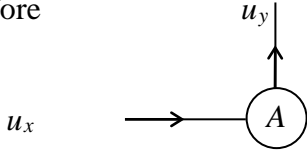
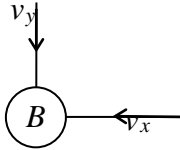
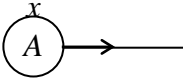
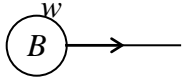


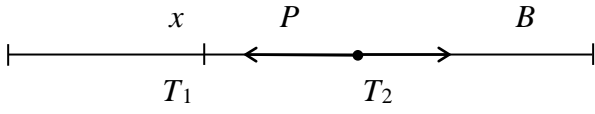
EDEXCEL 6680 MECHANICS M4 JANUARY 2004 MARK SCHEME

Question Number	Scheme	Marks
1.	<p>N2L $-2v = 3a$</p> <p>$-2v = 3v \frac{dv}{ds}$</p> <p>$s = -\frac{3}{2}v(+c)$ or $v = -\frac{2}{3}s(+c)$ cancelling v and integrating</p> <p>$s = 0, v = 5 \Rightarrow c = \frac{15}{2}$ or $s = \left[-\frac{3}{2}v\right]_5^2$</p> <p>Distance travelled is 4.5 m</p>	<p>M1</p> <p>A1</p> <p>M1</p> <p>M1</p> <p>A1</p> <p>(5 marks)</p>
2.	<p>(a) Before</p> <div style="display: flex; justify-content: space-around; align-items: center;"> <div style="text-align: center;">  </div> <div style="text-align: center;">  </div> </div> <p>A: \uparrow $u_y = 2.5 \sin \alpha = 2.5 \times \frac{4}{5} = 2 \text{ (ms}^{-1}\text{)}$ either</p> <p>\rightarrow $u_x = 2.5 \cos \alpha = 2.5 \times \frac{3}{5} = 1.5 \text{ (ms}^{-1}\text{)}$ both</p> <p>B: \downarrow $v_y = 1.3 \sin \beta = 1.3 \times \frac{12}{13} = 1.2 \text{ (ms}^{-1}\text{)}$ either</p> <p>\leftarrow $v_x = 1.3 \cos \beta = 1.3 \times \frac{5}{13} = 0.5 \text{ (ms}^{-1}\text{)}$ both</p> <p>(b) After</p> <div style="display: flex; justify-content: space-around; align-items: center;"> <div style="text-align: center;">  </div> <div style="text-align: center;">  </div> </div> <p>LM $2x + w = 3 - 0.5 \text{ (= 2.5)}$</p> <p>NEL $w - x = \frac{1}{2} \times 2 \text{ (= 1)}$</p> <p>Solving $x = 0.5, y = 1.5$ M1 solving for either</p> <p>Speed of A is $\sqrt{(2^2 + 0.5^2)} = \sqrt{4.25} \approx 2.1 \text{ (ms}^{-1}\text{)}$ M1 either</p> <p>Speed of B is $\sqrt{(1.2^2 + 1.5^2)} = \sqrt{3.69} \approx 1.9 \text{ (ms}^{-1}\text{)}$</p> <p>(13 marks)</p> <p><i>Note: Not 1 d.p. loses maximum of one mark</i></p>	<p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>(4)</p> <p>M1 A1 ft</p> <p>M1 A1 ft</p> <p>M1 A1</p> <p>M1 A1</p> <p>A1</p> <p>(9)</p>


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Question Number	Scheme	Marks
3.	(a) $AP = s - AD - DE$ $= s - L - 2L \sin \theta$	M1 A1 (2)
	(b) $V(\theta) = 2 \times 2mg \times L \cos \theta + \dots$ $= \dots + mg(2L \cos \theta - AP)$ $= 4mgL \cos \theta + mg(2L \cos \theta + 2L \sin \theta) (+C)$ $= 2mgL(3 \cos \theta + \sin \theta) + \text{constant} (*) \quad \text{cso}$	B1 M1 M1 A1 (4)
	(c) $V'(\theta) = 2mgL(-3 \sin \theta + \cos \theta)$ $= 0$ $\tan \theta = \frac{1}{3}$ $\theta \approx 18^\circ \quad \text{awrt } 18^\circ, 0.32^c$	M1 M1 A1 A1 (4)
	(d) $V''(\theta) = 2mgL(-3 \cos \theta - \sin \theta)$ $\left(V''\left(\arctan \frac{1}{3}\right) = -2\sqrt{10}mgL \right)$ $V''(\theta) < 0, \text{ for any acute } \theta$ Equilibrium is <u>unstable</u> ft any acute θ	M1 A1 M1 A1 ft (4) (14 marks)

