing that this value of <i>t</i> gives a	Or complete argument from the shape of the curve,	
		minimum	[3]		or from first derivatives	
	с	$s = \frac{2}{5}t^5 - 3t^3 - 4t \ (+c)$	M1* (AO 1.1a)	Attempt to integrate ν (all powers increased		
		$-6.4125 = 0.4 - 3 - 4 + c \Rightarrow c = \mathbf{K}$ $s = 0.4(1.5)^5 - 3(1.5)^3 - 4(1.5) + 0.1875$	M1dep* (AO 2.1a) M1 (AO 1.1)	by 1) Constant not Attempt to find <i>c</i> required for this first M mark		
		s = -12.9 so distance of <i>P</i> from <i>O</i> is 12.9m		Substitute 1.5 into their expression for <i>s</i> – dependent on both previous M marks	<i>c</i> = 0.1875	
			[4]			
		Total	10			