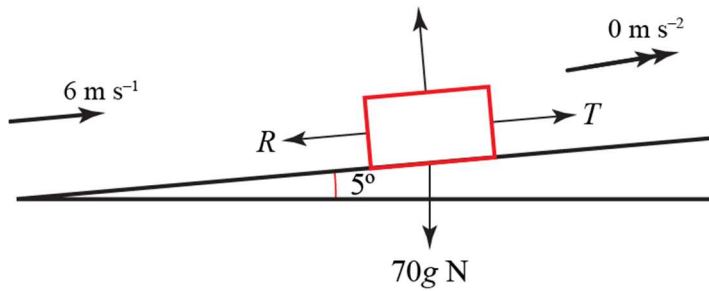


## Chapter Review

1



$$\text{Power} = Fv$$

$$480 = T \times 6$$

$$T = \frac{480}{6} = 80$$

Resolving parallel to the slope:

$$T = R + 70g \sin 5^\circ$$

$$80 = R + 70 \times 9.8 \sin 5^\circ$$

$$R = 80 - 70 \times 9.8 \sin 5^\circ$$

$$R = 20.21\dots$$

The magnitude of the resistance is 20.2 N (3 s.f.)

$$\begin{aligned} 2 \text{ a } \text{P.E. gained by water and bucket} &= mgh \\ &= 12 \times 9.8 \times 25 \\ &= 2940 \end{aligned}$$

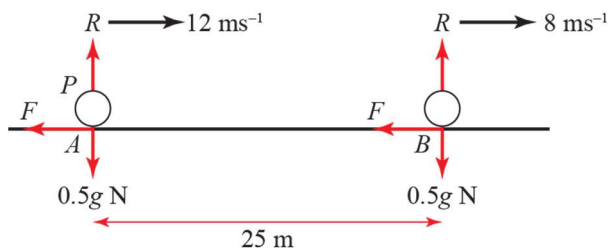
$$\text{Initial K.E.} = \text{final K.E.} = 0$$

$$\begin{aligned} \text{Work done by the boy} &= \text{P.E. gained by bucket} \\ &= 2940 \text{ J} \end{aligned}$$

$$\begin{aligned} \text{b } \text{Average rate of working} &= \frac{\text{work done}}{\text{time taken}} = \frac{2940}{30} \\ &= 98 \end{aligned}$$

The average rate of working of the boy is  $98 \text{ J s}^{-1}$  (or 98 W)

3



$$\begin{aligned} \text{a } \text{K.E. lost by particle} &= \frac{1}{2} \times 0.5 \times 12^2 - \frac{1}{2} \times 0.5 \times 8^2 \\ &= 20 \end{aligned}$$

$$\text{Work done by friction} = \text{K.E. lost by particle}$$

$$\therefore \text{Work done by friction} = 20 \text{ J}$$

- 3 b Resolving vertically:  $R = 0.5g$

Friction is limiting:

$$F = \mu R = \mu \times 0.5g$$

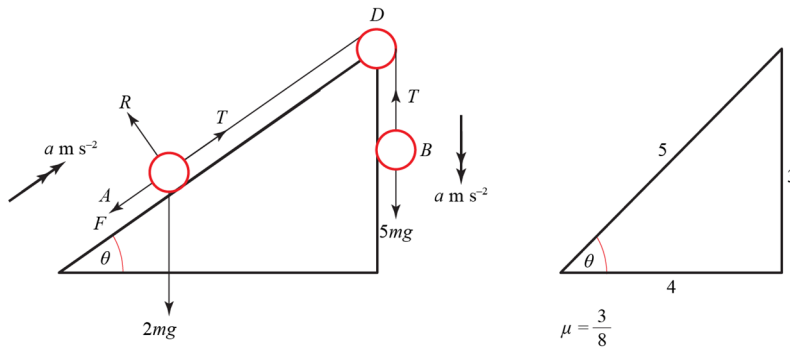
Work done by friction =  $F \times s$

$$20 = \mu \times 0.5g \times 25$$

$$\mu = \frac{20}{0.5g \times 25} = 0.1632\dots$$

The coefficient of friction is 0.163 (3 s.f.)

