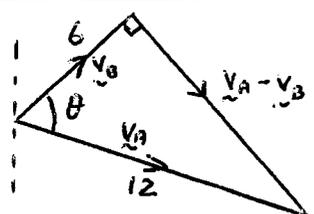


<p>1 (i)</p>	$\theta = \omega_1 t + \frac{1}{2} \alpha t^2, \quad 180 = 25 \times 5 + \frac{1}{2} \alpha \times 25$ $\alpha = 4.4 \text{ rads}^{-2}$	<p>M1 A1</p>	<p>2</p>
<p>(ii)</p>	<p>Moment = $I\alpha = 0.65 \times 4.4$ = 2.86 Nm</p>	<p>M1 A1 ft</p>	<p>2</p>
<p>2</p>	$\text{Area} = \int_0^9 \sqrt{x} \, dx = \left[\frac{2}{3} x^{\frac{3}{2}} \right]_0^9 = 18$ $\int xy \, dx = \int_0^9 x^{\frac{3}{2}} \, dx = \left[\frac{2}{5} x^{\frac{5}{2}} \right]_0^9 = 97.2$ $\bar{x} = \frac{97.2}{18}$ $= \frac{27}{5} = 5.4$ $\int \frac{1}{2} y^2 \, dx = \int_0^9 \frac{1}{2} x \, dx = \left[\frac{1}{4} x^2 \right]_0^9 = 20.25$ $\bar{y} = \frac{20.25}{18}$ $= \frac{9}{8} = 1.125$	<p>B1 B1 M1 A1 B1 M1 A1</p>	<p>For $\frac{2}{5} x^{\frac{5}{2}}$ For $\frac{1}{4} x^2$ (or $\frac{9}{2} y^2 - \frac{1}{4} y^4$)</p> <p>7</p>
<p>3 (i)</p>	$I = 0.02 + 0.12 = 0.14$ <p>Period is $2\pi \sqrt{\frac{I}{mgh}} = 2\pi \sqrt{\frac{0.14}{1.5 \times 9.8 \times 0.2}}$ = 1.37 s</p>	<p>B1 M1 A1</p>	<p>3</p>
<p>(ii)</p>	<p>WD by couple is $3.2 \times \frac{1}{2} \pi$ $3.2 \times \frac{1}{2} \pi = 1.5 \times 9.8 \times 0.2 + \frac{1}{2} (0.14) \omega^2$ $\omega = 5.46 \text{ rads}^{-1}$</p>	<p>B1 M1 A1 ft A1</p>	<p>For WD = PE + KE</p> <p>4</p>
<p>4 (i)</p>	 <p>$\cos \theta = \frac{6}{12}$ $\theta = 60^\circ$ Bearing of B's velocity is $110 - 60 = 050^\circ$</p>	<p>M1 A1 M1 A1</p>	<p>Relative velocity perpendicular to v_B Correct velocity triangle</p> <p>4</p>

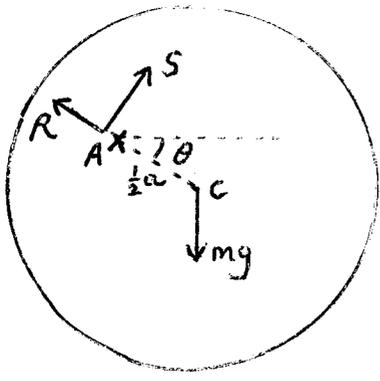
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Mark Scheme

June 2005

(ii)	As viewed from B:		M1	Considering relative displacement
			A1	
	Shortest distance is $250 \sin 40$ $= 161 \text{ m}$		M1 A1	
			4	

5	$m = \rho \int \pi y^2 dx = \rho \pi \int_0^{ka} a^2 e^{-\frac{2x}{a}} dx$ $= \rho \pi \left[-\frac{1}{2} a^3 e^{-\frac{2x}{a}} \right]_0^{ka}$ $= \frac{1}{2} \rho \pi a^3 (1 - e^{-2k})$ $I = \int \frac{1}{2} \rho \pi y^4 dx$ $= \frac{1}{2} \rho \pi \int_0^{ka} a^4 e^{-\frac{4x}{a}} dx$ $= \frac{1}{2} \rho \pi \left[-\frac{1}{4} a^5 e^{-\frac{4x}{a}} \right]_0^{ka} = \frac{1}{8} \rho \pi a^5 (1 - e^{-4k})$ $= \frac{\frac{1}{4} m a^2 (1 - e^{-4k})}{1 - e^{-2k}}$ $= \frac{\frac{1}{4} m a^2 (1 - e^{-2k})(1 + e^{-2k})}{1 - e^{-2k}} = \frac{1}{4} m a^2 (1 + e^{-2k})$	M1	Integral of $\left(e^{-\frac{x}{a}} \right)^2$
		A1	(when finding mass or volume)
			For $\int e^{-\frac{2x}{a}} dx = -\frac{1}{2} a e^{-\frac{2x}{a}}$
			For mass or volume
			Integral of y^4
			Correct integral expression (in terms of x)
			Dependent on previous M1M1
	Intermediate step not required, provided no wrong working seen		
	A1 (ag)	8	

