



GCE

# Mathematics

Advanced GCE

Unit 4730: Mechanics 3

## Mark Scheme for January 2011

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|--------|--|---------------------------|---|
| 1<br>i | $(-)15\cos\alpha = (0 -) 0.5 \times 22$ or $15\sin\beta = 0.5 \times 22$<br><br>Impulse makes angle $42.8^\circ$ (0.748 rads) with negative x-axis   | M1<br>A1<br>A1<br><br>[3] | M1 for using $\mathbf{I} = \Delta(m\mathbf{v})$ in 'x' direction or for sketching $\Delta$ reflecting $\mathbf{I} = m(\mathbf{v} - \mathbf{u})$<br><br>AEF, but angle must be clear |
| ii     | $15\sin\alpha = 0.5v$ or $15\cos\beta = 0.5v$<br>or $(0.5v)^2 = 15^2 - 11^2$<br>Correct explicit expression for v<br>Speed is $20.4 \text{ ms}^{-1}$ | M1<br><br>A1<br>A1<br>[3] | For using $\mathbf{I} = \Delta(m\mathbf{v})$ in 'y' direction or using sketched $\Delta$  |

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| 2 | $\frac{1}{2}(m)(v^2 - 6^2) = -(m)g \times 0.5$ in (i) or<br>$\frac{1}{2}(m)(v^2 - 6^2) = -(m)g \times 1$ in (ii)<br>$v^2 = 26.2$ in (i) and $16.4$ in (ii)<br><br>$T = 0.4v^2/0.5$ in (i) or<br>$T + 0.4g = 0.4v^2/0.5$<br><br>Tension is $21.0\text{N}$ in (i) (20.96)<br>$9.2\text{N}$ in (ii) | M1<br><br>A1<br><br>M1<br>A1<br><br>A1<br>A1<br>[6] | For using the principle of conservation of energy in (i) or (ii)<br><br>soi<br><br>For using Newton's second law with $a = v^2/L$ . M1 for either attempt, A1 for both right |
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| 3<br>i | $2.8V = 1.4 \times 72$<br>Vertical component at P is 36 N   | M1<br>A1<br>[2]                   | For taking moments about Q for PQ or for using symmetry                                 |
| ii     | $36 + N = 72 + 54$<br>Normal component at R is 90 N   | M1<br>A1<br>[2]                   | For resolving forces vertically on both rods AG   |
| iii    | $1.44F = 1.2 \times 90 - 0.8 \times 54$ or<br>$72 \times 1.4 + 54 \times 3.6 + 1.44F = 90 \times 4$<br>with not more than 1 error in either case<br>Equation correct and leading to $F = 45$<br>For using $F = \mu R$<br>Coefficient is 0.5 | M1<br>A1<br>A1<br>M1<br>A1<br>[5] | For taking moments about Q for QR or about P for the whole structure (all terms needed) |

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| 4<br>i | $0.4(7 \times 0.6) - 0.3 \times 2.8 = 0.4a + 0.3b$<br>$0.7(7 \times 0.6 + 2.8) = b - a$<br>Speed of B is $4 \text{ms}^{-1}$                                    | M1<br>A1<br>M1<br>A1<br>M1<br>A1<br>[6] | For using the principle of conservation of momentum<br>For using $e(\Delta u) = \Delta v$<br>For eliminating a from equations   |
| ii     | $a = (-)0.9$<br>Component perp. to l.o.c. is 5.6<br>$\tan \alpha = 5.6/0.9$<br>$\alpha = 80.9^\circ$<br>Angle turned through is $46.0^\circ$ ( $0.803^\circ$ ) | B1<br>B1<br>M1<br>A1<br>A1ft<br>[5]     | For attempting to find $\alpha$ - the angle between the direction of motion of A after collision and the l.o.c. to the left, or $90^\circ - \alpha$<br>$126.9^\circ - \alpha$ |

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| 5<br>i | $2.45e/0.5 = 0.05g$<br>( $e = 0.1$ )<br>Distance from O is $0.5 + 0.1 = 0.6\text{m}$   | M1<br>A1<br>A1<br>[3]                           | For using $T = \lambda e/L$ and resolving forces vertically<br>accept use of 0.1 to show both sides equal to 0.49<br>AG  |
| ii     | $mg - T = m\ddot{x}$<br>$0.05g - 2.45(0.1 + x)/0.5 = 0.05\ddot{x}$<br>$\ddot{x} = -98x$  | M1<br>A1<br>A1<br>[3]                           | For using Newton's second law with 3 terms<br>AG   |
| iii    | $a = 0.075$<br>$n = 7\sqrt{2}$ oe<br>$x = 0.075\cos(7\sqrt{2}t)$<br>$x(0.2) = -0.0298$<br>$v = -0.075(7\sqrt{2})\sin(7\sqrt{2}t)$<br>$v(0.2) = -0.681 \rightarrow$ velocity is $0.681\text{ms}^{-1}$ upwards | B1<br>B1<br>M1<br>A1<br>M1<br>A1ft<br>A1<br>[7] | accept 9.90<br>For using $x = a\cos nt$ oe<br>For differentiating $x = a\cos nt$ and using it<br>ft incorrect $a$ and/or $n$<br>If from $v^2 = n^2(a^2 - x^2)$ the direction must be clearly established |

