

OCR Maths M2

Mark Scheme Pack

2005-2014

<b>1</b>	(i)	use of $h/4$	B1			
		com vert above lowest pt of contact	B1		can be implied	
		$r = 5 \times \tan 24^\circ$	M1			
		$r = 2.2$	A1	4	2.226	
	(ii)	No & valid reason (eg $24^\circ \rightarrow 26.6^\circ$ )	B1✓	1	✓Yes if their $r \approx 2.5$	<b>5</b>

<b>2</b>		$v^2 = 2 \times 9.8 \times 10$	M1		energy: $\frac{1}{2}mv^2 = \frac{1}{2}mu^2 + mgh$	
		$v = 14$	A1		$\frac{1}{2}v^2 = \frac{1}{2} \cdot 36 + 9.8 \times 10$	
		speed = $\sqrt{(14^2 + 6^2)}$	M1		(must be $6^2$ ) $v^2 = 36 + 196 = 232$	
		speed = $15.2 \text{ ms}^{-1}$	A1			
		$\tan \theta = 14/6$	M1		$\cos^{-1}(6/15.2)$ etc	
		$\theta = 66.8^\circ$ (below) horiz.	A1	6	or $23.2^\circ$ to the vertical	<b>6</b>

<b>3</b>	(i)	$T \cos \theta = 0.01 \times 9.8$	M1		resolving vertically	
		$8/10T = 0.01 \times 9.8$	A1		with $\cos \theta = 8/10$	
		$T = 0.1225 \text{ N}$	A1	3	AG	
	(ii)	$T + T \sin \theta = ma$	M1		resolving horizontally	
		use of $m r \omega^2$	M1			
		$\omega = 5.72 \text{ rads}^{-1}$	A1	3		
	(iii)	$\text{K.E.} = \frac{1}{2} \times 0.01 \times (r\omega)^2$	M1		$\frac{1}{2}mv^2$ with $v=r\omega$	
		$\text{K.E.} = 0.0588$	A1✓	2	✓ $0.0018 \times \text{their } \omega^2$	<b>8</b>

<b>4</b>	(i)	$5m = mu + 4m$	M1		cons. of mom.	
		$u = 1$	A1			
		$e = (2-1)/5$	M1			
		$e = \frac{1}{5}$	A1	4		
	(ii)	$I = 4m$	B1			
		$\rightarrow$	B1	2	to the right	
	(iii)	$4m = 5mv$	M1			
		$v = \frac{4}{5}$	A1			
		$\frac{4}{5} < 1$	B1	3		<b>9</b>

<b>5</b>	(i)	$60T = 15 \times 30 \cos \theta$	M1		moments about A	
		“	A1			
		$60T = 15 \times 30 \times 0.6$	A1		$\cos \theta = 0.6$	
		$T = 4.5 \text{ N}$	A1	4	AG	
	(ii)	$X = T \sin \theta$	M1		res. horiz. (or moments)	
		$X = 3.6 \text{ N}$	A1			
		$Y + T \cos \theta = 15$	M1		res. vert.(3 terms) (or moments)	
		$Y = 12.3 \text{ N}$	A1			
		$R = 12.8 \text{ N}$	A1✓		✓(their $X^2 + Y^2$ )	
		$73.7^\circ$ to horizontal	A1✓	6	or $16.3^\circ$ to vert. ✓ $\tan^{-1}$ their $(Y/X)$	<b>10</b>
		<b>or triangle of forces:</b> Triangle (M1) $R^2 = 15^2 + 4.5^2 - 2 \times 4.5 \times 15 \times 0.6$ (M1A1)				
		$R = 12.8$ (A1) $\sin \theta / 4.5 = \sin \alpha / 12.8$ (M1) $\theta = 16.3^\circ$ to vert. (A1)				

6	(i)	$\frac{1}{2} \cdot 700 \cdot 20^2$ or $\frac{1}{2} \cdot 700 \cdot 15^2$	B1		either K.E.	
		$700 \times 9.8 \times 400 \sin 5^\circ$	B1		correct P.E.	
		$\frac{1}{2} \cdot 700 \cdot 15^2 + 700 \cdot 9.8 \cdot 400 \sin 5^\circ =$ $\frac{1}{2} \cdot 700 \cdot 20^2 + \text{W.D.}$	M1		for 4 terms with W.D.	
		W.D. = 178,000 J	A1	4	or 178 kJ	
	(ii)	$D = 200 + 700 \cdot 9.8 \sin 5^\circ$	M1			
		$D = 798 \text{ N}$	A1		may be implied	
		$P = D \times 15 = 12,000 = 12 \text{ kW}$	A1	3	AG (11,968W)	
	(iii)	$D' = 11,968 \div 20 = 598$	M1			
		$D' - 700 \cdot 9.8 \sin 5^\circ - 200 = 700a$	M1			
		$a = 0.285 \text{ ms}^{-2}$ ( $\pm$ )	A1	3	allow 0.283 (from 12kW)	10
<b>Alternative for false assumption</b>					<b>of constant acceleration</b>	
(i)	$D - 700 \times 9.8 \sin 5^\circ = 700a$ and $15^2 = 20^2 + 2a \cdot 400$	M1		(D = 445, a = -0.21875)		
	W.D. = $400 \times D = 178,000$	A1		2 marks (out of 4) maximum		

