

**OXFORD CAMBRIDGE AND RSA EXAMINATIONS**

**Advanced Subsidiary General Certificate of Education  
Advanced General Certificate of Education**

**MATHEMATICS****4730**

Mechanics 3

**Specimen Paper**

Additional materials:  
Answer booklet  
Graph paper  
List of Formulae (MF 1)

**TIME** 1 hour 30 minutes**INSTRUCTIONS TO CANDIDATES**

- Write your Name, Centre Number and Candidate Number in the spaces provided on the answer booklet.
- Answer **all** the questions.
- Give non-exact numerical answers correct to 3 significant figures, unless a different degree of accuracy is specified in the question or is clearly appropriate.
- Where a numerical value for the acceleration due to gravity is needed, use  $9.8 \text{ m s}^{-2}$ .
- You are permitted to use a graphic calculator in this paper.

**INFORMATION FOR CANDIDATES**

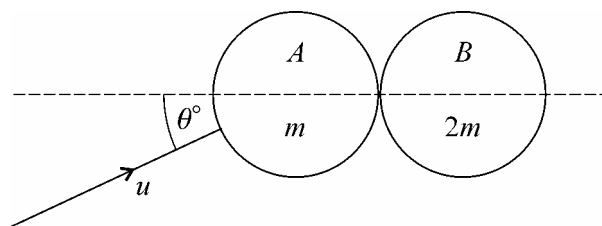
- The number of marks is given in brackets [ ] at the end of each question or part question.
- The total number of marks for this paper is 72.
- Questions carrying smaller numbers of marks are printed earlier in the paper, and questions carrying larger numbers of marks later in the paper.
- **You are reminded of the need for clear presentation in your answers.**

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**This question paper consists of 4 printed pages.**

- 1 A particle is moving with simple harmonic motion in a straight line. The period is 0.2 s and the amplitude of the motion is 0.3 m. Find the maximum speed and the maximum acceleration of the particle. [6]

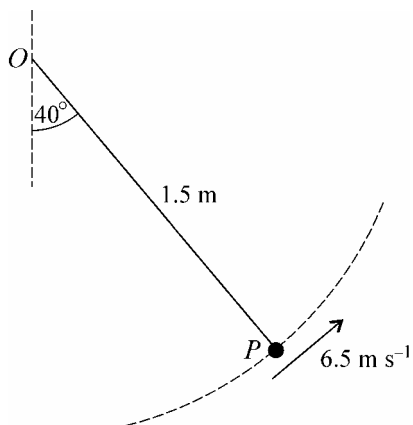
2



A sphere  $A$  of mass  $m$ , moving on a horizontal surface, collides with another sphere  $B$  of mass  $2m$ , which is at rest on the surface. The spheres are smooth and uniform, and have equal radius. Immediately before the collision,  $A$  has velocity  $u$  at an angle  $\theta^\circ$  to the line of centres of the spheres (see diagram). Immediately after the collision, the spheres move in directions that are perpendicular to each other.

- (i) Find the coefficient of restitution between the spheres. [4]
- (ii) Given that the spheres have equal speeds after the collision, find  $\theta$ . [3]
- 3 An aircraft of mass 80 000 kg travelling at  $90 \text{ m s}^{-1}$  touches down on a straight horizontal runway. It is brought to rest by braking and resistive forces which together are modelled by a horizontal force of magnitude  $(27\,000 + 50v^2)$  newtons, where  $v \text{ m s}^{-1}$  is the speed of the aircraft. Find the distance travelled by the aircraft between touching down and coming to rest. [8]
- 4 For a bungee jump, a girl is joined to a fixed point  $O$  of a bridge by an elastic rope of natural length 25 m and modulus of elasticity 1320 N. The girl starts from rest at  $O$  and falls vertically. The lowest point reached by the girl is 60 m vertically below  $O$ . The girl is modelled as a particle, the rope is assumed to be light, and air resistance is neglected.
- (i) Find the greatest tension in the rope during the girl's jump. [2]
- (ii) Use energy considerations to find
- (a) the mass of the girl, [4]
- (b) the speed of the girl when she has fallen half way to the lowest point. [3]

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A particle  $P$  of mass  $0.3\text{ kg}$  is moving in a vertical circle. It is attached to the fixed point  $O$  at the centre of the circle by a light inextensible string of length  $1.5\text{ m}$ . When the string makes an angle of  $40^\circ$  with the downward vertical, the speed of  $P$  is  $6.5\text{ m s}^{-1}$  (see diagram). Air resistance may be neglected.