4



- a Resolving perpendicular to the plane for  $A$ :

$$R = 2mg \cos \theta$$

Friction is limiting:

$$F = \mu R$$

$$F = \frac{3}{8} \times 2mg \cos \theta$$

$$= \frac{3}{8} \times 2mg \times \frac{4}{5}$$

$$= \frac{3}{5} mg$$

$$F = ma \text{ for } A: \quad T - (F + 2mg \sin \theta) = 2ma$$

$$T - \left( \frac{3}{5} mg + 2mg \times \frac{3}{5} \right) = 2ma$$

$$T - \frac{9mg}{5} = 2ma \quad (1)$$

$$F = ma \text{ for } B: \quad 5mg - T = 5ma \quad (2)$$

$$(1) + (2): \quad 5mg - \frac{9mg}{5} = 7ma$$

$$\frac{16mg}{5} = 7ma$$

$$a = \frac{16g}{35} = \frac{16 \times 9.8}{35}$$

$$a = 4.48$$

The initial acceleration of  $A$  is  $4.48 \text{ m s}^{-2}$

4 b For the first 1 m  $A$  travels ←

The motion must be considered in two parts, before and after the string breaks. The friction force acting on  $A$  is the same throughout the motion.

$$u = 0$$

$$a = 4.48 \text{ m s}^{-2}$$

$$s = 1 \text{ m}$$

$$v = ?$$

$$v^2 = u^2 + 2as$$

$$v^2 = 2 \times 4.48 \times 1$$

$$v^2 = 8.96$$

After string breaks:

$$\begin{aligned} \text{Loss of K.E. (of } A) &= \frac{1}{2}mu^2 - \frac{1}{2}mv^2 \\ &= \frac{1}{2} \times 2m \times 8.96 - 0 \\ &= 8.96m \end{aligned}$$

$$\begin{aligned} \text{Gain of P.E. (of } A) &= mgh \\ &= 2mg \times (x \sin \theta) \\ &= 2mg \times x \times \frac{3}{5} \\ &= \frac{6mgx}{5} \end{aligned}$$

where  $x$  is the distance moved up the plane.

$$\text{Work done by friction} = \frac{3mg}{5} \times x$$

Work–energy principle:

$$\begin{aligned} \frac{3mgx}{5} + \frac{6mgx}{5} &= 8.96m \\ \frac{9gx}{5} &= 8.96 \end{aligned}$$

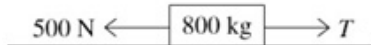
$$x = \frac{8.96 \times 5}{9 \times 9.8}$$

$$x = 0.5079\dots$$

$$\begin{aligned} \text{Total distance moved} &= 1 + 0.5079\dots \\ &= 1.51 \end{aligned}$$

The total distance moved by  $A$  before it first comes to rest is 1.51 m (3 s.f.)

5 a  $\longrightarrow 15 \text{ m s}^{-1}$   $\longrightarrow a \text{ m s}^{-2}$



$$\text{Power} = Fv$$

$$16000 = T \times 15$$

Ensure units are consistent.

$$T = \frac{16000}{15}$$

Using  $F = ma$  :

$$T - 500 = 800a$$

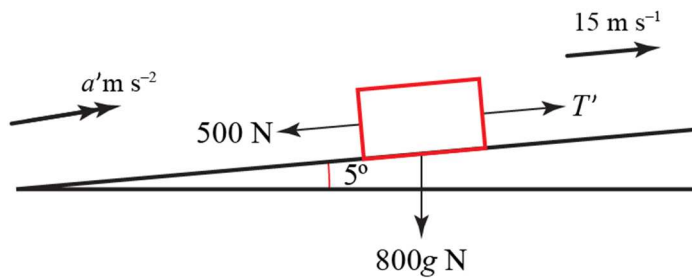
$$\frac{16000}{15} - 500 = 800a$$

$$a = \frac{\frac{16000}{15} - 500}{800}$$

$$a = 0.7083\dots$$

The acceleration is  $0.708 \text{ m s}^{-2}$

b



$$\text{Power} = Fv$$

$$24000 = T' \times 15$$

$$T' = \frac{24000}{15}$$

Resolving parallel to the slope and using  $F = ma$  :

$$T' - 500 - 800g \sin 5^\circ = 800a'$$

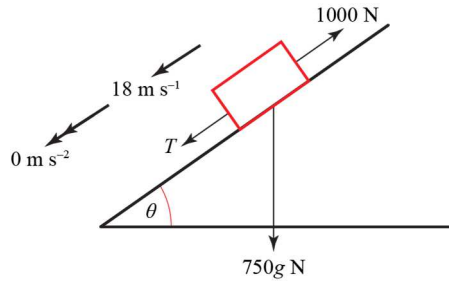
$$\frac{24000}{15} - 500 - 800 \times 9.8 \sin 5^\circ = 800a'$$

$$800a' = 416.698\dots$$

$$a' = 0.5208\dots$$

The new acceleration is  $0.521 \text{ m s}^{-2}$  (3 s.f.)