7	(i)	$50 \times 9.8 \times 2 = R \times 3.75 + 80 \times 9.8 \times 0.25$	M1		moments about D.	
		“	A1		SR/no g/ R = 21.3 (M1A1A0)	
		R = 209 N	A1	3		
	(ii)	$130 \bar{x} = 50 \times 2 + 80 \times 4.25$	M1 A1		moments about BC or FE..... $130 \bar{x} = 80 \times 0.25 + 50 \times 2.5$	
		$\bar{x} = 3.385$	A1		$\bar{x} = 1.115$	
		$130 \bar{y} = 50 \times 0.125 + 80 \times 0.25$	M1 A1		moments about EC	
		$\bar{y} = 0.202$	A1			
		$\tan \theta = 0.615 / 0.202$	M1			
		$\theta = 71.8^\circ$ to the horizontal	A1	8	$71.6^\circ$ to $72.0^\circ$	11

8	(i)	$x = 49 \cos \theta \cdot t$	B1			
		$y = 49 \sin \theta \cdot t - \frac{1}{2} \cdot 9.8 \cdot t^2$	B1			
		$y = x \tan \theta - 4.9x^2 / 49^2 \cdot \cos^2 \theta$	M 1		aef (eliminating t)	
		$y = x \tan \theta - x^2(1 + \tan^2 \theta) / 490$	A1	4	AG	
	(ii)	$30 = 70 \tan \theta - 10(1 + \tan^2 \theta)$	M 1			
		$\tan \theta = (70 \pm \sqrt{3300}) \div 20$	M 1		(6.37/0.628)	
		$81.1^\circ$	A1		$\theta_1$ or $\theta_2$	
		$32.1^\circ$	A1	4	“	
	(iii)	$x^2(1 + \tan^2 \theta) / 490 = x \tan \theta$	M 1		set y = 0	
		$x = 490 \tan \theta / (1 + \tan^2 \theta)$	A1			
$x = 75.0$		A1				

	$x = 221$ (220.6)	A1			
	$d = 146$ m	A1 ✓	5	✓	<b>13</b>
(iii)	Alternatively (1 <sup>st</sup> 2 marks)				
	$t = 49 \sin \theta / 4.9$ and (9.88/5.31) $x = 49 \cos \theta . t$	M 1		$s = ut + \frac{1}{2}at^2$ and $x = 49 \cos \theta . t$ or $R = u^2 \sin 2\theta / g$ (precise)	
	$x = 490 \sin \theta \cos \theta$	A1		$245 \sin 2\theta$	

<b>1</b>		$\tan\theta = \frac{1}{3}$ ( $\theta = 18.4^\circ$ at B)	B1		71.6° at C
		$3 \times T \sin\theta = 20 \times 1.5$ must	M1		M(A) ( $d=3/\sqrt{10}$ )
		have two distances and no g	A1		
		$T = 31.6$ N	A1	4	<b>4</b>

<b>2</b>	(i)	$0 = 50 \sin 25^\circ t - 4.9t^2$	M1		or $0=50\sin 25^\circ - 9.8t$ & $2t : 2 \times 2.16$	
			A1			
		$t = 4.31$ s	A1	3		
	(ii)	$d = 50 \cos 25^\circ \times 4.31$	M1		or $u^2 \sin(2 \times 25^\circ)/g$	
		195 m	A1✓	2	✓ $50 \cos 25^\circ \times$ their t	<b>5</b>

<b>3</b>	(i)a	100 J	B1	1		
	b	7500 Nm	B1	1		
	(ii)	$400 \cos \alpha \times 25 = 7500 + 100$	M1		sc N II gets M1A1 only. This M1	
		✓ for $a + b$	A1✓		for total M ( $a=0.08$ ) & A1 for $\alpha$	
		$\alpha = 40.5$	A1	3	or 0.707 rads	<b>5</b>

<b>4</b>	(i)	horiz comps in opp direct	B1		at E & F	
		Right at E + Left at F	B1	2		
	(ii)	$1.6 \times 9.8 \times 30 = 20X$ or	M1		or $10X + 1.6g \times 30 = 30X$ M(A)	
		$0.5 \times 30g + 0.7 \times 30g +$	A1		or $10X + (\dots = 470.4) = 30X$ M	
		$0.2 \times 60g = 20X$	A1	3	mark ok without g but 3 parts	
	(iii)	$1.6 \bar{y} =$	M1		must be moments with vert dists	
		$20 \times 0.2 + 20 \times 0.2 + 40 \times 0.5$	A1		or $1.6 \bar{y} = 20 \times 0.2 \times 2 + 40 \times 0.7 (22.5)$	
		$\bar{y} = 17.5$ cm	A1	3		<b>8</b>