- (i) Find the radial and transverse components of the acceleration of  $P$  at this instant. [2]

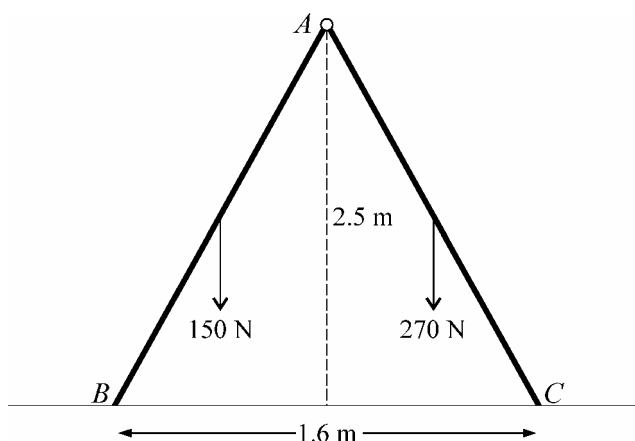
In the subsequent motion, with the string still taut and making an angle  $\theta^\circ$  with the downward vertical, the speed of  $P$  is  $v\text{ m s}^{-1}$

- (ii) Use conservation of energy to show that  $v^2 \approx 19.7 + 29.4\cos\theta^\circ$ . [4]

- (iii) Find the tension in the string in terms of  $\theta$ . [4]

- (iv) Find the value of  $v$  at the instant when the string becomes slack. [3]

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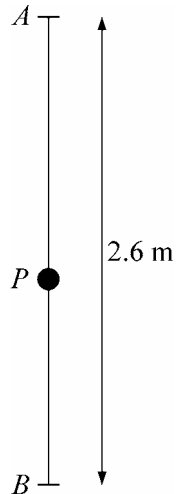


A step-ladder is modelled as two uniform rods  $AB$  and  $AC$ , freely jointed at  $A$ . The rods are in equilibrium in a vertical plane with  $B$  and  $C$  in contact with a rough horizontal surface. The rods have equal lengths;  $AB$  has weight  $150\text{ N}$  and  $AC$  has weight  $270\text{ N}$ . The point  $A$  is  $2.5\text{ m}$  vertically above the surface, and  $BC = 1.6\text{ m}$  (see diagram).

- (i) Find the horizontal and vertical components of the force acting on  $AC$  at  $A$ . [8]

- (ii) The coefficient of friction has the same value  $\mu$  at  $B$  and at  $C$ , and the step-ladder is on the point of slipping. Giving a reason, state whether the equilibrium is limiting at  $B$  or at  $C$ , and find  $\mu$ . [6]

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Two points  $A$  and  $B$  lie on a vertical line with  $A$  at a distance 2.6 m above  $B$ . A particle  $P$  of mass 10 kg is joined to  $A$  by an elastic string and to  $B$  by another elastic string (see diagram). Each string has natural length 0.8 m and modulus of elasticity 196 N. The strings are light and air resistance may be neglected.

- (i) Verify that  $P$  is in equilibrium when  $P$  is vertically below  $A$  and the length of the string  $PA$  is 1.5 m. [4]

The particle is set in motion along the line  $AB$  with both strings remaining taut. The displacement of  $P$  below the equilibrium position is denoted by  $x$  metres.

- (ii) Show that the tension in the string  $PA$  is  $245(0.7 + x)$  newtons, and the tension in the string  $PB$  is  $245(0.3 - x)$  newtons. [3]
- (iii) Show that the motion of  $P$  is simple harmonic. [3]
- (iv) Given that the amplitude of the motion is 0.25 m, find the proportion of time for which  $P$  is above the mid-point of  $AB$ . [5]