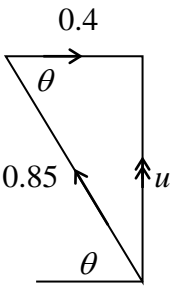
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Question Number	Scheme	Marks
4.	<p>(a) </p> <p>HL $T_1 = \frac{2mk^2L(0.5L+x)}{L}$ either M1</p> <p>HL $T_2 = \frac{2mk^2L(0.5L-x)}{L}$ both A1</p> <p>N2L $T_2 - T_1 - 2mk \frac{dx}{dt} = m \frac{d^2x}{dt^2}$ M1 A1, A1</p> <p>$4mk^2x - 2mk \frac{dx}{dt} = m \frac{d^2x}{dt^2}$</p> <p>$\frac{d^2x}{dt^2} + 2k \frac{dx}{dt} + 4k^2x = 0$ * cso A1 (6)</p> <p>(b) $m^2 + 2km + 4m^2 = 0$ ae M1</p> <p>$m = -k \pm k\sqrt{3}i$ M1</p> <p>$x = e^{-kt} (A \cos \sqrt{3}kt + B \sin \sqrt{3}kt)$ oe A1</p> <p>$t = 0, x = \frac{L}{2} \Rightarrow A = \frac{L}{2}$ B1</p> <p>$\dot{x} = -k e^{-kt} (A \cos \sqrt{3}kt + B \sin \sqrt{3}kt)$</p> <p>$+ \sqrt{3}k e^{-kt} (-A \sin \sqrt{3}kt + B \cos \sqrt{3}kt)$ M1</p> <p>$t = 0, \dot{x} = 0 \Rightarrow 0 = -kA + \sqrt{3}kB$ M1</p> <p>$B = \frac{1}{\sqrt{3}} A = \frac{L}{2\sqrt{3}}$ A1</p> <p>$AP = 1.5L + \frac{L}{2\sqrt{3}} e^{-kt} (\sqrt{3} \cos \sqrt{3}kt + \sin \sqrt{3}kt)$ oe A1 (8)</p> <p><i>Alternatives forms of the answer are given on the next page</i></p>	<p>(14 marks)</p>

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Question Number	Scheme	Marks
4.	<p>(b) <i>Alternative form of the General Solution</i> As before</p> $x = Ae^{-kt} \cos(\sqrt{3kt} - \varepsilon)$ $t = 0, x = \frac{L}{2} \Rightarrow \frac{L}{2} = A \cos(-\varepsilon) (= A \cos \varepsilon)$ $\dot{x} = -kAe^{-kt} \cos(\sqrt{3kt} - \varepsilon) - \sqrt{3k}Ae^{-kt} \sin(\sqrt{3kt} - \varepsilon)$ $t = 0, \dot{x} = 0 \Rightarrow 0 = -kA \cos \varepsilon - \sqrt{3k}A \sin(-\varepsilon)$ <p>Leading to $\tan \varepsilon = \frac{1}{\sqrt{3}} \Rightarrow \varepsilon = \frac{\pi}{6}$ and $A = \frac{L}{\sqrt{3}}$ both</p> $AP = 1.5L + \frac{L}{\sqrt{3}} e^{-kt} \cos\left(\sqrt{3kt} - \frac{\pi}{6}\right)$ <p>Note: Another possible trig form is $\sin\left(\sqrt{3kt} + \frac{\pi}{3}\right)$</p>	<p>M1 M1 A1 B1 M1 M1 A1 A1 (8)</p>
5.	<p>(a) Before After</p>  <p>→ LM $600u = 800x$ → NEL $x = eu$ $e = 0.75$</p> <p>(b) Van N2L $-500 = 800a$ $0^2 = x^2 - 2 \times 0.625 \times 45$, $x^2 = 56.25$ ($x = 7.5$) Car N2L $-300 = 600a$ $0^2 = v^2 - 2 \times 0.5 \times 21$, $v^2 = 21$ From (a) NEL $u = \frac{4}{3} \times 7.5 = 10$ $V^2 = 10^2 + 21$, $\Rightarrow V = 11$ (ms^{-1}) cao</p>	<p>M1 A1 M1 A1 A1 (5) M1 M1, A1 M1 M1, A1 M1 M1, A1 (9) (14 marks)</p>