6 a



$$\tan \theta = \frac{1}{20} \quad \text{so} \quad \theta = 2.8624^\circ$$

Resolving parallel to the slope:

$$T + 750g \sin \theta = 1000$$

$$T = 1000 - 750 \times 9.8 \sin 2.8624^\circ$$

$$T = 632.95$$

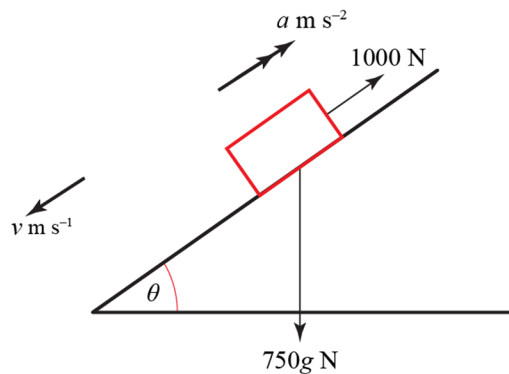
Power =  $Fv$ 

$$= 632.95 \times 18$$

$$= 11393.2 \dots$$

The rate of working of the car's engine is 11.4 kW (3 s.f.)

b



The tractive force is zero.

Resolving parallel to the slope and using  $F = ma$ :

$$1000 - 750 \times 9.8 \times \sin \theta = 750a$$

$$a = \frac{1000 - 750 \times 9.8 \sin 2.8624^\circ}{750}$$

$$a = 0.8439$$

Consider motion down the slope:

$$a = -0.8439 \text{ m s}^{-2}, \quad u = 18 \text{ m s}^{-1}, \quad v = 0 \text{ m s}^{-1}, \quad t = ?$$

$$v = u + at$$

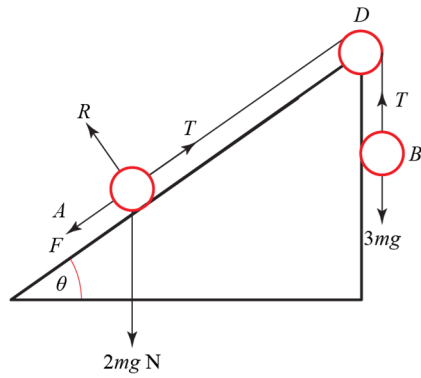
$$0 = 18 - 0.8439 \times t$$

$$t = \frac{18}{0.8439}$$

$$t = 21.32 \dots$$

The value of  $t$  is 21.3 (3 s.f.)

7



$$\begin{aligned}
 \text{a P.E. gained by } A &= mgh \\
 &= 2mg \times (s \times \sin \theta) \\
 &= 2mg \times s \times \frac{3}{5} \\
 &= \frac{6mgs}{5}
 \end{aligned}$$

$$\begin{aligned}
 \text{P.E. lost by } B &= mgh \\
 &= 3mgs
 \end{aligned}$$

$$\therefore \text{P.E. lost by system} = 3mgs - \frac{6mgs}{5} = \frac{9mgs}{5}$$

7 b Consider  $A$ :

Find the frictional force and use the work–energy principle.

Resolving perpendicular to the slope:

$$\begin{aligned} R &= 2mg \cos \theta \\ &= 2mg \times \frac{4}{5} \\ &= \frac{8mg}{5} \end{aligned}$$

Friction is limiting:

$$\begin{aligned} F &= \mu R \\ &= \frac{1}{4} \times \frac{8mg}{5} \\ &= \frac{2mg}{5} \end{aligned}$$

Work done against friction =  $Fs$

$$= \frac{2mgs}{5}$$

K.E. gained by  $A$  and  $B = \frac{1}{2}(2m)v^2 + \frac{1}{2}(3m)v^2$

$$= \frac{5mv^2}{2}$$

Work–energy principle:

