

Question Number	Scheme	Marks
1.	$1000 \text{ r.p.m} = \frac{1000 \times 2\pi}{60} \text{ rad/s}$ $v = 0.035 \times \frac{1000 \times 2\pi}{60} = 3.67 \text{ ms}^{-1} \text{ (3 SF)}$	B1 M1 their $r \times$ their $\omega$ M1 A1 <b>(3 marks)</b>
2.	$\text{Extn at bottom} = \frac{a}{\cos \alpha} - a = \frac{2a}{3} \text{ (0.67a or better)}$ $\text{Energy: } mga \tan \alpha = \frac{2\lambda \left(\frac{2a}{3}\right)^2}{2a}$ $3mg = \lambda$	M1 A1 M1 A1 A1 ft M1 A1 Second M0 if treated as equilibrium Third M1 for solving for $\lambda$ <b>(7 marks)</b>
3. (a)	$mg \sin 30^\circ - mx^2 = ma$ $\frac{g}{2} - x^2 = v \frac{dv}{dx} \text{ or } \frac{d\left(\frac{1}{2}v^2\right)}{dx}$ $\frac{gx}{2} - \frac{x^3}{3} (+C) = \frac{v^2}{2}$ $x = 2 : g - \frac{8}{3} = \frac{v^2}{2}$ $v = 3.8 \text{ms}^{-1} \text{ (3.78)}$	M1 A1 M1 M1 A1 M1 A1 (7) Third M1 for attempting to integrate
(b)	$v = 0: \frac{gx}{2} - \frac{x^3}{3} = 0$ $x^2 = \frac{3g}{2} \Rightarrow x = 3.8, (3.83), \sqrt{\frac{3g}{2}}$	M1 M1 A1 c.s.o must have integrated for first M1 (3) <b>(10 marks)</b>

(ft = follow through mark)

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4.	(↑), $R = mg$	B1
	$m \frac{4a}{3} \omega^2$ (seen and used)	B1
	$m \frac{4a}{3} \omega^2 \leq \frac{3}{5} mg$	M1
	$\omega^2 \leq \frac{9g}{20a} *$	A1 c.s.o (4)
	(b) $T = \frac{2mg}{a} \frac{a}{3} = \frac{2mg}{3}$	B1
	$(\rightarrow), \frac{3}{5}mg + \frac{2mg}{3} \geq m \frac{4a}{3} \omega_{\max}^2$	M1 A1 f.t
	$\frac{19g}{20a} = \omega_{\max}^2$	A1
$(\rightarrow), -\frac{3}{5}mg + \frac{2mg}{3} \leq m \frac{4a}{3} \omega_{\min}^2$	M1 A1 f.t	
$\frac{g}{20a} = \omega_{\min}^2$	A1 (7)	
If only one answer, must be clear whether max or min for final A1		<b>(11 marks)</b>

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<p>5. (a)</p> <p>mass ratio</p> <p>dist. From <math>O</math></p> <p>(b)</p> <p>(c)</p>	<p>Cylinder (<math>36\pi r^3</math>)</p> <p>3</p> <p><math>2r</math></p> <p><math>(3 \times 2r) - r = 4\bar{x}</math></p> <p><math>\frac{5r}{4} = \bar{x}</math></p> <p>M1 for clear attempt at <math>\Sigma mx = \bar{x} \Sigma m</math> – correct no. of terms. If distances not measured from <math>O</math>, B1B1M1A1 available.</p> <p><math>AG</math> vertical, seen or implied</p> <p><math>\tan \theta = \frac{3r}{4r-x}</math></p> <p><math>\theta = 47.5^\circ</math> (1 d.p.)</p> <p>Sim <math>\Delta</math>'s: <math>\frac{OX}{3r} = \frac{3r}{4r}</math> (<math>= \tan \alpha</math>)</p> <p><math>\Rightarrow OX = \frac{9r}{4}</math></p> <p><math>\bar{x} &lt; OX</math></p> <p><math>\Rightarrow</math> won't topple</p>	<p>Cone (<math>12\pi r^3</math>)</p> <p>1</p> <p><math>(-r)</math></p> <p><math>\bar{x}</math></p> <p>second M1 for use of tan</p>	<p>Toy (<math>48\pi r^3</math>)</p> <p>4</p> <p><math>\bar{x}</math></p> <p>M1 A1</p> <p>A1 (5)</p> <p>M1</p> <p>M1 A1</p> <p>A1 (4)</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>A1 c.s.o (4)</p>	<p>(13 marks)</p>
		<p>Note that second M1 is independent, for the general idea.</p>		

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6.	All M marks require correct number of terms with appropriate terms resolved B to C: $\frac{1}{2}mv^2 - \frac{1}{2}m20^2 = mg \times 50(1 - \sin 30^\circ)$ $v = 30 \text{ ms}^{-1}$ (29.8)	M1 A1 A1 (3)
	(↑) at C, $R - mg = m \frac{890}{50}$ $R = 1900 \text{ N}$ (1930 N)	M1 A1 ft A1 (3)
	C to D: $\frac{1}{2}m890 - \frac{1}{2}mw^2 = mg \times 50(1 - \cos 30^\circ)$ $w = 28 \text{ ms}^{-1}$ (27.5)	M1 A1 ft A1 (3)
	Before: $R = mg \cos \theta$ After: $R = mg \cos \theta + m \frac{20^2}{50}$ Change = $70 \times \frac{20^2}{50} = 560 \text{ N}$	B1 M1 A1 A1 c.s.o (4)
	Lower speed at C $\Rightarrow$ R reduced	M1 A1 (2) <b>(15 marks)</b>

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7. (a)	$(-) \frac{21.6x}{2} = 0.3\ddot{x}$	M1 A1
	$-36x = \ddot{x}$	M1
	$\text{S.H.M., period} = \frac{2\pi}{\sqrt{36}} = \frac{\pi}{3} *$	A1 c.s.o. (4)
(b)	$\text{At A: } v = aw = 1.5 \times 6 = 9 \text{ ms}^{-1}$	M1 A1 (2)
(c)	$x = a \cos \omega t$	
	$0.75 = 1.5 \cos 6t$	M1
	$\frac{\pi}{3} = 6t \Rightarrow t = \frac{\pi}{18} \text{ (no decimals)}$	M1 A1 (3)
(d)	$(-) \frac{21.6x}{2} = 0.5\ddot{x}$	M1 A1
	$-21.6x = \ddot{x} \Rightarrow \text{S.H.M., } \omega = \sqrt{21.6}$	A1
	$\text{At collision: CLM: } 0.3 \times 9 = 0.5v \Rightarrow v = 5.4$	M1 A1 ft
	$a \times \sqrt{21.6} = 5.4$	M1
	$a = 1.16 \text{ m (3SF)}$	A1 (7)
		<b>(16 marks)</b>

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