<b>5</b>	(i)	$6m = 3mx + 2my$	M1		- 3mx ok if clear on diagram	
		$6 = 3x + 2y$	A1		m must have been cancelled	
		$e = 1 = (y-x)/2$	M1		or $\frac{1}{2} \cdot 3m \cdot 2^2 = \frac{1}{2} \cdot 3mx^2 + \frac{1}{2} \cdot 2my^2$	
			A1		$6 = 3x^2/2 + y^2$ aef	
		$x = 0.4$ or $2/5$	A1		sc A1A0 if $x = 2, y = 0$ not rejected	
		$y = 2.4$ or $12/5$	A1	6		
	(ii)	$4.8m$ or $24m/5$	B1✓		✓ $2m \times$ their y or $3m(2 - \text{their } x)$	
		same as original dir. of A	B1	2	use their diagram (or dir. of B)	
	(iii)	$e = (2.8 - 1.0)/2.4$	M1			
		0.75 watch out for $\pm$ fiddles	A1✓	2	✓ $(1.8/\text{their } y)$ with $0 < e < 1$	<b>10</b>

<b>6</b>	(i)	$x = 7t$	B1			
		$y = -4.9t^2$ or $-\frac{1}{2}gt^2$	M1		some attempt at vertical motion	
			A1		sc $y = x \tan \theta - gx^2 / (2V^2 \cos^2 \theta)$	
		$y = -x^2/10$ <b>AG</b> (no fiddles)	A1	4	with $\theta=0$ M1 then A1 (max = 2)	
	(ii)	$-20 = -x^2/10$	M1		or $t = \sqrt{(20/4.9)}$ & $x=7t$	
		14.1 m	A1	2	sc B1 for 14.1 after wrong work	
	(iii)	$\frac{1}{2}mv^2 = \frac{1}{2}m7^2 + mgx20$ n.b. $v^2 = u^2$	M1		<b>OR</b> $v_h = 7$ (B1)	
		+2as gets M0	A1		$v_v = \pm 19.8$ (B1) $14\sqrt{2}, 2\sqrt{98}$ etc	
		$v = 21 \text{ ms}^{-1}$	A1		$v = 21$ (B1)	
		$dy/dx = -2x/10$ & $\tan \theta$	M1		<b>OR</b> $\tan \theta = 19.8/7$ or	
			A1		$\cos \theta = 7/21$ or $\sin \theta = 19.8/21$	
		70.5° to horizontal	A1	6	or 19.5° to vertical	<b>12</b>

<b>7</b>	(i)	$F = 300/12$	M1			
		$R = 25$	A1	2		
	(ii)	$P = 17.5 \times 12$ ( $R_2 = 17.5$ & $F_2 = 17.5$ )	M1		n.b. B1 only for 210 W	
		$P = 210 \text{ W}$	A1	2	without working	
	(iii)	$500 = Fx12$	M1			
		$F = 41.67$ or $500/12$ aef	A1			
		$41.67 - 25 - 75 \times 9.8 \sin 1^\circ = 75a$	M1			
			A1			
		$0.0512 \text{ ms}^{-2}$	A1	5	or 0.051	
	(iv)	$PE = 75 \times 9.8 \times 200 \sin 10^\circ$ (25530)	B1		<b>OR</b> $75 \times 9.8 \sin 10^\circ - 120 = 75a$	
		$WD = 200 \times 120$ (24000)	B1		(M1 + A1)	
		$\frac{1}{2} \cdot 75v^2 =$	M1		$a = 0.102$ (A1)	
		$\frac{1}{2} \cdot 75 \cdot 13^2 + 75 \times 9.8 \times 200 \sin 10^\circ - 200 \cdot 120$	A1		$v^2 = 169 + 2 \times 0.102 \times 200$ (M1)	
		$14.5 \text{ ms}^{-1}$	A1	5	$v = 14.5$	<b>14</b>

<b>8</b>	(i)	$R \cos 30^\circ = 0.1 \times 9.8$	M1		resolving vertically	
			A1			
		$R = 1.13 \text{ N}$	A1	3		
	(ii)	$r = 0.8 \cos 30^\circ = 0.693$ or $2\sqrt{3}/5$	B1		may be implied	
		$R \cos 60^\circ = 0.1 \times 0.693 \omega^2$	M1		or $0.1v^2/r$ & $\omega = v/r$	
			A1			
		$\omega = 2.86$	A1	4		
	(iii)	$T = 1.96 \text{ N}$	B1	1		
	(iv)	$R \cos 30^\circ = T \cos 60^\circ + 0.1 \times 9.8$	M1			
				A1		
		$R = 2.26 \text{ N}$	A1			
		$R \cos 60^\circ + T \cos 30^\circ = 0.1 \times v^2/r$	M1		or $m\omega^2$ & use of $v = r\omega$	
			A1		with $R=1.13$ can get M1 only	
		$4.43 \text{ ms}^{-1}$	A1	6		<b>14</b>
<b>or</b>	(iv)	LHS (or RHS)	M1*		method without finding R	
		$T + 0.1 \times 9.8 \cos 60^\circ$	A1		i.e. resolving along PA	
		RHS (or LHS)	M1*			
		$0.1 \times v^2/r \times \cos 30^\circ$	A1		r to be $0.8 \cos 30^\circ$ for A1	
		solve to find v	M1*		depends on 2* Ms above	
		$4.43 \text{ ms}^{-1}$	A1	(6)		