K.E. gained + work done against friction = P.E. lost

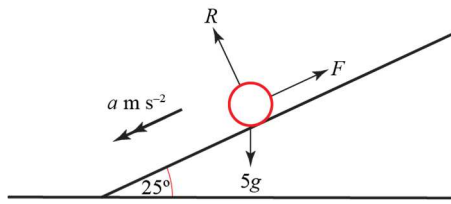
$$\frac{5mv^2}{2} + \frac{2mgs}{5} = \frac{9mgs}{5}$$

$$\frac{5mv^2}{2} = \frac{7mgs}{5}$$

$$v^2 = \frac{2 \times 7mgs}{5 \times 5m}$$

$$v^2 = \frac{14gs}{25}$$

8 a



Resolving parallel to the slope and using  $F = ma$ :

$$5g \sin 25^\circ - F = 5a$$

Friction is limiting:

$$F = \mu R$$

$$F = 0.3 \times 5g \cos 25^\circ$$

$$\text{So } 5g \sin 25^\circ - 5 \times 0.3 \times g \cos 25^\circ = 5a$$

$$a = g(\sin 25^\circ - 0.3 \cos 25^\circ)$$

Consider the motion down the slope.

$$u = 0 \text{ and } t = 2$$

$$v = u + at$$

$$= 0 + 2g(\sin 25^\circ - 0.3 \cos 25^\circ)$$

$$= 2g(\sin 25^\circ - 0.3 \cos 25^\circ)$$

$$= 2.9542\dots$$

After it has been moving for 2 s the parcel has speed  $2.95 \text{ m s}^{-1}$  (3 s.f.)

**b** In 2 s the parcel slides a distance  $s$  m down the sloping platform.

$$\text{Loss of P.E.} = mgh$$

$$= mg \times s \sin 25^\circ$$

$$= 5g \times s \sin 25^\circ$$

$$u = 0, v = 2.954 \text{ m s}^{-1}, t = 2 \text{ s}$$

$$\text{Using } s = \frac{u+v}{2} \times t$$

$$s = \frac{0 + 2.954}{2} \times 2 = 2.954$$

$$\text{So, loss of P.E.} = 5g \times 2.954 \times \sin 25^\circ$$

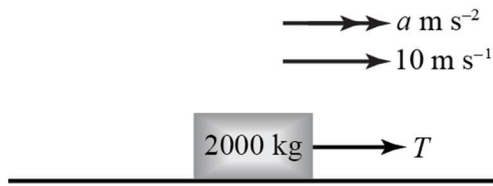
$$= 5 \times 9.8 \times 2.954 \times \sin 25^\circ$$

$$= 61.17\dots$$

During the 2 s, the parcel loses 61.2 J of potential energy (3 s.f.)



9



$$\text{Power} = 4000 \text{ W}$$

$$\text{Power} = Tv = 10T$$

$$\text{So } T = \frac{4000}{10} = 400 \text{ N}$$

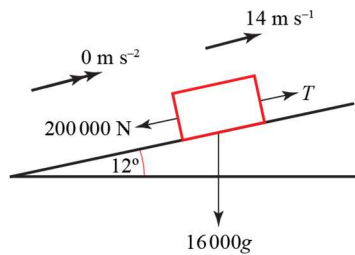
Using  $F = ma$ :

$$T = 2000 \times a$$

$$400 = 2000a$$

$$\text{So } a = \frac{400}{2000} = 0.2 \text{ m s}^{-2}$$

10



Resolving parallel to the slope:

$$T = 200000 + 16000g \sin 12^\circ$$

$$T = 232600.5 \dots$$

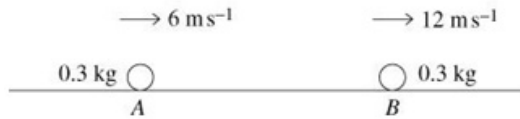
Work done in 10 s = force  $\times$  distance moved

$$= 232600 \dots \times (14 \times 10)$$

$$= 32564000 \text{ (3 s.f.)}$$

The work done in 10s is 32 600 000 J (or 32 600 kJ) (3 s.f.)

11



$$\begin{aligned} \text{a K.E. gained} &= \frac{1}{2}mv^2 - \frac{1}{2}mu^2 \\ &= \frac{1}{2} \times 0.3 \times 12^2 - \frac{1}{2} \times 0.3 \times 6^2 \\ &= 16.2 \end{aligned}$$

The K.E. gained is 16.2 J

b The work done by the force is 16.2 J

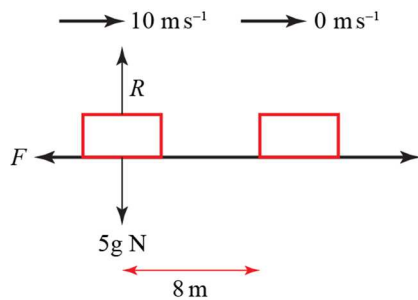
$$\begin{aligned} \text{c Work done} &= Fs \\ 16.2 &= F \times 4 \end{aligned}$$

$$F = \frac{16.2}{4}$$

$$F = 4.05$$

The force has magnitude 4.05 N

12



$$\begin{aligned} \text{a K.E. lost} &= \frac{1}{2}mu^2 - \frac{1}{2}mv^2 \\ &= \frac{1}{2} \times 5 \times 10^2 - 0 \\ &= 250 \end{aligned}$$

