[2]

[6]

[2]

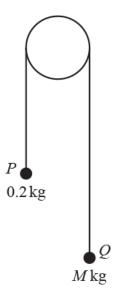
In this question the unit vectors \mathbf{i} and \mathbf{j} are in the directions east and north respectively.

Distance is measured in metres and time in seconds.

A ship of mass 100 000 kg is being towed by two tug boats. The cables attaching each tug to the ship are horizontal. One tug produces a force of $(350\mathbf{i} + 400\mathbf{j})$ N and the other tug produces a force of $(250\mathbf{i} - 400\mathbf{j})$ N. The total resistance to motion is 200 N. At the instant when the tugs begin to tow the ship, it is moving east at a speed of 1.5 m s⁻¹.

- (a) Explain why the ship continues to move directly east.
- (b) Find the acceleration of the ship. [2]
- (c) Find the time which the ship takes to move 400 m while it is being towed. Find its speed after moving that distance.

2.



Particles P and Q, of masses 0.2 kg and M kg respectively, where M > 0.2, are attached to the ends of a light inextensible string. The string passes over a smooth fixed pulley (see diagram). The system is in motion with the string taut and with each of the particles moving vertically.

The tension in the string is 2.1 N.

- (a) Show that the acceleration of P is 0.7 m s⁻².
- (b) Find the value of M. [2]
- (c) At one instant *P* has speed 0.3 m s⁻¹ upwards. Find its speed 1.5 seconds later, assuming that it has not yet reached the pulley. [1]

In this question the horizontal unit vectors **i** and **j** are in the directions east and north respectively.

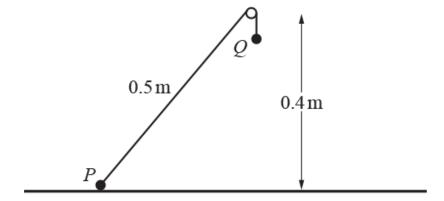
A toy car of mass 0.5 kg is moving so that its acceleration vector \mathbf{a} ms⁻² at time t seconds is given by

 $\mathbf{a} = 6t\mathbf{i} + (2 - 3t^2)\mathbf{j}$. When t = 2 the horizontal force acting on the car is \mathbf{F} N. Find

• the magnitude of F,

• the bearing of F. [5]

4.



A particle P of mass 0.4 kg is attached to one end of a light inextensible string. The string passes over a small smooth fixed pulley, and a particle Q of mass 0.1 kg is attached to the other end of the string. P rests in limiting equilibrium on a horizontal surface which is 0.4 m below the pulley, with the string taut and in the same vertical plane as P, Q and the pulley. P is 0.5 m from the pulley (see diagram).

Calculate the coefficient of friction and the magnitude of the contact force exerted on $P_{[7]}$ by the surface.

Q is now moved to the position on the surface below the pulley such that the portion of the string attached to Q is vertical. P hangs freely below the pulley and the portion of the string attached to P is vertical. Both particles are at rest when Q is released.

(ii) Find the acceleration of the particles and the tension in the string while *P* is descending. [5]

P strikes the surface and remains at rest. Q comes to instantaneous rest immediately before reaching the pulley.

(iii) Find the length of the string. [5]

In this question the horizontal unit vectors **i** and **j** are in the directions east and north respectively.

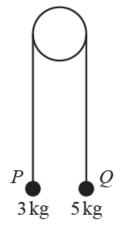
A model ship of mass 2 kg is moving so that its acceleration vector \mathbf{a} ms⁻² at time t seconds is given by

 $\mathbf{a} = 3(2t - 5)\mathbf{i} + 4\mathbf{j}$. When t = T, the magnitude of the horizontal force acting on the ship is 10 N.

Find the possible values of T.

[4]

Particles P and Q, of masses 3 kg and 5 kg respectively, are attached to the ends of a light inextensible string. The string passes over a smooth fixed pulley. The system is held at rest with the string taut. The hanging parts of the string are vertical and P and Q are above a horizontal plane (see diagram).



(a) Find the tension in the string immediately after the particles are released.

[4]

[4]

After descending 2.5 m, Q strikes the plane and is immediately brought to rest. It is given that P does not reach the pulley in the subsequent motion.