1		$mgh = 35 \times 9.8 \times 4$  $mgh/t = 1372/10$ 137 W	M1 A1 M1 A1	4	watch out for extras or 0.137 kW	4
2		$v^2 = 2gh$ $u = \sqrt{4g}$ or $\sqrt{39.2}$ or 6.26 $v = \sqrt{2.8g}$ or $\sqrt{27.44}$ (5.24) $I = \rho 0.3(6.26 + 5.24)$ 3.45 Ns	M1 A1 A1 M1 A1✓	5	kinematics or energy speed of impact ( $\pm$ ) speed of rebound ( $\pm$ ) must be sum of mags. of vels. ✓ must be positive	5
3	(i)	$d = 2.25$ $h = 1.125$ or 1.12 or 1.13 or 9/8	B1 B1	2	3/8x6 OG (be generous) horizontal distance	7
	(ii)	$T_1 + T_2 = 12$ resolving vertically $T_1 \times 6\cos 30^\circ = 12xh$ (their h) mom(O) (their h ok for A1) $T_1 = 2.60$ N or $3\sqrt{3}/2$ $T_2 = 9.40$ N ✓ ( $12 - T_1$ ) above ✓ depends on at least one of the M marks ( $T_s > 0$ )	M1 M1 A1 A1 A1✓	5	if not then next M1 ok or $\text{mom}(A)T_2 \times 6\cos 30^\circ =$ $12(6\cos 30^\circ - h)$ or $T_2 = 9.40$ or $T_1 = 2.60$ or ✓( $12 - T_2$ )	
4	(i)	$P = 13500$ W	B1	1	or 13.5 kW	9
	(ii)	$500 = 13500/v$ $v = 27$ ms <sup>-1</sup>	M1 A1	2		
	(iii)	$15000/25 - 500 = 950a$  $a = 0.105$ or $2/19$	M1 A1 A1	3	2 parts to F A0 for 900a or 100/950	
	(iv)	$15000/26 - 500 -$ $950.9.8\sin 5^\circ = 950a$ $a = (-).773$ ms <sup>-2</sup>	M1 A1 A1	3	3 parts to F A0 for 900a s.c. accept 0.77	
5	(i)	$\bar{x} = 9$ c of m of $\Delta$ 4 cm above BD  $(324 + 108)(m)\bar{y} =$ $324(m) \times 9 + 108(m) \times (18+4)$ $432\bar{y}$ $324 \times 9$ (18 <sup>2</sup> x 9) $108 \times (18 + 4)$ $\bar{y} = 12.25$	B1 B1  M1 A1 A1 A1 A1	7	ignore any working  8 cm below C/see their diagram $432\bar{y} = 108 \times 8 + 18^2(12 + 9)$ from C left hand side 1 <sup>st</sup> term on right hand side 2916 2 <sup>nd</sup> term on right hand side 2376 $5292 \div 432$ or 49/4	9
	(ii)	$\tan \theta = 5.75/9$ $\theta = 32.6^\circ$ or $147.4^\circ$	M1 A1✓	2	must be .../9 ✓ $\tan^{-1}((18 - \text{their } \bar{y})/9)$ or $180^\circ..$	

