GCE Examinations

Mechanics Module M3

Advanced Subsidiary / Advanced Level

Paper D

Time: 1 hour 30 minutes

Instructions and Information

Candidates may use any calculator except those with a facility for symbolic algebra and/or calculus.

Full marks may be obtained for answers to ALL questions.

Mathematical and statistical formulae and tables are available.

This paper has 7 questions.

When a numerical value of g is required, use $g = 9.8 \text{ m s}^{-2}$.

Advice to Candidates

You must show sufficient working to make your methods clear to an examiner. Answers without working will gain no credit.



Written by Shaun Armstrong & Chris Huffer © Solomon Press

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1. The mechanism for releasing the ball on a pinball machine contains a light elastic spring of natural length 15 cm and modulus of elasticity λ .

The spring is held compressed to a length of 9 cm by a force of 4.5 N.

- Find λ . *(a)* (3 marks)
- *(b)* Find the work done in compressing the spring from a length of 9 cm to a length of 5 cm.

2. A small bead P is threaded onto a smooth circular wire of radius 0.8 m and centre O which is fixed in a vertical plane.

The bead is projected from the point vertically below O with speed $u \text{ m s}^{-1}$ and moves in complete circles about *O*.

- Suggest a suitable model for the bead. (a)
- Given that the minimum speed of *P* is 60% of its maximum speed, use the principle of *(b)* conservation of energy to show that u = 7.

(6 marks)

At time t seconds the acceleration, $a \text{ m s}^{-2}$, of a particle is given by 3.

$$a = \frac{4}{\left(1+t\right)^3}.$$

When t = 0, the particle has velocity 1 m s⁻¹ and displacement 3 m from a fixed origin O.

- (a)Find an expression for the velocity of the particle in terms of *t*. (4 marks)
- Show that when t = 3 the particle is 10.5 m from *O*. *(b)* (5 marks)

(4 marks)

(1 mark)

4. A particle of mass 0.5 kg is moving on a straight line with simple harmonic motion.

At time t = 0 the particle is instantaneously at rest at the point A. It next comes instantaneously to rest 3 seconds later at the point B where AB = 4 m.

- (a) For the motion of the particle write down
 - (i) the period,
 - (ii) the amplitude. (2 marks)
- (b) Find the maximum kinetic energy of the particle in terms of π . (4 marks)

The point *C* lies on *AB* at a distance of 1.2 m from *B*.

(c) Find the time it takes the particle to travel directly from A to C, giving your answer in seconds correct to 2 decimal places.

(4 marks)

5. When a particle of mass M is at a distance of x metres from the centre of the moon, the gravitational force, F N, acting on it and directed towards the centre of the moon is given by

$$F = \frac{(4.90 \times 10^{12})M}{x^2} \,.$$

A rocket is projected vertically into space from a point on the surface of the moon with initial speed $u \text{ m s}^{-1}$. Given that the radius of the moon is $(1.74 \times 10^6) \text{ m}$,

(a) show that the speed of the rocket, $v \text{ m s}^{-1}$, when it is x metres from the centre of the moon is given by

$$v^2 = u^2 + \frac{a}{x} - b,$$

where *a* and *b* are constants which should be found correct to 3 significant figures.

(7 marks)

(b) Find, correct to 2 significant figures, the minimum value of u needed for the rocket to escape the moon's gravitational attraction.

(4 marks)

Turn over

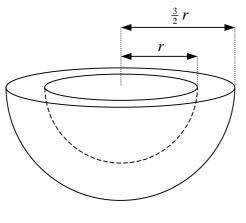


Fig. 1

Figure 1 shows a bowl formed by removing from a solid hemisphere of radius $\frac{3}{2}r$ a smaller hemisphere of radius *r* having the same axis of symmetry and the same plane face.

(a) Show that the centre of mass of the bowl is a distance of $\frac{195}{304}r$ from its plane face. (7 marks)

The bowl has mass *M* and is placed with its curved surface on a smooth horizontal plane. A stud of mass $\frac{1}{2}M$ is attached to the outer rim of the bowl.

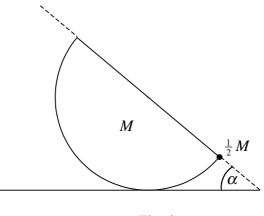


Fig. 2

When the bowl is in equilibrium its plane surface is inclined at an angle α to the horizontal as shown in Figure 2.

(b) Find $\tan \alpha$.

(6 marks)

7. A cyclist is travelling round a circular bend of radius 25 m on a track which is banked at an angle of 35° to the horizontal.

In a model of the situation, the cyclist and her bicycle are represented by a particle of mass 60 kg and air resistance and friction are ignored.

Using this model and assuming that the cyclist is not slipping,

(a) find, correct to 3 significant figures, the speed at which she is travelling. (5 marks)

In tests it is found that the cyclist must travel at a minimum speed of 10 m s⁻¹ to prevent the bicycle from slipping down the slope. A more refined model is now used with a coefficient of friction between the bicycle and the track of μ .

Using this model,

- (b) show that $\mu = 0.227$, correct to 3 significant figures, (8 marks)
- (c) find, correct to 2 significant figures, the maximum speed at which the cyclist can travel without slipping up the slope.

(5 marks)

END