(b) Find the distance travelled by P between the instant when Q strikes the plane and the instant when the string becomes taut again.

END OF QUESTION paper

Mark scheme

Question		n	Answer/Indicative content	Marks	Guidance		
1		а	Resultant force from the tug boats is positive so it is moving east There is zero resultant force in the j direction, so it is not moving north or south	E1(AO2.2a) E1(AO2.2a)	(600i)		
		b	350 + 250 - 200 =100000 <i>a</i> Obtain 0.004 m s ⁻²	M1(AO3.3) A1(AO1.1)	Use $F = ma$. Allow sign errors and one missing force		
		С	$400 = 1.5t + \frac{1}{2}(0.004)t^{2}$ $0.002t^{2} + 1.5t - 400 = 0$ Obtain 209 (seconds) $v^{2} = 1.5^{2} + 2(0.004)(400)$ Obtain 2.33 (m s ⁻¹)	M1(AO3.1b) A1(AO1.1) M1(AO3.4) A1(AO1.1) M1(AO3.4)	Use $s = ut + \frac{1}{2}at^2$ Obtain correct quadratic. Any equivalent form Use any method to solve their quadratic If negative root given (-958.63088) this must be clearly discarded Use $v^2 = u^2 + 2as$ with their a or $v = u + at$ with their a and t Accept better (2.3345235)	Including BC Accept better (208.630877) but not 208	
			Total	10			
2		а	$a = \frac{2.1 - 0.2 \times 9.8}{0.2} = \frac{0.14}{0.2} = 0.7$	M1 (AO3.3) E1 (AO1.1) [2]	Attempt N2L for P	Must include sufficient working	

Newton's Second Law and Weight

				1	Newton's Second Law and Weight			
						to justify the given answer		
		р	Mg - T = Ma $M = 0.231 (3 sf)$	M1 (AO3.3) A1 (AO1.1) [2]	Attempt N2L for Q	0.23076923		
		С	$v = 0.3 + 0.7 \times 1.5 = 1.35 \text{ m s}^{-1}$	B1 (AO3.4)	Use of $v = u + at$ with given information			
			Total	5				
			a = 12 i – 10 j	B1 (AO1.1)	Substitute $t = 2$			
			$F = 0.5\sqrt{(12)^2 + (-10)^2}$	M1 (AO3.3)	Use of F = ma and Pythagoras			
			F= 7.81 N	A1FT (AO3.4)	Tythagorae			
3			$90 + \tan^{-1}\left(\frac{5}{6}\right)$	M1 (AO3.1a)	FT their a at $t = 2$			
			(0)	A4 (AO4 4)	$90 + \tan^{-1} \left(\frac{y}{x} \right)_{to}$			
			= 130°	A1 (AO1.1) [5]	give a 3-figure bearing			
			Total	5				
		$\sin\theta = 0.4/0.5 \text{ or } \cos\theta = 0.3/0.5$ $T = 0.1g (=0.98) \text{ N}$ i $Fr = T\cos\theta (=0.588)$	B1	θ is angle between string and horizontal				
				B1	and nonzontal			
4				M1		If two values of T		
			$Fr = T\cos\theta (= 0.588)$		CorS. T, angle do not have to be	are employed, award B1 for 0.1 <i>g</i>		
			$R = 0.4g - T\sin\theta (= 3.136)$	M1	numerical SorC. T, angle do	associated with <i>Q</i> .		
					, 5			

