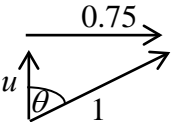
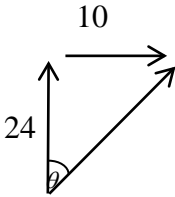
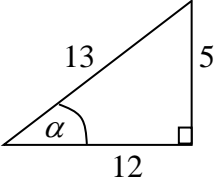


Question Number	Scheme	Marks
1.	<p>Let boy's velocity be <math>\begin{matrix} \uparrow u \\ \longrightarrow 0.75 \end{matrix}</math></p> <p>Speed = 1 <math>\Rightarrow 1^2 = u^2 + \frac{9}{16}, \therefore u^2 = \frac{7}{16}</math> or <math>u = \frac{\sqrt{7}}{4}</math> or 0.661...</p> <p>Time = <math>\frac{100}{\sqrt{7}/4} = 151.18... = 151\text{s}</math></p>  <p><math>\sin \theta = \frac{0.75}{1} \Rightarrow \theta = 48.6</math></p> <p><math>\therefore</math> Bearing is <math>049^\circ</math> or <math>048.6^\circ</math></p>	<p>M1</p> <p>M1 A1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>(6)</p> <p><b>(6 marks)</b></p>
2.	<p>Let wind be <math>\begin{matrix} \uparrow W_y \\ \longrightarrow W_x \end{matrix}</math></p> <p>Relative to A: <math>\begin{matrix} \uparrow W_y \\ \longrightarrow W_x - 10 \end{matrix}</math> From South, <math>\Rightarrow W_x = 10</math></p> <p>Relative to B: <math>\begin{matrix} \uparrow W_y - 14 \\ \longrightarrow W_x \end{matrix}</math> From SW, <math>\Rightarrow W_y - 14 = W_x \therefore W_y = 24</math></p> <p><math>\therefore</math> Magnitude of <math>W = \sqrt{10^2 + 24^2} = 26 \text{ km h}^{-1}</math></p>  <p><math>\tan \alpha = \frac{10}{24} \Rightarrow \alpha = 22.6</math></p> <p><math>\therefore</math> Bearing <math>023^\circ</math> or <math>022.6^\circ</math></p>	<p>M1</p> <p>M1, A1</p> <p>M1, A1</p> <p>A1</p> <p>A1</p> <p><b>(7 marks)</b></p>

Question Number	Scheme	Marks
3.	$(\downarrow) \quad mg - mkv^2 = ma$ $g - kv^2 = v \frac{dv}{dx}$ $x = \int \frac{v}{g - kv^2} dv$ $x = -\frac{1}{2k} \ln  g - kv^2  + c$ $x = 0, v = 0 \Rightarrow 0 = -\frac{1}{2k} + c$ $x = \frac{1}{2k} \ln \left  \frac{g}{g - kv^2} \right $ $e^{2kx} = \frac{g}{g - kv^2}$ $kv^2 = g(1 - e^{-2kx})$ $v = \sqrt{\frac{g}{k}(1 - e^{-2kD})}$	<p>M1 A1</p> <p><math>v \frac{dv}{dx}</math> M1</p> <p>M1</p> <p>M1 A1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>must use <math>D</math> A1</p> <p><b>(11 marks)</b></p>

Question Number	Scheme	Marks
4. (a)	P.E.of rod = $mg \times 2a \sin 2\theta$ $AC = a \cot \theta$ EPE in String = $\frac{1}{2} \times \frac{3}{4} \times \frac{mg}{a} (a \cot \theta - a)^2$ Total P.E $V = mg \cdot 2a \sin 2\theta + \frac{3}{8} \frac{mg}{a} (a \cot \theta - a)^2$ $= \frac{mga}{8} [16 \sin 2\theta + 3 \cot^2 \theta - 6 \cot \theta + 3]$ i.e. $V = \frac{mga}{8} [16 \sin 2\theta + 3 \cot^2 \theta - 6 \cot \theta] + \text{const} \quad (*)$	B1 B1 M1 A1 M1 M1 A1 cso (7)
(b)	$\frac{dv}{d\theta} = \frac{mga}{8} [32 \cos 2\theta - 6 \cot \theta \operatorname{cosec}^2 \theta + 6 \operatorname{cosec}^2 \theta]$ $\left. \frac{dv}{d\theta} \right _{\theta=0.535} = \frac{mga}{8} (-0.5^{0.1\dots\dots})$ $\left. \frac{dv}{d\theta} \right _{\theta=0.545} = \frac{mga}{8} (0.2^{99\dots\dots})$ Change of sign $\therefore \frac{dv}{d\theta} = 0$ in range, so $\exists$ find a position of equilibrium	M1 A2, 1, 0 M1 A1 A1 (6)
(c)	$\left. \frac{dv}{d\theta} \right _{0.535} < 0, \left. \frac{dv}{d\theta} \right _{0.545} > 0$ So turning point is <i>minimum</i> , $\therefore$ equilibrium is <i>stable</i>	M1 A1, A1 (3) <b>(16 marks)</b>

