

# GCE Examinations

## Mechanics

### Module M3

Advanced Subsidiary / Advanced Level

Paper F

Time: 1 hour 30 minutes

#### *Instructions and Information*

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Candidates may use any calculator except those with a facility for symbolic algebra and/or calculus.

Full marks may be obtained for answers to ALL questions.

Mathematical and statistical formulae and tables are available.

This paper has 6 questions.

When a numerical value of  $g$  is required, use  $g = 9.8 \text{ m s}^{-2}$ .

#### *Advice to Candidates*

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You must show sufficient working to make your methods clear to an examiner. Answers without working will gain no credit.



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1. A particle  $P$  of mass  $1.5 \text{ kg}$  moves from rest at the origin such that at time  $t$  seconds it is subject to a single force of magnitude  $(4t + 3) \text{ N}$  in the direction of the positive  $x$ -axis.

(a) Find the magnitude of the impulse exerted by the force during the interval  $1 \leq t \leq 4$ .

**(3 marks)**

Given that at time  $T$  seconds,  $P$  has a speed of  $22 \text{ m s}^{-1}$ ,

(b) find the value of  $T$  correct to 3 significant figures.

**(5 marks)**

2.

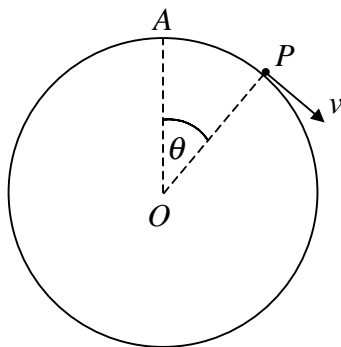


Fig. 1

A particle  $P$  of mass  $0.5 \text{ kg}$  is at rest at the highest point  $A$  of a smooth sphere, centre  $O$ , of radius  $1.25 \text{ m}$  which is fixed to a horizontal surface.

When  $P$  is slightly disturbed it slides along the surface of the sphere. Whilst  $P$  is in contact with the sphere it has speed  $v \text{ m s}^{-1}$  when  $\angle AOP = \theta$  as shown in Figure 1.

(a) Show that  $v^2 = 24.5(1 - \cos \theta)$ .

**(3 marks)**

(b) Find the value of  $\cos \theta$  when  $P$  leaves the surface of the sphere.

**(5 marks)**

3. A car starts from rest at the point  $O$  and moves along a straight line. The car accelerates to a maximum velocity,  $V \text{ m s}^{-1}$ , before decelerating and coming to rest again at the point  $A$ .

The acceleration of the car during this journey,  $a \text{ m s}^{-2}$ , is modelled by the formula

$$a = \frac{500 - kx}{150},$$

where  $x$  is the distance in metres of the car from  $O$ .

Using this model and given that the car is travelling at  $16 \text{ m s}^{-1}$  when it is 40 m from  $O$ ,

- (a) find  $k$ , **(6 marks)**
- (b) show that  $V = 41$ , correct to 2 significant figures, **(3 marks)**
- (c) find the distance  $OA$ . **(3 marks)**

4.

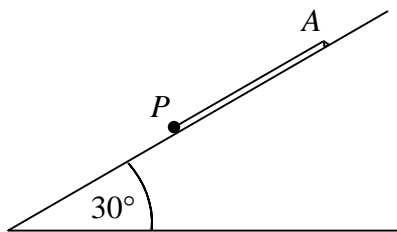


Fig. 2

A particle  $P$  of mass 2 kg is attached to one end of a light elastic string of natural length 1.5 m and modulus of elasticity  $\lambda$ . The other end of the string is fixed to a point  $A$  on a rough plane inclined at an angle of  $30^\circ$  to the horizontal as shown in Figure 2. The coefficient of friction between  $P$  and the plane is  $\frac{1}{6}\sqrt{3}$ .

$P$  is held at rest at  $A$  and then released. It first comes to instantaneous rest at the point  $B$ , 2.2 m from  $A$ . For the motion of  $P$  from  $A$  to  $B$ ,

- (a) show that the work done against friction is 10.78 J, **(5 marks)**
- (b) find the change in the gravitational potential energy of  $P$ . **(2 marks)**

By using the work-energy principle, or otherwise,

- (c) find  $\lambda$ . **(5 marks)**

*Turn over*

5.

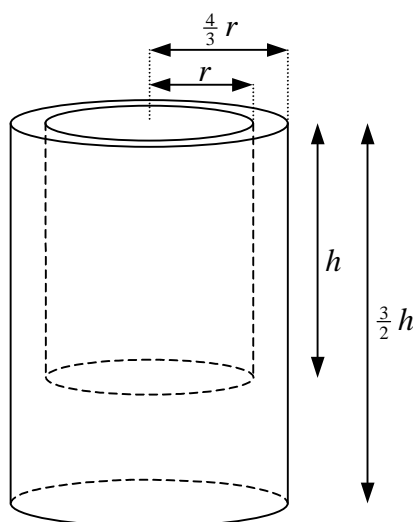


Fig. 3

A flask is modelled as a uniform solid formed by removing a cylinder of radius  $r$  and height  $h$  from a cylinder of radius  $\frac{4}{3}r$  and height  $\frac{3}{2}h$  with the same axis of symmetry and a common plane as shown in Figure 3.

- (a) Show that the centre of mass of the flask is a distance of  $\frac{9}{10}h$  from the open end of the flask.

**(7 marks)**

The flask is made from a material of density  $\rho$  and is filled to the level of the open plane face with a liquid of density  $k\rho$ . Given that the centre of mass of the flask and liquid together is a distance of  $\frac{15}{22}h$  from the open end of the flask,

- (b) find the value of  $k$ .
- (c) Explain why it may be advantageous to make the base of the flask from a more dense material.

**(2 marks)**

6. A particle  $P$  of mass 2.5 kg is moving with simple harmonic motion in a straight line between two points  $A$  and  $B$  on a smooth horizontal table. When  $P$  is 3 m from  $O$ , the centre of the oscillations, its speed is  $6 \text{ m s}^{-1}$ . When  $P$  is 2.25 m from  $O$ , its speed is  $8 \text{ m s}^{-1}$ .

- (a) Show that  $AB = 7.5 \text{ m}$ .
- (b) Find the period of the motion.
- (c) Find the kinetic energy of  $P$  when it is 2.7 m from  $A$ .
- (d) Show that the time taken by  $P$  to travel directly from  $A$  to the midpoint of  $OB$  is  $\frac{\pi}{4}$  seconds.

**END**