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Question Number	Scheme	Marks	
6.	 <p>(a) Vector ! or ←</p> $\cos \theta = \frac{0.4}{0.85}$ $\theta \approx 61.9^\circ \quad \text{awrt } 62^\circ$ <p>(b) $u = \sqrt{(0.85^2 - 0.4^2)}$ or $u = 0.85 \sin \theta$</p> $t = \frac{60}{u} = \frac{60}{0.75} = 80 \quad (\text{s}) \quad \text{cao}$	M1 M1 A1 (3) M1 M1 A1 (3)	
	<p>(c) $\mathbf{v}_{N \text{ rel } W} = -0.4\mathbf{i} + 0.75\mathbf{j}$ Allow for $\pm 0.4\mathbf{i}$</p> $\mathbf{v}_N = \mathbf{v}_{N \text{ rel } W} + 0.5\mathbf{i} = 0.1\mathbf{i} + 0.75\mathbf{j} \quad 0.1\mathbf{i}$ $t = \frac{40}{0.75} = \frac{160}{3}$ $\delta = 0.1 \times \frac{160}{3} = \frac{16}{3} \quad \text{awrt } 5.3$	M1 A1 M1 M1 A1 (5)	
	<p>(d) As in (c) $\mathbf{v}_N = -0.2\mathbf{i} + 0.75\mathbf{j}$ $\pm 0.2\mathbf{i}$</p> $t = \frac{20}{0.75} = \frac{80}{3}$ $\delta = 0.2 \times \frac{80}{3} = \frac{16}{3}$ <p>Hence N lands at D cso</p>	M1 M1 M1 A1 (4)	
	<p>Notes:</p> <ol style="list-style-type: none"> In (c) and (d), the candidate can take components without using vectors. Mark as vector method. After the first line in (d), the result is clear by proportion. Allow as long as some explanation given. $\cos \theta = \frac{8}{17} = 0.4705\dots$, $\sin \theta = \frac{15}{17} = 0.8823\dots$ Alternatives to (c) and (d), using vector triangles are given on the next page. 		(15 marks)

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Question Number	Scheme	Marks
6.	<p data-bbox="347 282 687 315"><i>Alternatives to (c) and (d)</i></p> <p data-bbox="284 376 323 409">(c)</p> <div data-bbox="376 434 724 763"> </div> $v^2 = 0.5^2 + 0.85^2 - 2 \times 0.5 \times 0.85 \times \cos \theta$ $= 0.5725 \quad (v = \frac{\sqrt{229}}{20} \approx 82.4^\circ)$ $\frac{\sin \phi}{0.85} = \frac{\sin \theta}{v}$ $\sin \phi = \frac{15}{\sqrt{229}} \quad (\approx 0.9912; \phi \approx 82.4^\circ)$ $\frac{\delta}{40} = \cot \phi; \quad \delta = 40 \times \frac{2}{5} = \frac{16}{3} \text{ awrt } 5.3$ <p data-bbox="180 813 220 846">(d)</p> $w^2 = 0.2^2 + 0.85^2 - 2 \times 0.2 \times 0.85 \times \cos \theta$ $= 0.6025 \quad \left(w = \frac{\sqrt{241}}{20} \approx 0.7762... \right)$ <div data-bbox="432 898 687 1256"> </div> $\frac{\sin \psi}{0.85} = \frac{\sin \theta}{w}$ $\sin \psi = \frac{15}{\sqrt{241}} \quad (\approx 0.9662; \psi \approx 104.9^\circ)$ <p data-bbox="772 1104 1023 1137">$\psi = 75.1^\circ$ gains M1</p> $\frac{\epsilon}{20} = \cot(180^\circ - \psi) = \frac{4}{15}$ $\epsilon = \frac{16}{3} = \delta$ <p data-bbox="772 1305 1161 1339">Hence N lands at D cso</p> <p data-bbox="347 1379 1118 1485"><i>Note: Exact working is needed for final A1 but all previous marks in (c) and (d) may be gained by approximate working.</i></p>	<p data-bbox="1289 461 1337 495">M1</p> <p data-bbox="1289 546 1337 580">M1</p> <p data-bbox="1289 631 1337 665">A1</p> <p data-bbox="1289 716 1445 750">M1 A1 (5)</p> <p data-bbox="1289 875 1337 909">M1</p> <p data-bbox="1289 1034 1337 1068">M1</p> <p data-bbox="1289 1240 1337 1274">M1</p> <p data-bbox="1289 1303 1445 1337">A1 (4)</p>