The K.E. lost is 250 J

b Work done against friction = 250 J

$$\begin{aligned} \text{Work done} &= Fs \\ 250 &= F \times 8 \end{aligned}$$

$$F = \frac{250}{8}$$

Resolving perpendicular to the slope:  $R = 5g$

Friction is limiting:  $F = \mu R$

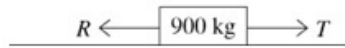
$$\frac{250}{8} = \mu \times 5g$$

$$\mu = \frac{250}{8 \times 5g}$$

The coefficient of friction is 0.638 (3 s.f.)

13

$$\longrightarrow 20 \text{ m s}^{-1} \quad \longrightarrow\!\!\!> 0.3 \text{ m s}^{-2}$$



**a** Power =  $Fv$

$$15000 = T \times 20$$

$$T = \frac{15000}{20} = 750$$

Using  $F = ma$ :

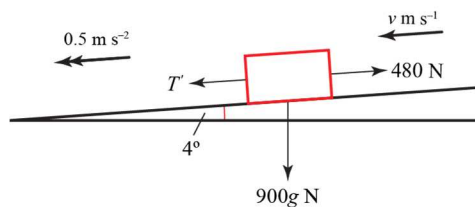
$$T - R = 900 \times 0.3$$

$$750 - R = 270$$

$$R = 750 - 270$$

$$R = 480$$

The magnitude of the resistance is 480 N

**b**

Resolving along the slope and using  $F = ma$ :

$$T' + 900g \sin 4^\circ - 480 = 900 \times 0.5$$

$$T' = 450 + 480 - 900g \sin 4^\circ$$

Power =  $Fv$

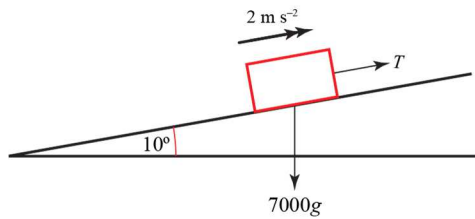
$$8000 = (450 + 480 - 900g \sin 4^\circ)v$$

$$v = \frac{8000}{(450 + 480 - 900g \sin 4^\circ)}$$

$$v = 25.41\dots$$

The speed of the car is  $25.4 \text{ m s}^{-1}$  (3 s.f.)

14



$$\text{Power} = Fv$$

$$\text{Power} = 4000 \text{ W}$$

$$T = \frac{4000}{v}$$

Resolving along the slope and using  $F = ma$ :

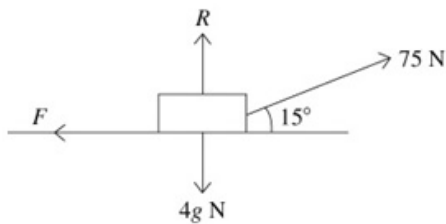
$$\frac{4000}{v} - 7000g \sin 10^\circ = 7000 \times 2$$

$$\frac{4000}{v} = 25912$$

$$\text{So } v = \frac{4000}{25912} = 0.154\dots$$

The speed of the bus is  $0.15 \text{ m s}^{-1}$  (2 s.f.)

15



$$\mu = \frac{3}{8}$$

**a** Resolving perpendicular to the floor:

$$R + 75 \sin 15^\circ = 4g$$

$$R = 4g - 75 \sin 15^\circ$$

Friction is limiting:

$$F = \mu R$$

$$F = \frac{3}{8} \times (4 \times 9.8 - 75 \sin 15^\circ)$$

$$F = 7.420\dots$$

The magnitude of the frictional force is  $7.42 \text{ N}$  (3 s.f.)

**b** Work done =  $F_s$

$$= 75 \cos 15^\circ \times 6$$

$$= 434.66\dots$$

The work done is  $435 \text{ J}$  (3 s.f.)

