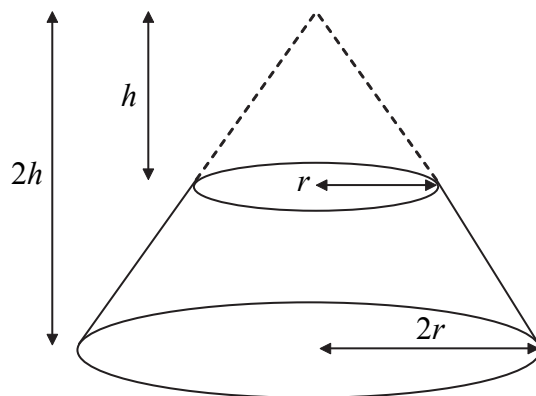


Leave blank

3.

Figure 1



A uniform solid S is formed by taking a uniform solid right circular cone, of base radius $2r$ and height $2h$, and removing the cone, with base radius r and height h , which has the same vertex as the original cone, as shown in Figure 1.

(a) Show that the distance of the centre of mass of S from its larger plane face is $\frac{11}{28}h$. (5)

The solid S lies with its larger plane face on a rough table which is inclined at an angle θ° to the horizontal. The table is sufficiently rough to prevent S from slipping. Given that $h = 2r$,

(b) find the greatest value of θ for which S does not topple. (3)



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4. A particle P of mass m lies on a smooth plane inclined at an angle 30° to the horizontal. The particle is attached to one end of a light elastic string, of natural length a and modulus of elasticity $2mg$. The other end of the string is attached to a fixed point O on the plane. The particle P is in equilibrium at the point A on the plane and the extension of the string is $\frac{1}{4}a$. The particle P is now projected from A down a line of greatest slope of the plane with speed V . It comes to instantaneous rest after moving a distance $\frac{1}{2}a$.

By using the principle of conservation of energy,

(a) find V in terms of a and g , (6)

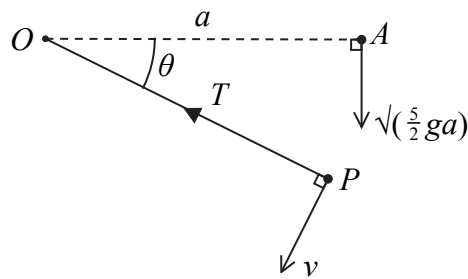
(b) find, in terms of a and g , the speed of P when the string first becomes slack. (4)



Leave blank

6.

Figure 2



A particle P of mass m is attached to one end of a light inextensible string of length a . The other end of the string is attached to a fixed point O . At time $t = 0$, P is projected vertically downwards with speed $\sqrt{\frac{5}{2}ga}$ from a point A which is at the same level as O and a distance a from O . When the string has turned through an angle θ and the string is still taut, the speed of P is v and the tension in the string is T , as shown in Figure 2.

(a) Show that $v^2 = \frac{ga}{2}(5 + 4\sin\theta)$. (3)

(b) Find T in terms of m , g and θ . (3)

The string becomes slack when $\theta = \alpha$.

(c) Find the value of α . (3)

The particle is projected again from A with the same velocity as before. When P is at the same level as O for the first time after leaving A , the string meets a small smooth peg B which has been fixed at a distance $\frac{1}{2}a$ from O . The particle now moves on an arc of a circle centre B . Given that the particle reaches the point C , which is $\frac{1}{2}a$ vertically above the point B , without the string going slack,

(d) find the tension in the string when P is at the point C . (6)



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blank

7. A particle P of mass 2 kg is attached to one end of a light elastic string, of natural length 1 m and modulus of elasticity 98 N . The other end of the string is attached to a fixed point A . When P hangs freely below A in equilibrium, P is at the point E , 1.2 m below A . The particle is now pulled down to a point B which is 0.4 m vertically below E and released from rest.

(a) Prove that, while the string is taut, P moves with simple harmonic motion about E with period $\frac{2\pi}{7} \text{ s}$. (5)

(b) Find the greatest magnitude of the acceleration of P while the string is taut. (1)

(c) Find the speed of P when the string first becomes slack. (3)

(d) Find, to 3 significant figures, the time taken, from release, for P to return to B for the first time. (7)