Newton's Second Law and Weight

				Newton's Second Law and Weight		
		μ (= 0.588 /3.136) = 3/16 or 0.1875 C^2 = 0.588 ² + 3.136 ²	A1 M1	not have to be numerical with 0.4 <i>g</i> 0.187 or 0.188 Must have two non-zero numerical values	R must be a difference of forces	
			[7]	Examiner's Comments		
				Part (i) was often incomplete as caterm "contact force". The initial part and candidates who could not find gain a majority of marks.	rt was well answered by many,	
		0.4 <i>g-T</i> = 0.4 <i>a</i>	М1	N2L for either particle, no components	Finding <i>a</i> correctly from the combined equation gets	
		<i>T</i> -0.1 <i>g</i> = 0.1 <i>a</i>	A1	correct an N2 for Po	M1A1. Using <i>a</i> in an N2L equation for <i>P</i> or <i>Q</i> can get M1, and obtaining	
	ii	0.3 <i>g</i> = 0.5 <i>a OR</i> 0.4g - 0.1g = 0.4a + 0.1a	M1	Solves two simultaneous equations	the correct value of T gets A1, hence 4 marks out of 5	
		a = 5.88 m s ⁻²	A1			
		T = 1.568 N = 1.57 N	[5]	Examiner's Comments In part (ii) many fully correct solution common error was to omit an ans		
		P descends = x m (= (2x0.4 - $\frac{1}{3}$ m) $v^2 = 2x5.88x$ (=11.76 x)	M1	Pand Q moving		
	iii	$0 = v^2 - 2g(0.4-x)$ $x = 0.25$	M1 A1	unknowns Q rising alone	Eqn has two	
		String is 0.8-0.25 m long /= 0.55 m	M1 A1		uriknowns	
		OR (P starts d m below pulley)	[5]			

	1	Newton's Second Law and Weight			na vveignt	
		$v^2 = 2x5.88(0.4 - d)$ $v^2 = 2gd$ $d = 0.15$ String is 0.4+0.15 m long $l = 0.55 \text{ m}$	M1 A1 M1 A1	Pand Q moving together Q rising alone	Eqn ha unkno Eqn ha unkno	wns as two
		Total	17	Examiner's Comments Part (iii) was challenging for most, simultaneous $v^2 = v^2 + 2as \text{ equations being unfa}$		nd solving two
		Total	17			
5		$F = \sqrt{36(2T - 5)^2 + 64}$ $36(2T - 5)^2 = 36$ $2T - 5 = \pm 1 \Rightarrow T = \dots$ $T = 2 \text{ and } T = 3$	M1* (AO 3.3) A1 (AO 1.1) Dep*M1 (AO 1.1) A1 (AO 2.2a) [4]	Correct use of $F = ma$ and Pythago Correct equation(s) both values of $Te.g.$ $10 = 2\sqrt{9(2T-5)^2}$ Attempt to solve a quadratic leading to least one value for $Te.g.$ Examiner's Comments This question proved to be challer candidates. The need to find the not well understood. For those who numerical errors sometimes marred $te.g.$ How is a sometime in the but in many cases equations like the number of candidates ignored the	at an agnitude of the solution and the solution are correct met $t_0 = 12t - 30$	the acceleration was algebraic and n. $(\pm)10 = 2(3(2t-5)i)$ hods then followed, were used. A
		Total	4			

Newton's Second Law and Weight

	Newton's Second Law and Weight				
6	а	$7-3g=3a$ $5g-T=5a$ $5g-T=5\left(\frac{T-3g}{3}\right) \Rightarrow T=$	M1* (AO 3.3) A1 (AO 1.1) Dep*M1 (AO 1.1)	Attempt N2L for <i>P</i> and <i>Q</i> – three terms, mass required, condone sign errors Eliminate <i>a</i> and attempt to solve for <i>T</i> Accept 4, 36.8	M0 for $a = 0$ or $\pm g$
		T = 36.75 (N)	A1 (AO 1.1) [4]	Examiner's Comments Whilst this standard situation was not uncommon to see attempts w after release was g or 0. Those whe equations generally produced fully errors were sometimes seen.	hich assumed the acceleration no produced initial appropriate
	b	$a = 2.45 \text{ ms}^{-2}$ $v^2 = 0 + 2(2.45)(2.5)$ $0 = 12.25 + 2h(-g)$ $(2h =) 1.25(m)$	B1 (AO 3.4) M1* (AO 3.3) Dep*M1 (AO 3.3) A1 (AO 1.1)	Use of $v^2 = u^2 + 2as$ for P with $u = 0$ Use of $v^2 = u^2 + 2as$ for P with $v = 0$ Oe Examiner's Comments We expected to see an acceleration descent of Q . Some candidates us than $u = 0$, presumably because 'dimmediately brought to rest'. Those phase of the motion sometimes distinct under gravity. Some good attempts	sed ν = 0 for this phase rather Q strikes the plane and is see who now looked at the next d not realise that it was motion
		Total	8		