

1. A particle is in equilibrium under the action of three forces in newtons given by

$$\mathbf{F}_1 = \begin{pmatrix} 8 \\ 0 \end{pmatrix}, \mathbf{F}_2 = \begin{pmatrix} 2a \\ -3a \end{pmatrix} \text{ and } \mathbf{F}_3 = \begin{pmatrix} 0 \\ b \end{pmatrix}.$$

Find the values of the constants  $a$  and  $b$ .

[3]

2. Fig. 1 shows a pile of four uniform blocks in equilibrium on a horizontal table. Their masses, as shown, are 4 kg, 5 kg, 7 kg and 10 kg.

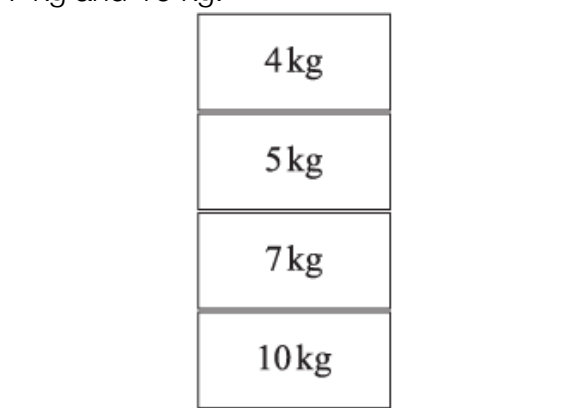


Fig.1

Mark on the diagram the magnitude and direction of each of the forces acting on the 7 kg block.

[3]

3. Fig. 3 shows a particle of weight 8 N on a rough horizontal table. The particle is being pulled by a horizontal force of 10 N. It remains at rest in equilibrium.

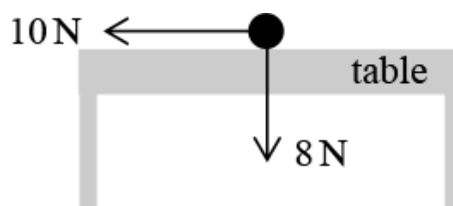


Fig. 3

(a) What information given in the question tells you that the forces shown in Fig. 3 cannot be the only forces acting on the particle?

[1]

(b) The only other forces acting on the particle are due to the particle being on the table. State the types of these forces and their magnitudes.

[2]

4. A block of mass  $5m$  kg is in equilibrium on a rough horizontal table. It is connected by horizontal light inextensible strings over smooth pulleys to particles of mass  $m$  kg and  $2m$  kg which hang freely, as shown in Fig. 3.

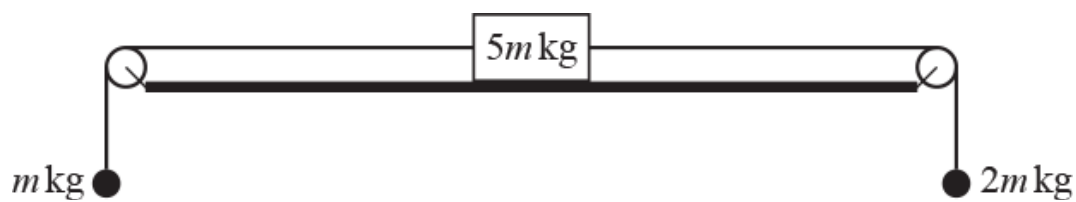


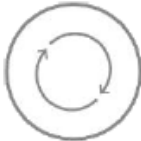
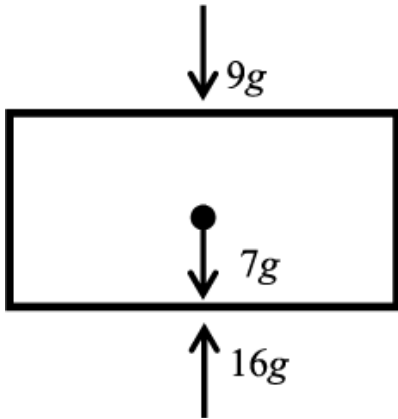
Fig. 3

Find the frictional force acting on the block, clearly indicating its direction.