6	(i)	$T = 4.9 \text{ N}$ $T = 0.3 \times 0.2 \times \omega^2$  $\omega = 9.04 \text{ rads}^{-1}$	B1 M1 A1 A1	4	B0 for 0.5g or $0.3v^2/0.2$ and $\omega = v/0.2$	6
	(ii)	$\cos\theta = \sqrt{0.6/0.8}$ (0.968) $T\cos\theta = 0.5 \times 9.8$  $T = 5.06 \text{ N}$	B1 M1 A1 A1	4	$(\theta=14.5^\circ)$ angle to vert. or equiv. angle consistent with diagram can be their angle	
	(iii)	$T\sin\theta = 0.5 \times v^2/0.2$  $v = 0.711 \text{ ms}^{-1}$	M1 A1 A1	3	must be a component of T $(\sin\theta = 1/4)$ can be their angle	11
7	(i)	$v\sin 50^\circ$ $0 = v^2\sin^2 50^\circ - 2 \times 9.8 \times 13$ (must be 13) $v = 20.8 \text{ ms}^{-1}$	B1 M1  A1	3	initial vertical component or $m \times 9.8 \times 13 = \frac{1}{2}m(v\sin 50^\circ)^2$  sin/cos mix ok for above M1	13
	(ii)	$45 = v\cos 50^\circ \cdot t$ $t = 3.36$ ✓ their v (3.13 for $v=22.4$ ) $s = v\sin 50^\circ \times t - \frac{1}{2} \times 9.8 \times t^2$  $s = -1.6$ to $-2.0$ inclusive (-1.68) ht above ground = 0.320 m	M1 A1 ✓  M1 A1 A1 A1	6	see alternative below other methods include other $t_s$  ignore ht adjustments can be their v and their t can be implied from next A1	
	(iii)	$v_v = v\sin 50^\circ - 9.8 \times t$ $v_v = -17.0$ ✓ their v, t (-13.5 for 22.4) $\text{speed} = \sqrt{(v_v^2 + (v\cos 50^\circ)^2)}$ $\text{speed} = 21.6 \text{ ms}^{-1}$ ✓ their v and $v_v$ (19.7 for $v = 22.4$ )	M1 A1 ✓  M1 A1 ✓	4	or $v_v^2 = 2g(15 - \text{their ans to ii})$ ✓ above for $v_v$  or $\frac{1}{2}mv^2 - mgx1.68 = \frac{1}{2}m \times 20.8^2$ (4 marks) M1/A1 ✓ s,v /M1 solve/ A1 ✓	
	(ii)	$y = x\tan\theta - gx^2/2v^2\cos^2\theta$ $y = 45\tan 50^\circ - 9.8 \cdot 45^2 / 2 \cdot v^2 \cos^2 50^\circ$  calculate y $y = -1.6$ to $-2.0$ inclusive	B1 M1  A1 M1 A1		<b>Alternative 1<sup>st</sup> 5 marks</b> substitute v and $50^\circ$ and $x=45$  can be their v  should be $-1.68$	



8	(i)	$10 = 4 + m \cdot x$ $e = \dots$ or rationale for $x = 2$ $m = 3$	M1 M1 A1	3	conservation of momentum	
	(ii)	$v = 6$ $e = 4/5$ or 0.8	B1 M1 A1			
	(iii)	$10 - 5 = 2x + y$ ( $5 = -2a + b$ ) $(-5 = 2c + d)$  $e = 0.8 = (y-x)/10$ $y = x + 8$ ( $a + b = 8$ ) ( $c - d = 8$ ) $x = -1$ ( $a=1$ ) ( $c=1$ ) $y = 7$ ( $b=7$ ) ( $d=-7$ ) $\frac{1}{2} \cdot 2 \cdot 5^2 + \frac{1}{2} \cdot 1 \cdot 5^2 - \frac{1}{2} \cdot 2 \cdot 1^2 - \frac{1}{2} \cdot 1 \cdot 7^2$ 12 J	M1  A1 M1 A1 A1 A1 M1 A1	8	look for consistency  or 1 in opp. direction to 1st  K.E. lost. Must be 4 parts	
			(37.5 – 25.5)		<b>14</b>	