<p>6 (i)</p>	 $I = \frac{1}{2}ma^2 + m\left(\frac{1}{2}a\right)^2$ $= \frac{3}{4}ma^2$ $mg\left(\frac{1}{2}a \cos \theta\right) = I\alpha = \left(\frac{3}{4}ma^2\right)\alpha$ $\alpha = \frac{2g \cos \theta}{3a}$	<p>M1 A1 M1 A1 (ag)</p> <p style="text-align: right;">4</p>	<p>Using parallel axes rule</p> <p>Or differentiating the energy equation</p>
<p>(ii)</p>	$\frac{1}{2}I\omega^2 = mg\left(\frac{1}{2}a \sin \theta\right)$ $\omega = \sqrt{\frac{4g \sin \theta}{3a}}$	<p>M1 A1 A1</p> <p style="text-align: right;">3</p>	<p>Using $\frac{1}{2}I\omega^2$</p>
<p>(iii)</p>	$R - mg \sin \theta = m\left(\frac{1}{2}a\right)\omega^2$ $R = \frac{5}{3}mg \sin \theta$ <hr style="border-top: 1px dashed black;"/> $mg \cos \theta - S = m\left(\frac{1}{2}a\right)\alpha$ $S = \frac{2}{3}mg \cos \theta$ <hr style="border-top: 1px dashed black;"/> <p>OR</p> $S\left(\frac{1}{2}a\right) = I_G \alpha$ $S\left(\frac{1}{2}a\right) = \left(\frac{1}{2}ma^2\right)\alpha$ $S = \frac{2}{3}mg \cos \theta$	<p>B1 M1 A1</p> <hr style="border-top: 1px dashed black;"/> <p>B1 M1 A1</p> <hr style="border-top: 1px dashed black;"/> <p>M1 A1 A1</p>	<p>For radial acc'n of C is $\left(\frac{1}{2}a\right)\omega^2$ $\pm R \pm mg \sin \theta = m r \omega^2$ or $k m a \omega^2$ (with numerical k)</p> <hr style="border-top: 1px dashed black;"/> <p>For transverse acc'n of C is $\left(\frac{1}{2}a\right)\alpha$ as above</p> <p>6 Direction must be clear</p> <p><i>Equations involving horizontal and vertical components can earn B1M1B1M1</i></p> <hr style="border-top: 1px dashed black;"/> <p>Must use I_G</p>

7 (i)	$RB^2 = a^2 + (2a)^2 - 2(a)(2a)\cos(\theta + \frac{1}{4}\pi)$ $= 5a^2 - 4a^2(\cos\theta\cos\frac{1}{4}\pi - \sin\theta\sin\frac{1}{4}\pi)$ $= a^2(5 - 2\sqrt{2}\cos\theta + 2\sqrt{2}\sin\theta)$	M1 A1 (ag) 2	
(ii)	$V = -mg(2a\sin\theta) + \frac{mg\sqrt{2}}{2a} \times RB^2$ $= \frac{5}{2}\sqrt{2}mga - 2mga\cos\theta$ $\frac{dV}{d\theta} = 2mga\sin\theta$ <p>When $\theta = 0$, $\frac{dV}{d\theta} = 0$, hence equilibrium</p> $\frac{d^2V}{d\theta^2} = 2mga\cos\theta$ <p>When $\theta = 0$, $\frac{d^2V}{d\theta^2} = 2mga > 0$, hence stable</p>	M1 A1 M1 A1 M1 A1 6	Considering PE and EE Correctly shown or other method for max / min Correctly shown
(iii)	<p>KE is $\frac{1}{2}m(2a\dot{\theta})^2$</p> $\frac{5}{2}\sqrt{2}mga - 2mga\cos\theta + 2ma^2\dot{\theta}^2 = E$ <p>Differentiating w.r.t. t,</p> $2mga\sin\theta\dot{\theta} + 4ma^2\dot{\theta}\ddot{\theta} = 0$ $\ddot{\theta} = -\frac{g}{2a}\sin\theta$ <hr/> <p>OR $(mg\cos\theta - T\sin\phi)(2a) = I\ddot{\theta}$, where</p> $T = \frac{mg\sqrt{2}(RB)}{a} \text{ and } \frac{\sin\phi}{a} = \frac{\sin(\theta + \frac{1}{4}\pi)}{RB}$ $\ddot{\theta} = -\frac{g}{2a}\sin\theta$ <hr/> <p>Period is $2\pi\sqrt{\frac{2a}{g}}$</p>	B1 M1 M1 A1 M2 A2 B1 ft 5	Requires fully correct working or $mg\cos\theta - T\sin\phi = m(2a\ddot{\theta})$ Give A1 if just one minor error ft provided that k is in terms of a and g only