[3]

END OF QUESTION paper

# Mark scheme

Question	Answer/Indicative content	Marks	Guidance
1	$\begin{pmatrix} 8 \\ 0 \end{pmatrix} + \begin{pmatrix} 2a \\ -3a \end{pmatrix} + \begin{pmatrix} 0 \\ b \end{pmatrix} = 0$ <p><math>a = -4,</math></p> <p><math>b = -12</math></p>	<p>M1 (AO2.5)</p> <p>A1 (AO1.1b)</p> <p>A1 (AO1.1b)</p> <p>[3]</p>	<div style="border: 1px solid black; padding: 5px; margin-bottom: 10px;"> <p>Setting up a correct vector equilibrium equation or two separate equations.</p> </div> <p><u>Examiner's Comments</u></p> <p>Many candidates did not form an equilibrium equation in vector form nor a pair of equilibrium equations for the two directions. Many made the mistake of writing <math>F_1 + F_2 = F_3</math> or similar and received no marks. Others had correct equations to obtain the method mark but subsequent sign errors cost the accuracy marks.</p> <div style="text-align: center;">  </div> <p>In future teaching, emphasise to candidates the importance of setting up their equilibrium equation i.e. total force = 0</p>
Total		3	
2	<div style="text-align: center;">  </div>	<p>B1</p> <p>B1</p> <p>B1</p>	<p>One mark for each force with correct magnitude and direction</p> <hr/> <p>Deduct 1 mark only for <math>g</math> missing</p> <hr/> <p>16g ↑</p> <hr/> <p>7g ↓</p> <hr/> <p>9g ↓</p>

					<p>If all three forces are correct but there is at least one extra force, deduct 1 mark and so give 2 marks. Otherwise ignore extra forces.</p> <p>Note For 16g <math>\uparrow</math> 16g <math>\downarrow</math> Award B1 B0 B0</p> <p><b>Examiner's Comments</b></p> <p>This question, about drawing a force diagram, was not well answered. Candidates were expected to identify the three forces acting on a block and to mark each of them on a given diagram. Many tried to combine two of them, even though they were quite different forces; other answers can only be described as chaotic.</p>
			<b>Total</b>	<b>3</b>	
3		a	E.g. The particle is in equilibrium [and the given forces cannot sum to zero as at 90°]	B1(AO2.2a)  [1]	oe  Accept "without another force present, the particle would be moving on a rough surface without a frictional force"
		b	<p>Friction 10 N [to give horizontal resultant of 0]</p> <p>Normal reaction from table. 8 N [to give vertical resultant of 0]</p> <p><b>Alternative method</b></p> <p>One extra force that gives equilibrium. Components 10 N <math>\rightarrow</math> and 8 N <math>\uparrow</math></p> <p>Components from Friction <math>\rightarrow</math> and normal reaction <math>\uparrow</math></p>	<p>B1(AO3.3)</p> <p>B1(AO1.2)</p> <p>B1(AO3.3)</p> <p>B1(AO1.2)</p> <p>[2]</p>	<p>oe Accept 'Because the surface is rough' for 'Friction' Oe</p> <p>oe Accept <math>\sqrt{164}</math> at <math>\approx 39^\circ</math> to horizontal</p> <p>oe Accept 'because the surface is rough' for 'Friction'</p>
			<b>Total</b>	<b>3</b>	

4		<p>Let <math>T_1</math> and <math>T_2</math> be the tensions in the strings to <math>m</math> kg mass and <math>2m</math> kg mass respectively  <math>T_1 = mg</math> and <math>T_2 = 2mg</math></p> $T_2 - T_1 - F = 0$ <p><math>F = mg</math> towards the <math>m</math> kg mass (to the left on the diagram)</p>	<p>B1(AO 3.3)</p> <p>M1(AO 3.3) A1(AO 2.2a)</p> <p>[3]</p>	<p>For values of tensions clearly stated or shown on the diagram</p>
		<p><b>Total</b></p>	<p>3</p>	