Question Number	Scheme	Marks
5.	<p>(a) Auxiliary Equation.: <math>m^2 + 2m + 2 = 0, \Rightarrow m = -1 \pm i</math></p> <p><math>\therefore</math> Complementary. Function is: <math>x = e^{-t} (A \cos t + B \sin t)</math></p> <p>Let <math>x = p \cos 2t + q \sin 2t, \dot{x} = -2p \sin 2t + 2q \cos 2t, \ddot{x} = -4x</math></p> <p>Sub. in D.E.</p> $-2p \cos 2t - 2q \sin 2t - 4p \sin 2t + 4q \cos 2t = 12 \cos 2t - 6 \sin 2t$ $-2p + 4q = 12, -4p - 2q = -6$ $-10p = 0 \Rightarrow p = 0, q = 3$ <p><math>\therefore x = 3 \sin 2t + e^{-t} (A \cos t + B \sin t)</math></p> <p><math>t = 0, x = 0 \Rightarrow 0 = A</math></p> $\dot{x} = 6 \cos 2t - e^{-t} B \sin t + e^{-t} B \cos t$ <p><math>t = 0, \dot{x} = 0 \Rightarrow 0 = 6 + B \therefore B = -6</math></p> <p><math>\therefore x = 3 \sin 2t - 6 e^{-t} \sin t</math></p> <p>(b) <math>\dot{x} = 6[\cos 2t + e^{-t} \sin t - e^{-t} \cos t]</math></p> <p>Sub <math>t = \frac{\pi}{4} \dot{x} = 6[\cos 2t + e^{-t} - 6 e^{-t} \cos t]</math></p> $\dot{x} = 6 \left[ 0 + e^{-\frac{\pi}{4}} \times \frac{1}{\sqrt{2}} - e^{-\frac{\pi}{4}} \times \frac{1}{\sqrt{2}} \right] = 0$ <p><math>\therefore P</math> comes to instantaneous rest when <math>t = \frac{\pi}{4}</math></p> <p>(c) sub <math>t = \frac{\pi}{4}</math> in <math>x = 3 \sin \frac{\pi}{2} - 6 e^{-\frac{\pi}{4}} \frac{1}{\sqrt{2}}, = 1.07</math></p> <p>(d) <math>t \rightarrow \infty \quad x \approx 3 \sin 2t,</math> approximate period is <math>\pi</math></p>	<p>M1, A1</p> <p>M1 ft</p> <p>M1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>B1</p> <p>M1</p> <p>A1 (11)</p> <p>M1</p> <p>A1 (2)</p> <p>M1, A1 (2)</p> <p>M1, A1 (2)</p> <p>(17 marks)</p>

Question Number	Scheme	Marks
<p>6. (a)</p>	 <p><math>P</math> before: <math>\rightarrow \frac{13u}{12} \cos \alpha = u</math>, <math>\uparrow \frac{13u}{12} \sin \alpha = \frac{5u}{12}</math></p> <p> <math>\begin{matrix} \rightarrow u &amp; \rightarrow 0 &amp; \rightarrow v &amp; \rightarrow \frac{3u}{5} \\ \bullet &amp; \bullet &amp; \bullet &amp; \bullet \\ m &amp; 2m &amp; m &amp; 2m \end{matrix}</math> </p> <p>PCLM (<math>\rightarrow</math>) <math>mu = mv + 2m \frac{3u}{5} \Rightarrow v = \frac{-u}{5}</math>, i.e. <math>\frac{u}{5} // CB</math></p> <p>(b) NLI <math>\rightarrow eu = v_2 - v_1 \Rightarrow eu = \frac{3u}{5} - \frac{u}{5}</math>, i.e. <math>e = \frac{4}{5}</math></p> <p>(c) <math>Q \rightarrow C</math> <math>t_1 = \frac{d_1}{3u/5} = \frac{5d_1}{3u}</math></p> <p><math>P</math> travels <math>\frac{u}{5} \times \frac{5d_1}{3u} = \frac{d_1}{3}</math> in direction <math>CB</math></p> <p><math>\therefore P</math> is <math>d_1 + \frac{d_1}{3} = \frac{4d_1}{3}</math> from <math>w</math> (*)</p> <p>(d) After hitting <math>w</math>, <math>Q</math> has speed <math>\frac{3u}{10}</math> in direction <math>CB</math></p> <p>Velocity of <math>Q</math> relative to <math>P</math> in direction <math>CB</math> is <math>\frac{u}{10}</math></p> <p>Time for <math>Q</math> to travel <math>\frac{4}{3}d_1</math> is: <math>\frac{4d_1}{3u} \times 10 = \frac{40d_1}{3u}</math></p> <p>Total time between collisions is: <math>\frac{40d_1}{3u} + \frac{5d_1}{3u} = \frac{15d_1}{u}</math> (*)</p> <p>(e) For collision to occur <math>P</math> must travel <math>\uparrow d_2</math> and <math>\downarrow d_2</math> in time <math>\frac{15d_1}{u}</math></p> <p><math>d_2 \uparrow</math> <math>t_2 = \frac{d_2}{5u/12} = \frac{12d_2}{5u}</math></p> <p><math>\downarrow d_2</math> velocity <math>\downarrow</math> is <math>\frac{5u}{24}</math>, <math>\therefore t_3 = \frac{d_2}{5u/24} = \frac{24d_2}{5u}</math></p> <p>Total time is <math>\frac{36d_2}{5u} = \frac{15d_1}{u}</math>,</p> <p><math>\therefore 12d_2 = 25d_1</math>, i.e. <math>d_1:d_2 = 12:25</math></p>	<p>B1, B1</p> <p>M1 A1 (4)</p> <p>M1, A1 (2)</p> <p>B1</p> <p>M1</p> <p>A1 c.s.o (3)</p> <p>B1</p> <p>M1</p> <p>A1</p> <p>A1 c.s.o (4)</p> <p>B1</p> <p>B1, B1</p> <p>M1</p> <p>A1 (5)</p> <p><b>(18 marks)</b></p>

