

GCE Examinations  
Advanced Subsidiary / Advanced Level

**Mechanics**  
**Module M3**

Paper B

**MARKING GUIDE**

This guide is intended to be as helpful as possible to teachers by providing concise solutions and indicating how marks should be awarded. There are obviously alternative methods that would also gain full marks.

Method marks (M) are awarded for knowing and using a method.

Accuracy marks (A) can only be awarded when a correct method has been used.

(B) marks are independent of method marks.

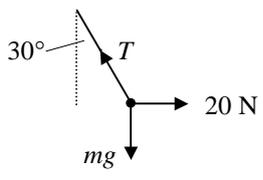
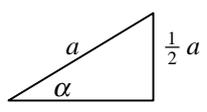
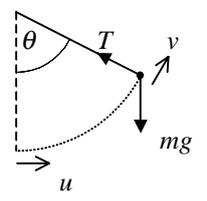


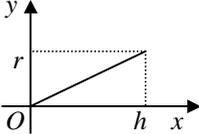
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### M3 Paper B – Marking Guide

1. (a)  $s = e^{0.3} - 1 = 0.3499 \text{ m} = 35 \text{ cm}$  (nearest cm) M1 A1
- (b)  $v = \frac{ds}{dt} = 3e^{3t}$  M1 A1  
when  $t = 0$ ,  $v = 3 \text{ ms}^{-1}$  A1
- (c)  $a = \frac{dv}{dt} = 9e^{3t} \text{ ms}^{-2}$  A1
- (d) e.g. model predicts increasing accel., more likely to be decreasing B1 (7)
- 
2. (a) 
- resolve  $\rightarrow$ :  $20 - T \sin 30^\circ = 0 \therefore T = 40 \text{ N}$  M1 A2
- (b) let natural length be  $l \therefore T = \frac{\lambda x}{l} = \frac{80(1.2-l)}{l}$  M1 A1  
 $T = 40 \therefore l = 2(1.2 - l)$  giving  $l = 0.8 \text{ m}$  A1  
EPE =  $\frac{\lambda x^2}{2l} = \frac{80 \times 0.4^2}{2 \times 0.8} = 8 \text{ J}$  M1 A1 (8)
- 
3. (a)   $\sin \alpha = \frac{1}{2} \therefore \alpha = 30^\circ$  M1  
 $\angle BOA = 90 + \alpha = 120^\circ$  A1
- (b) 
- resolve  $\curvearrowright$ :  $T - mg \cos \theta = \frac{mv^2}{r}$  M1  
at B,  $T = 0$ ,  $\theta = 120^\circ \therefore v^2 = \frac{1}{2} ga$  A1  
con. of ME:  $\frac{1}{2} m(u^2 - v^2) = mg \times \frac{3}{2} a$  M1  
 $\therefore v^2 = u^2 - 3ga$  A1  
combining,  $\frac{1}{2} ga = u^2 - 3ga \therefore u^2 = \frac{7}{2} ga$  M1 A1 (8)
- 
4. (a) amplitude =  $\frac{1}{2} (14 - 6) = 4 \text{ m}$  B1  
period =  $2 \times 6 \frac{1}{4} = 12 \frac{1}{2} \text{ hours}$  B1
- (b)  $x = a \cos \omega t \therefore -1 = 4 \cos \omega t$  M1 A1  
 $\cos \omega t = -\frac{1}{4} \therefore \omega t = 1.8235, \dots$  A1  
period =  $\frac{2\pi}{\omega} = 12 \frac{1}{2} \therefore \omega = \frac{4\pi}{25}$  M1  
giving  $t = 1.8235 \div \frac{4\pi}{25} = 3.6277 \text{ hours}$  A1  
depth 9 m at 11 am + 3.6277 hours = 2.38 pm (nearest min.) A1
- (c) depth 9 m again when  $\omega t = 2\pi - 1.8235 = 4.4597$  M1  
 $t = 4.4597 \div \frac{4\pi}{25} = 8.8723$  A1  
wait until 11 am + 8.8723 hours = 7.52 pm M1  
 $\therefore 2 \text{ hours } 52 \text{ min. wait}$  (nearest min.) A1 (12)
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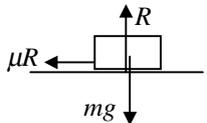
5. (a)  let  $y = \frac{r}{h}x$ ,  $\rho =$  mass per unit volume M1  
 $\therefore \frac{1}{3}\rho\pi r^2 h \bar{x} = \int_0^h \rho\pi y^2 x dx$  A1  
 $\frac{1}{3}r^2 h \bar{x} = \int_0^h \frac{r^2}{h^2} x^3 dx = \frac{r^2}{h^2} \left[ \frac{x^4}{4} \right]_0^h$  M1 A1  
 $\frac{1}{3}r^2 h \bar{x} = \frac{1}{4}r^2 h^2 \therefore \bar{x} = \frac{3}{4}h$  M1 A1