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| <p>6<br/>i</p> | $112e/4 = 3.5 \times 9.8 \times \frac{40}{49}$ $V^2 = 2 \times 8 \times (4 + 1)$ $V^2 = 80$ $0.5 \sqrt{80} = (0.5 + 3.5)u$ <p>Initial speed of combined particles is</p> $\frac{1}{2} \sqrt{5} \text{ ms}^{-1}$   | <p>M1<br/>A1<br/>M1<br/>A1<br/><br/>M1<br/>A1<br/>[6]</p>      | <p>For using <math>mg \sin \theta</math> and <math>\lambda e/L</math><br/><br/>For using <math>s = 4 + e</math> and <math>a = 8</math> in <math>v^2 = 2as</math>, or by energy<br/><br/>For using the principle of conservation of momentum<br/><br/>AG</p> |
| <p>ii</p>      | <p>Gain in EE = <math>(112/(2 \times 4))\{(X + 1)^2 - 1^2\}</math><br/>Loss of KE = <math>\frac{1}{2} (0.5 + 3.5) \times 5/4</math><br/>Loss of PE = <math>(0.5 + 3.5) \times 9.8 \times \frac{40}{49} X</math></p> $14(X^2 + 2X) = 2.5 + 32X$ $28X^2 - 8X - 5 = 0$ | <p>M1<br/>A1<br/>B1<br/>B1<br/><br/>M1<br/>A1<br/>[6]</p>      | <p>For using <math>EE = \lambda x^2/2L</math><br/><br/><br/><br/>For using the principle of conservation of energy<br/><br/>AG</p>  |
| <p>OR</p>      | $T - mg \sin \theta = -ma$ $\frac{112(x+1)}{4} - 4g \frac{40}{49} = -4a$ $\int (7x - 1) dx = - \int v dv (+c)$ $\frac{7x^2}{2} - x = -\frac{v^2}{2} + c$ $c = \frac{5}{8}$ $28X^2 - 8X - 5 = 0$   | <p>M1<br/>A1<br/><br/>M1<br/><br/>A1<br/>A1<br/>A1<br/>[6]</p> | <p>For use of <math>F = ma</math><br/>allow one sign slip for A1<br/><br/>Using <math>a = v \frac{dv}{dx}</math> and integrating<br/><br/><br/><br/>AG Convincingly</p>   |

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| 7<br>i | $0.2g - v^2/2000 = 0.2v(dv/dx)$ $\left(\frac{400v}{3920 - v^2}\right) \frac{dv}{dx} = 1.$   | M1<br>A1<br>[2]                               | For using Newton's second law with<br>$a = v(dv/dx)$<br>AG Convincing, with no slips.   |
| ii     | $-200 \ln(3920 - v^2) = x + (A)$ $-200 \ln(3920) = A$ $x = 200 \ln\left(\frac{3920}{3920 - v^2}\right)$ $e^{x/200} = 3920/(3920 - v^2)$ $v^2 = 3920(1 - e^{-x/200})$ $0 < e^{-x/200} \rightarrow v^2 < 3920$  | M1<br>A1<br>M1<br>A1<br>M1<br>A1<br>B1<br>[7] | For separating variables and integrating<br><br>For using $v(0) = 0$<br><br>For using inverse ln process<br><br>AG Convincingly – dep on correct answer |
| iii    | <p>Using <math>0.2g - v^2/2000 = 0.2a</math><br/> <math>v = 40</math><br/>                 Gain in KE = <math>\frac{1}{2} 0.2 \times 1600</math> (=160J)<br/> <math>x = 200 \ln\left(\frac{3920}{3920 - 1600}\right)</math> (= 104.90)<br/><br/> <math>0.2g \times (104.9) - 160</math><br/>                 Work done is 45.6 J</p>  | M1<br>A1<br>B1ft<br>B1ft<br>M1<br>A1<br>[6]   | For using WD = loss of PE – gain in KE  |
| OR     | <p>Using <math>0.2g - v^2/2000 = 0.2a</math><br/> <math>v = 40</math><br/> <math>x = 200 \ln\left(\frac{3920}{3920 - 1600}\right)</math> (= 104.90...)<br/><br/> <math>WD = \int \frac{v^2}{2000} dx + c</math><br/> <math>= \int \frac{3920}{2000} (1 - e^{-x/200}) dx</math><br/> <math>= 3920 / 2000(x + 200e^{-x/200}) - 392</math><br/><br/>                 Work done is 45.6 J</p> | M1<br>A1<br>B1ft<br>M1<br>A1<br>A1<br>[6]     | Use of $WD = \int Fdx$ and subst for $v^2$  |

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