**15 c** Using the work–energy principle:

K.E. gained = work done by tension – work done against friction

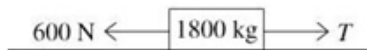
$$\frac{1}{2} \times 4v^2 = 434.66 - 7.420 \times 6$$

$$v^2 = \frac{1}{2}(434.66 - 7.420 \times 6)$$

$$v = 13.96\dots$$

The block is moving at  $14.0 \text{ m s}^{-1}$  (3 s.f.)

**16 a**  $\longrightarrow v \text{ m s}^{-1}$   $\longrightarrow\!\!\!\!\!\gg 0 \text{ m s}^{-2}$



At maximum speed,  $a = 0$

Resolving along the road and using  $F = ma$ :

$$T - 600 = 0$$

$$T = 600$$

Power =  $Fv$

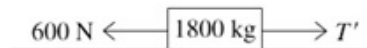
$$20000 = 600v$$

$$v = \frac{20000}{600}$$

$$v = 33.33$$

The lorry's maximum speed is  $33.3 \text{ m s}^{-1}$  (3 s.f.)

**b**  $\longrightarrow 20 \text{ m s}^{-1}$   $\longrightarrow\!\!\!\!\!\gg a \text{ m s}^{-2}$



Power =  $Fv$

$$20000 = T' \times 20$$

$$T' = 1000$$

Using  $F = ma$ :

$$T' - 600 = 1800a$$

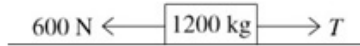
$$1000 - 600 = 1800a$$

$$a = \frac{400}{1800}$$

$$a = 0.2222\dots$$

The acceleration of the lorry is  $0.222 \text{ m s}^{-2}$  (3 s.f.)

17  $\longrightarrow 20 \text{ m s}^{-1}$   $\longrightarrow\!\!\!\!\!\gg 0 \text{ m s}^{-2}$



a Resolving along the road:  $T = 600$

$$\begin{aligned} \text{Power} &= Fv \\ &= 600 \times 20 \\ &= 12000 \text{ W} \\ &= 12 \text{ kW} \end{aligned}$$

The power is 12 kW

b  $\longrightarrow 20 \text{ m s}^{-1}$   $\longrightarrow\!\!\!\!\!\gg 0.5 \text{ m s}^{-2}$



$$F = ma$$

$$T' - 600 = 1200 \times 0.5$$

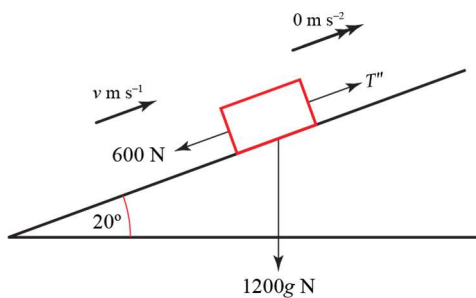
$$T' = 600 + 600$$

$$T' = 1200$$

$$\begin{aligned} \text{Power} &= F \times v \\ &= 1200 \times 20 \\ &= 24000 \end{aligned}$$

The new rate of working is 24 kW

c



Resolving along the slope:

$$T'' = 600 + 1200g \sin 20^\circ$$

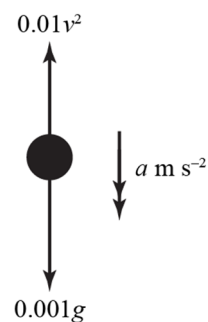
$$\text{Power} = Fv$$

$$50000 = (600 + 1200g \sin 20^\circ)v$$

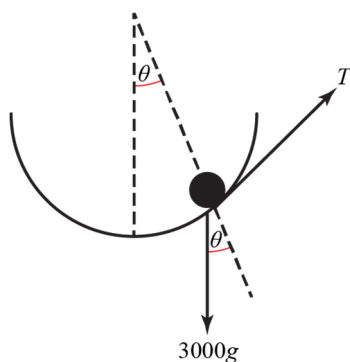
$$v = \frac{50000}{(600 + 1200g \sin 20^\circ)}$$

$$v = 10.82\dots$$

The value of  $v$  is 10.8 (3.s.f.)



## Challenge



- a** Car is moving with constant speed in a direction along the tangent to the cylinder.  
Resolving along the path of the car:

$$T = 3000g \sin \theta$$

$$\text{Power} = Tv$$

$$\text{Power} = 3000g \sin \theta \times 20 = 60\,000g \sin \theta = 588\,000 \sin \theta \text{ W}$$

- b** When  $\theta = 0^\circ$ , there is no force to act against, so no power is required.  
When  $\theta = 90^\circ$ , maximum power is needed.