(b)

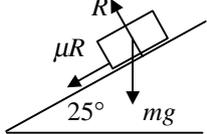
portion	mass	y	my
cone	$\rho \times \frac{1}{3}\pi r^2 \times r = \frac{1}{3}\rho\pi r^3$	$\frac{3}{4}r$	$\frac{1}{4}\rho\pi r^4$
hemisphere	$\frac{1}{2} \times \rho \times \frac{4}{3}\pi r^3 = \frac{2}{3}\rho\pi r^3$	$r + \frac{3}{8}r = \frac{11}{8}r$	$\frac{11}{12}\rho\pi r^4$
paperweight	$\rho\pi r^3$	$\bar{y}$	$\frac{7}{6}\rho\pi r^4$

$\rho =$  mass per unit volume y coords. taken vert. from vertex M2 A3

$\rho\pi r^3 \times \bar{y} = \frac{7}{6}\rho\pi r^4 \therefore \bar{y} = \frac{7}{6}r$  M1 A1 (13)

6. (a)  resolve  $\uparrow$ :  $R - mg = 0$ ,  $R = mg$  M1  
 resolve  $\leftarrow$ :  $\mu R = \frac{mv^2}{r}$ ,  $\frac{2}{5}R = \frac{mv^2}{40}$  M1 A1  
 combining,  $\frac{2}{5}mg = \frac{mv^2}{40}$  M1  
 $\therefore v^2 = \frac{2}{5}g \times 40$  giving  $v = 12.5 \text{ ms}^{-1}$  (3sf) A1

(b)

 resolve  $\uparrow$ :  $R \cos 25 - \mu R \sin 25 - mg = 0$  M1 A1  
 $R = \frac{mg}{\cos 25 - \frac{2}{5}\sin 25}$   
 resolve  $\leftarrow$ :  $R \sin 25 + \mu R \cos 25 = \frac{mv^2}{r}$  M1 A1  
 combining,  $\frac{mg(\sin 25 + \frac{2}{5}\cos 25)}{\cos 25 - \frac{2}{5}\sin 25} = \frac{mv^2}{40}$  M1  
 giving  $v^2 = \frac{40g(\sin 25 + \frac{2}{5}\cos 25)}{\cos 25 - \frac{2}{5}\sin 25} \therefore v = 20.43$  A1  
 % increase =  $\frac{20.43 - 12.52}{12.52} \times 100\% = 63\%$  (nearest WN) M1 A1 (13)

7. (a)  $a = v \frac{dv}{dx} = \frac{2}{x+1} \times \frac{-2}{(x+1)^2} = \frac{-4}{(x+1)^3}$  M2 A2

(b)  $\frac{dx}{dt} = \frac{2}{x+1} \therefore \int (x+1) dx = \int 2 dt$  M2  
 $\frac{1}{2}x^2 + x = 2t + c$  A1  
 $t = 0, x = 0 \therefore c = 0$  so  $x^2 + 2x = 4t$  M1  
 $t = T, x = d \therefore d^2 + 2d = 4T$  A1  
 $t = T + 9, x = d + 4 \therefore (d + 4)^2 + 2(d + 4) = 4(T + 9)$  M1  
 combining,  $d^2 + 8d + 16 + 2d + 8 = d^2 + 2d + 36$  M1  
 giving  $8d = 12$  so  $d = 1.5$  A1

(c)  $(1.5)^2 + 2(1.5) = 4T$  giving  $T = \frac{21}{16}$  or 1.3125 s M1 A1 (14)

Total (75)

