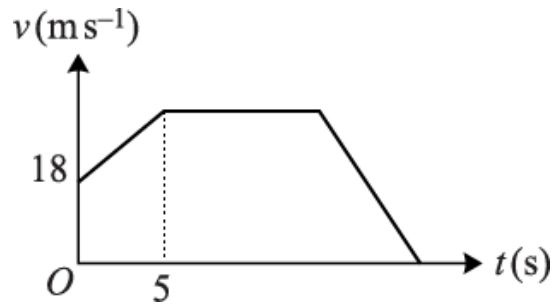


1.



The diagram shows the (t, v) graph of a car moving along a straight road, where $v \text{ m s}^{-1}$ is the velocity of the car at time $t \text{ s}$ after it passes through the point A . The car passes through A with velocity 18 m s^{-1} , and moves with constant acceleration 2.4 m s^{-2} until $t = 5$. The car subsequently moves with constant velocity until it is 300 m from A . When the car is more than 300 m from A , it has constant deceleration 6 m s^{-2} , until it comes to rest.

- i. Find the greatest speed of the car.

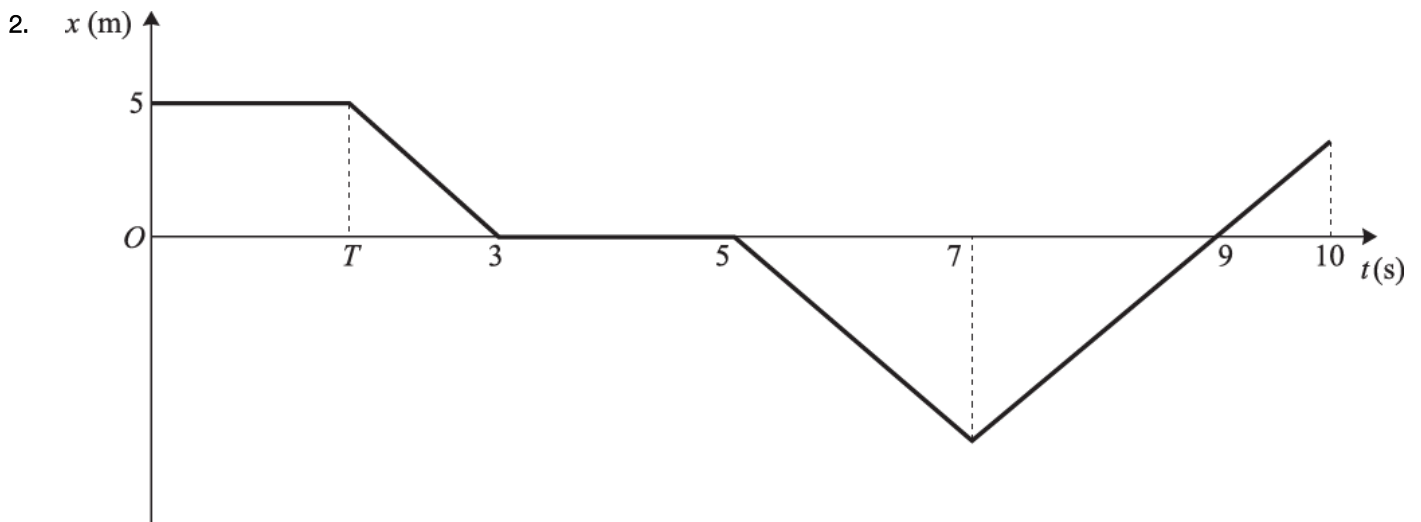
[2]

- ii. Calculate the value of t for the instant when the car begins to decelerate.

[5]

- iii. Calculate the distance from A of the car when it is at rest.

[3]



A particle P can move in a straight line on a horizontal surface. At time t seconds the displacement of P from a fixed point A on the line is x m. The diagram shows the (t, x) graph for P . In the interval $0 \leq t \leq 10$, either the speed of P is 4 ms^{-1} , or P is at rest.

- i. Show by calculation that $T = 1.75$.

[2]

- ii. State the velocity of P when

a. $t = 2$,

[1]

b. $t = 8$,

[1]

c. $t = 9$.

[1]

- iii. Calculate the distance travelled by P in the interval $0 \leq t \leq 10$.

[3]

For $t > 10$, the displacement of P from A is given by $x = 20t - t^2 - 96$.

- iv. Calculate the value of t , where $t > 10$, for which the speed of P is 4 ms^{-1} .