$\pm 1$  in 3<sup>rd</sup> sig. fig. except where stated

<b>1</b>		com directly above lowest point	B1			
		$\tan \alpha = 6/10$	M1			
		$\alpha = 31.0$	A1	3	or 0.540 rads	<b>3</b>
<b>2</b>		$e = 1 = (y-x)/4$	B1		or $\frac{1}{2}x0.2x^2 + \frac{1}{2}x0.1y^2 =$	
		$0.8 = 0.2x + 0.1y$	B1		$\frac{1}{2}x0.2x4^2$ (B1/B1 for any 2)	
		solving sim. equ.	M1		not if poor quad. soln.	
		$x = 4/3$ only	A1	4		<b>4</b>
<b>3</b>	(i)	$x^2 = 21^2 + 2x40x9.8$	M1			
		$x = 35$	A1			
		$0 = y^2 - 2x40x9.8$	M1			
		$y = 28$	A1		may be implied	
		$e = 28/35$	M1			
		$e = 0.8$	A1	6	aef	
	(ii)	$0.2x28 - -0.2x35$	M1		must be double negative	
		$I = 12.6$	A1	2		<b>8</b>
<b>4</b>	(i)	$\frac{1}{2}x80x5^2$ or $\frac{1}{2}x80x2^2$ either KE	B1		1000/160	
		$70 \times 25$	B1		1750	
		$80x9.8x25\sin20^\circ$	B1		6703.6	
		$WD = \frac{1}{2}x80x5^2 - \frac{1}{2}x80x2^2 + 70x25 + 80x9.8x25\sin20^\circ$	M1		4 parts	
		9290	A1	5		
	(ii)	$P\cos30^\circ x25$	B1		or $a=0.42$	
		$P\cos30^\circ .25 = 9290 / P\cos30^\circ - 70 - 80x9.8\sin20^\circ = 80a$	M1			
		$P = 429$ /if P found 1 <sup>st</sup> then $P\cos30^\circ x25 = 9290$ ok	A1	3		<b>8</b>
<b>5</b>	(i)	$D = 3000/5^2 = 120$	M1			
			A1	2	<b>AG</b>	
	(ii)	$120 - 75 = 100a$	M1			
		$a = 0.45 \text{ ms}^{-2}$	A1	2		
	(iii)	$100x9.8x1/98$	B1		weight component	
		$3000/v^2 = 3v^2 + 100x9.8x1/98$	M1			
		$3000 = 3v^4 + 10v^2$	A1		aef	
		solving quad in $v^2$	M1		$(v^2 = 30)$	
	$v = 5.48 \text{ ms}^{-1}$	A1	5	accept $\sqrt{30}$	<b>9</b>	
<b>6</b>	(i)	com of $\Delta$ 4 cm right of C	B1			
		$1.5 \times 10 + 7 \times 20 = \bar{x} \times 30$	M1			
			A1			
		$\bar{x} = 5.17$	A1		5 1/6 31/6	
		com of $\Delta$ 6 cm above E	B1		or 3 cm below C	
		$4.5 \times 10 + 6 \times 20 = \bar{y} \times 30$	M1			
			A1			
		$\bar{y} = 5.5$	A1	8		
	(ii)	$\tan\theta = 5.17/3.5$	M1		right way up and $(9 - \bar{y})$	
		$55.9^\circ$ or $124^\circ$	A1✓	2	✓ their $\bar{x}/(9 - \bar{y})$	
	(iii)	$d = 15\sin45^\circ$ (10.61)	B1		dist to line of action of T	
$Td = 30 \times 5.17$		M1		allow $Tx15$ i.e. T vertical		
$T = 14.6$		A1	3		<b>13</b>	

7	(i)	$T\sin 30^\circ$	B1		
		$T\sin 30^\circ = 0.3 \times 0.4 \times 2^2$	M1		resolving horizontally
			A1		
		$T = 0.96$	A1	4	
	(ii)	$R + T\cos 30^\circ = 0.3 \times 9.8$	M1		resolving vertically
			A1		
		$R = 2.11$	A1✓	3	✓ their T (2.94 – $T\cos 30^\circ$ )
	(iii)	$T_1\sin 30^\circ = 0.3 \times v^2/0.4$	M1		or $0.3 \times 0.4 \times \omega^2$
			A1		( $T_1 = 1.5v^2$ )
		$T_1\cos 30^\circ = 0.3 \times 9.8$	B1		( $T_1 = 1.96\sqrt{3} = 3.3948$ )
		$R = 0$	B1		may be implied or stated
		$\tan 30^\circ = v^2 / (0.4 \times 9.8)$ for elim of $T_1$	M1		and $v = 0.4\omega$ ( $\omega = 3.76$ )
		$v = 1.50$	A1	6	
					<b>13</b>

8	(i)	$v_v = 42\sin 30^\circ (=21)$	B1		
		$0 = 21^2 - 2 \times 9.8xh$	M1		
		$h = 22.5$	A1	3	
	(ii)	$v_h = 42\cos 30^\circ (=36.4)$	B1		
			$v_v = \pm v_h \times \tan 10^\circ$	M1	
		$v_v = \pm 6.41$ or $21\sqrt{3} \tan 10^\circ$	A1		or $42\cos 30^\circ \cdot \tan 10^\circ$
		$-6.41 = 42\sin 30^\circ - 9.8t$	M1	**	must be $-6.41$ (also see "or" x 2)
		$t = 2.80$	A1	**	
		$y = 42\sin 30^\circ \times 2.8 - 4.9 \times 2.8^2$	M1	**	
		$y = 20.4$	A1✓	**	✓ their t
		$x = 42\cos 30^\circ \times 2.80$	M1		
		$x = 102$	A1✓		✓ their t
		$\sqrt{(x^2 + y^2)}$	M1		
		$d = 104$	A1	11	
	or	$6.41^2 = 21^2 + 2 \times -9.8s$	M1	**	vert dist first then time
		$s = 20.4$	A1	**	
		$20.4 = 21t + \frac{1}{2} \cdot -9.8t^2$	M1	**	
		$t = 2.80$	A1	**	
	or	$22.5 - s$ and $6.41^2 = 2 \times 9.8s$	M1	**	dist from top ( $s = 2.096$ )
		$y = 20.4$	A1	**	
		$22.5 \& 2.1 = \frac{1}{2} \cdot 9.8t^2$	M1	**	2 separate times (2.143, 0.654)
		$t = 2.80$	A1	**	2.143 + 0.654
		<b>alternatively</b>			
	(ii)	$y = x/\sqrt{3} - x^2/270$ aef	B1		$y = x\tan 30^\circ - 9.8x^2/2 \cdot 42^2 \cdot \cos^2 30^\circ$
			$dy/dx = 1/\sqrt{3} - x/135$	M1	
			A1		aef
		$dy/dx = -\tan 10^\circ$	M1		must be $-\tan 10^\circ$
		$1/\sqrt{3} - x/135 = -\tan 10^\circ$	A1		
		solve for x	M1		
		$x = 102$	A1✓		✓ on their dy/dx
		$y = x/\sqrt{3} - x^2/270$	M1		
		$y = 20.4$	A1✓		✓ their x
		$\sqrt{(x^2 + y^2)}$	M1		
		$d = 104$	A1	(11)	