[4]

3. A particle P is projected vertically downwards with initial speed 3.5 ms^{-1} from a point A which is 5 m above horizontal ground.
- i. Find the speed of P immediately before it strikes the ground.

[2]

After striking the ground, P rebounds and moves vertically upwards and 0.87 s after leaving the ground P passes through A .

- ii. Calculate the speed of P immediately after it leaves the ground.

[3]

It is given that the mass of P is 0.2 kg.

- iii. Calculate the change in the momentum of P as a result of its collision with the ground.

[2]

4. A small ball is projected vertically upwards with speed 18 m s^{-1} from a point O on the ground. At the same instant a small object is released from rest at a point 27 m vertically above O .

(i) Verify that the ball and the object collide 1.5 s after they are set in motion. [4]

(ii) Find the velocities of the ball and the object immediately before they collide. [3]

The ball and the object have equal mass. When the ball and the object collide, they coalesce.

(iii) Find the time after their collision when they strike the ground at O . [5]

END OF QUESTION paper

Mark scheme

Question	Answer/Indicative content	Marks	Part marks and guidance
1	i $v = 18 + 2.4 \times 5$	M1	$v = u + at$
	i $v = 30$	A1	
	ii Distance while accelerating = $(18 + 30) \times 5/2$	B1	Or $30 \times 5 - (30 - 18) \times 5/2$ etc = 120, or 45 + 75. Numerical.
	ii Distance at constant speed = $30(t - 5)$	B1	Tolerate $30t$. Algebraic.
	ii	M1	Adds their areas to get 300
	ii $30(t - 5) + (18 + 30) \times 5/2 = 300$	A1	$30T = 300 - 120$, $30t + 45 + 75 = 300$, etc
	ii $t = 11$	A1	
	ii <i>OR</i>		
	ii Distance while accelerating = $(18 + 30) \times 5/2 (= 120)$	B1	Or $30 \times 5 - (30 - 18) \times 5/2$ etc = 120, or 45 + 75. Numerical.
	ii Distance at constant speed = $300 - cv(120)$	M1	Subtracts their area from 300
	ii Time at constant speed = $\frac{(300 - cv(120))}{30}$	B1	Equivalent to "distance at constant speed algebraic"
	ii Time at constant speed = 6	A1	
	ii $t = 11$	A1	
	ii <i>OR</i>		
	ii Distance = $30t$	B1	Rectangle, comprising 300 + area of "missing triangle"
	ii Distance = $(30 - 18) \times 5/2$	B1	"Missing triangle", to be removed
	ii $30t - (30 - 18) \times 5/2 = 300$	M1A1	Subtracts their areas to get 300
	ii $t = 11$	A1	
	ii <i>OR</i>		
	ii Distance while accelerating = $(18 + 30) \times 5/2$	B1	120
	ii Distance at constant speed = $30(t - 5)$	B1	May be implied. Tolerate $30t$. Algebraic.
	ii Distance at constant speed = $300 - 120 = 30(t - 5)$	M1A1	<i>OR</i> $180 = 30t$ M1, $t = 6$ A1
	ii $t = 11$	A1	
	ii Splitting area horizontally		

Constant Acceleration and Graphical Representation

	ii	Distance = $18t$	B1	Lower portion of area	
	ii	Distance = $(t + [t - 5]) \times (30 - 18)/2$	B1	Upper portion of area	
	ii	$18t + (t + [t - 5]) \times (30 - 18)/2 = 300$	M1A1	$30t - 30 = 300$	
	ii	$t = 11$	A1		
	iii	$S = 30^2 / (2 \times (\pm 6))$	M1	$0^2 = 30^2 \pm 2 \times 6S$, with candidate's $v(i)$	
	iii	$S = 75$	A1		
	iii	Distance = 375 m	A1ft	$300 + cv(75)$	
	iii	OR	M1	Accept $T = 5$ if no working or from $30/-6$, with candidate's $v(i)$	
	iii	$T = 30/6$ and $S = 30 T/2$			
	iii	$S = 75$	A1	$300 + cv(75)$	
	iii	Distance = 375 m	A1ft	<p>Examiner's Comments</p> <p>Many fully correct solutions were seen. The most frequent error was not realising in part (ii) that 300 m was the entire journey distance while both accelerating and moving with constant speed. Thus "300/30 = 10, 10 + 5 = 15 seconds" was the most common mistake seen. Very many candidates expressed their work in a very informal way, their solutions consisting predominantly of numbers (120, 180, 6, 11) without much explanation of what they meant.</p> <p>Candidates could directly find in part (iii) the distance while decelerating (from $0^2 = 30^2 - 2 \times 6s$), and so those who first calculated a time while decelerating needed to use that time to find a distance before becoming eligible for any mark.</p>	
	Total		10		
2	i	$5/(T - 3) = -4$ OR $5/(3 - T) = 4$	M1	Accept verification, $4 \times (3 - 1.75)$ M1	
	i	$T = 1.75$	A1	$= 5$ A1 OR $5/(3 - 1.75)$ M1 = 4 A1	
	ii	(a) -4 ms^{-1}	B1		
	ii	(b) 4 ms^{-1}	B1		
	ii	(c) 4 ms^{-1}	B1		
	iii	$2 \times (-)4, 2 \times 4, (1 \times)4$	M1*	Calculates any one unknown distance	Allow if only one