<b>1</b>	$40 \cos 35^\circ$	B1	
	$WD = 40 \cos 35^\circ \times 100$	M1	
	3280 J	A1 <b>3</b>	ignore units <b>3</b>
<b>2</b>	$0 = 12 \sin 27^\circ t - 4.9t^2$ any correct.	M1	or $R = u^2 \sin 2\theta / g$ (B2)
	$t = 1.11$ .....method for total time	A1	correct formula only
	$R = 12 \cos 27^\circ \times t$	M1	$12^2 \times \sin 54^\circ / 9.8$ sub in values
	11.9	A1 <b>4</b>	11.9 <b>4</b>
<b>3 (i)</b>	$WD = \frac{1}{2} \times 250 \times 150^2 - \frac{1}{2} \times 250 \times 100^2$	M1	
	1 560 000	A1	1 562 500
	$450\,000 = 1\,560\,000/t$	M1	
	3.47	A1 <b>4</b>	
<b>(ii)</b>	$F = 450\,000/120$	M1	
	3750	A1	
	$3750 = 250a$	M1	
	$15 \text{ ms}^{-2}$	A1 <b>4</b>	<b>8</b>
<b>4 (i)</b>	$x = 7t$	B1	
	$y = 21t - 4.9t^2$	M1	or $-g/2$
		A1	
	$y = 21 \cdot x/7 - 4.9 x^2/49$	M1	
	$y = 3x - x^2/10$	A1 <b>5</b>	<b>AG</b>
<b>(ii)</b>	$-25 = 3x - x^2/10$ (must be -25)	M1	or method for total time (5.26)
	solving quadratic	M1	or 7 x total time
	36.8 m	A1 <b>3</b>	<b>8</b>
<b>5(i)</b>	$\frac{1}{2} \cdot 70 \cdot 4^2$	M1	
	560 J	A1 <b>2</b>	
<b>(ii)</b>	$70 \times 9.8 \times 6$	M1	
	4120	A1 <b>2</b>	4116
<b>(iii)</b>	60d	B1	
	$8000 = 560 + 4120 + 60d$	M1	4 terms
		A1 ✓	✓ their KE and PE
	55.4 m	A1 <b>4</b>	<b>8</b>

<b>6 (i)</b>	$5\cos 30^\circ = 0.3 \times 9.8 + S\cos 60^\circ$	M1	res. vertically (3 parts with comps)
		A1	
	2.78 N	A1	<b>3</b>
<b>(ii)</b>	$r = 0.4\sin 30^\circ = 0.2$	B1	may be on diagram
	$5\sin 30^\circ + S\sin 60^\circ = 0.3 \times 0.2 \times \omega^2$	M1	res. horizontally (3 parts with comps)
	$9.04 \text{ rads}^{-1}$	A1	<b>3</b>
<b>(iii)</b>	$v = 0.2 \times 9.04$	M1	<b>or</b> previous $v$ via $mv^2/r$
	$KE = \frac{1}{2} \times 0.3 \times (0.2 \times 9.04)^2$	M1	
	0.491 J or 0.49	A1 ✓	<b>3</b> ✓ their $\omega^2 \times 0.006$ <b>9</b>

<b>7 (i)</b>	$1.8 = -0.3 + 3m$	M1	
	$m = 0.7$	A1	<b>2</b> <b>AG</b>
<b>(ii)</b>	$e = 4/6$	M1	accept 2/6 for M1
	2/3	A1	<b>2</b> accept 0.67
<b>(iii)</b>	$\pm 3f$	B1	
	$1/3 \text{ } \odot \text{ } f \text{ ( } \ominus \text{ } 1 \text{ )}$	B1	<b>2</b>
<b>(iv)</b>	$I = 3f \times 0.7 - - 3 \times 0.7$	M1	ok for only one minus sign for M1
		A1	
	$I = 2.1 (f + 1)$	A1	<b>3</b> aef 2 marks only for $-2.1(f + 1)$
<b>(v)</b>	$0.3 + 6.3/4 = 0.3a + 0.7b$	M1	can be $-0.7b$
	$3a + 7b = 18.75$	A1	*
	$2/3 = (a - b)/ 5/4$	M1	allow $e=3/4$ or their $e$ for M1
	$3a - 3b = 5/2$	A1	*
	solve	M1	aef * means dependent.
	$a = 2.5$	A1	(2.46) allow $\pm$ (59/24)
	$b = 1.6$	A1	<b>7</b> (1.625) allow $\pm$ (13/8) <b>16</b>