Constant Acceleration and Graphical Representation

		iii	$d = (-)5 + (-)8 + 8 + 4$	D*M1	Adds 5 and "3 other" distances or -5 and "3 other" displacements	calc. correct Note $t = 5$ to $t = 9$, $t = 5$ to $t = 10$ etc, may be one term
		iii	$d = 25 \text{ m}$	A1	Correctly comes from $4 \times (1.25 + 4 + 1) \quad 3/3$	
		iv	$v = d(20t - t^2 - 96)/dt$	M1*	Differentiates x , accept $20 - t$ as "differentiation"	
		iv	$v = 20 - 2t$	A1		
		iv	$20 - 2t = -4$	D*M1	$20 - 2t + c = -4$ is DM0 Only from $20 - 2t = -4$. This answer can arise fortuitously from solving $20t - t^2 - 96 = 0$.	
		iv	$t = 12$ (ignore any solutions less than 10)	A1	Examiner's Comments In recent examinations, a (t, v) graph has been presented to candidates. It was clear that a minority of candidates used methods inappropriate to a (t, x) diagram. Others wrongly used constant acceleration formulae, in a problem where changes of velocity are instantaneous. Only the best candidates were able to solve fully, as only they realised that a speed of 4 m s^{-1} was consistent with $v = -4$.	SC Verifying that $t = 12$ gives $v = -4$ can gain final M1A1 (A special case of trial and refinement)
		Total		12		
3		i	$v^2 = 3.5^2 + 2g \times 5$	M1	Uses $v^2 = 3.5^2 +/ - 2g5$	Accept -3.5^2 for $(-3.5)^2$ etc
		i	$v = 10.5 \text{ ms}^{-1}$	A1	Examiner's Comments Was almost always answered correctly.	
		ii		M1	$+/-5 = 0.87u +/ - g0.87^2/2$	May come from $s = vt - g^t/2$
		ii	$5 = 0.87u - g \times 0.87^2 / 2$	A1		
		ii	$u = 10.0 \text{ ms}^{-1}$	A1	Examiner's Comments This part was almost always answered correctly, save for a significant minority of candidates who	

				had the wrong sign before the term involving g . One unusual feature was the high proportion of candidates who rearranged the standard $suvat$ equation into a form which had u as its subject.																		
	iii	Change = $0.2 \times 10.5 + 0.2 \times 10$	M1	Or +/- 0.2(Ans(i)) +/- Ans(ii) It is OK get -4.1 from correct work Examiner's Comments																		
	iii	Change = $4.1(0) \text{ kg ms}^{-1}$	A1	Was nearly always answered by subtracting the magnitudes of the momentum on landing and on lift-off. A minority of candidates used the initial speed of 3.5 m s^{-1} in their calculations.																		
		Total	7																			
4	i	<table border="1" style="width: 100%; border-collapse: collapse;"> <tr> <td style="padding: 5px;">Object fall = $9.8 \times 1.5^2 / 2$</td> <td style="width: 50px;"></td> </tr> <tr> <td style="padding: 5px;">Ball rise = $18 \times 1.5 - 9.8 \times 1.5^2 / 2$</td> <td></td> </tr> <tr> <td style="padding: 5px;">Distance = $11.025 + 15.975$</td> <td></td> </tr> <tr> <td style="padding: 5px;">Distance = 27 m</td> <td style="text-align: right;">AG</td> </tr> <tr> <td style="padding: 5px;"><i>OR</i></td> <td></td> </tr> <tr> <td style="padding: 5px;">Distance fallen = $9.8t^2/2$</td> <td></td> </tr> <tr> <td style="padding: 5px;">Distance risen = $18t - 9.8t^2/2$</td> <td></td> </tr> <tr> <td style="padding: 5px;">$9.8t^2/2 + 18t - 9.8t^2/2 = 27$</td> <td></td> </tr> <tr> <td style="padding: 5px;">$t = 1.5$</td> <td style="text-align: right;">AG</td> </tr> </table>	Object fall = $9.8 \times 1.5^2 / 2$		Ball rise = $18 \times 1.5 - 9.8 \times 1.5^2 / 2$		Distance = $11.025 + 15.975$		Distance = 27 m	AG	<i>OR</i>		Distance fallen = $9.8t^2/2$		Distance risen = $18t - 9.8t^2/2$		$9.8t^2/2 + 18t - 9.8t^2/2 = 27$		$t = 1.5$	AG	<p>11.025 m</p> <p>15.975 m</p> <p>Appropriate signs and full accuracy</p> <p>B1</p> <p>B1</p> <p>M1</p> <p>A1</p> <p>[4]</p> <p>B1</p> <p>B1</p> <p>M1</p> <p>A1</p> <p>Examiner's Comments</p> <p>In part (i), candidates were asked to "verify" $t = 1.5$ which indicated that finding the distances moved by the object and ball should first be calculated. The next stage was to demonstrate that these distances added together equalled the 27 m initial gap. This stage had to be done using exact arithmetic; the use of rounded figures could lead only to the conclusion that the ball and object were very close. Some candidates successfully set</p>	<p>SC $18 \times 1.5 = 27$ B1 only but $9.8 \times 1.5^2 / 2 + 18 \times 1.5 - 9.8 \times 1.5^2 / 2 = 27$ B1B1M1A1</p> <p>$9.8t^2/2$ without the context of "distance fallen" is B0. Similarly for $18t - 9.8t^2/2$</p>
Object fall = $9.8 \times 1.5^2 / 2$																						
Ball rise = $18 \times 1.5 - 9.8 \times 1.5^2 / 2$																						
Distance = $11.025 + 15.975$																						
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$9.8t^2/2 + 18t - 9.8t^2/2 = 27$																						
$t = 1.5$	AG																					

				up and solved and equation in t containing two squared terms (which subsequently cancelled) and so showed that t = 1.5.			
	ii	<p>Object vel (=9.8 x 1.5) = 14.7 m s⁻¹ (down)</p> <p>Ball vel =+/- (18 - 9.8 x 1.5)</p> <p>Ball vel = 3.3 (upwards)</p>	<p>B1</p> <p>M1</p> <p>A1</p> <p>[3]</p>	<table border="1"> <tr> <td>Accept -14.7 m s⁻¹</td> <td>Candidates may find object velocity and ball velocity in (i). These answers must be quoted here for 3 marks to be given.</td> </tr> </table> <p>Must be a difference expression</p> <p>3.3 if v=18 or -3.3 if v=-18</p> <p>Examiner's Comments</p> <p>Part (ii) was done well.</p>	Accept -14.7 m s ⁻¹	Candidates may find object velocity and ball velocity in (i). These answers must be quoted here for 3 marks to be given.	
Accept -14.7 m s ⁻¹	Candidates may find object velocity and ball velocity in (i). These answers must be quoted here for 3 marks to be given.						
	iii	<p>$14.7m - 3.3m = 2mu$</p> <p>$u = 5.7$</p> <p>$15.975 = 5.7t + 9.8t^2 / 2$</p> <p>Solve $4.9t^2 + 5.7t - 15.975 = 0$</p> <p>$t = 1.32$ s</p>	<p>M1</p> <p>A1</p> <p>M1*</p> <p>D*M1</p> <p>A1</p> <p>[5]</p>	<table border="1"> <tr> <td>Momentum conservation; after mass = 2xbefore mass</td> <td>Disregard signs</td> </tr> </table> <p>Must use coalesced velocity and s<27</p> <p>3 term QE and evidence of method of solution if answer incorrect.</p> <p>Find v (=18.537..), solve for t D*M1 Answer t = 1.32 s</p> <p>Examiner's Comments</p> <p>Part (iii) was often accompanied by diagrams which showed a horizontal collision. The momentum equation proved awkward, with uncertainty about the direction of motion signs, both before and after coalescence, or not having the "after" mass doubled.</p>	Momentum conservation; after mass = 2xbefore mass	Disregard signs	
Momentum conservation; after mass = 2xbefore mass	Disregard signs						

			Total	12	
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