<b>8 (i)</b>	com of hemisphere 0.3 from $O$	B1	<b>or</b> 0.5 from base
	com of cylinder $h/2$ from $O$	B1	
	$0.6 \times 45 = 40 \times 0.5 + (0.8 + h/2) \times 5$ <b>or</b>	M1	<b>or</b> $40 \times 0.3 - 5xh/2 = 45 \times 0.2$
	$45(h+0.2) = 5h/2 + 40(h+0.3)$	A1	<b>or</b> $5(0.2 + h/2) = 40 \times 0.1$
	$27 = 20 + (0.8 + h/2) \times 5$	M1	solving
	$h = 1.2$	A1	<b>6</b> <b>AG</b>
<b>(ii)</b>	1.2 T	B1	
	0.8 F	B1	
	$0.8F = 1.2T$	M1	
	$F = 3T/2$	A1	<b>4</b> aef
<b>(iii)</b>	$F + T\cos 30^\circ$	B1	<b>or</b> $45 \times 0.8 \sin 30^\circ$
	$45\sin 30^\circ$ must be involved in res.	B1	$T \times (1.2 + 0.8\cos 30^\circ)$
	resolving parallel to the slope	M1	mom. about point of contact
	$F + T\cos 30^\circ = 45\sin 30^\circ$ aef	A1	$45 \times 0.8 \sin 30^\circ = T(1.2 + 0.8\cos 30^\circ)$
	$T = 9.51$	A1	
	$F = 14.3$	A1	<b>6</b> <b>16</b>
<b>or</b>	$T + F\cos 30^\circ = R\sin 30^\circ$	B1	res. horizontally
<b>(iii)</b>	$R\cos 30^\circ + F\sin 30^\circ = 45$	B1	res. vertically
	$\tan 30^\circ = (T + F\cos 30^\circ) / (45 - F\sin 30^\circ)$	M1	eliminating R

## 4729 Mechanics 2

1 (i)	$12 \times \cos 55^\circ$ $6.88 \text{ m s}^{-1}$	M1 A1 2	
(ii)	$12 \times \cos 55^\circ \times 0.65$ $(\pm) 4.47 \text{ m s}^{-1}$ ✓	M1 A1 2	✓ $0.65 \times \text{their (i)}$ 4
2	$F = 0.2 \text{ mg} \cos 30^\circ$  $0.2 \text{ mg} \cos 30^\circ \times d$ $\text{mg} \times d \times \sin 30^\circ$ $d = \frac{1}{2} \times 25 / (0.2 \times 9.8 \cos 30^\circ + 9.8 \times \sin 30^\circ)$ $1.89 \text{ m}$	M1 A1 B1 B1 M1 A1 6	= = $(1.6974 \text{ m}) (49\sqrt{3}/50 \text{ m})$ $a = 0.2g \cos 30^\circ + g \sin 30^\circ$ $a = (\pm) 6.60$ $0 = 5^2 - 2 \times 6.60d$ 6
3	direction of R perp. to wall R at $70^\circ$ to rod $0.8 \times 25 \cos 60^\circ = 1.6 \times R \sin 70^\circ$ $0.8 \times 25 \cos 60^\circ$ $1.6 \times R \sin 70^\circ$ R = 6.65 N	B1 B1 M1 A1 A1 A1 6	$10^\circ$ to horiz. moments about A 6
4 (i)	$45\,000/v = kv$ k = 50	M1 A1 2	AG
(ii)	$45\,000/20 - 50 \times 20 = 1200a$  $a = 1.04 \text{ m s}^{-2}$	M1 A1 A1 3	
(iii)	$P/15 = 50 \times 15 + 1200 \times 9.8 \sin 10^\circ$  41 900 W	M1 A1 A1 3	8
5 (i)	$2mu - 3kmu = -mu + kmv$  $v = \dots$ $v = 3u(1 - k)/k$  $(0 <) k < 1$	M1 M1 A1  A1 4	attempting to make v the subject  $3u/k - 3u$ not $\leq 1$
(ii)	$I = mu - - 2mu$ $3mu$	M1 A1 2	or $km(3u/k - 3u + 3u)$ + only
(iii)	$v = \pm 3u$ $e = (u/2 + 3u)/4u$ $e = 7/8$ or $0.875$	B1 M1 A1 3	9

<b>6 (i)(a)</b>	$T \cos 45^\circ = 2.94$ $T = 4.16 \text{ N}$	M1 A1 <b>2</b>	Resolving vertically <b>AG</b>
<b>(b)</b>	$T \cos 45^\circ + T = 0.3 \times 1.96 \omega^2$ (res. horiz.) $\omega = 3.47 \text{ rad s}^{-1}$	M1 A1 A1 <b>3</b>	calculates $v = 6.81$ (Max 2/3)
<b>(ii)(a)</b>	$T \cos 30^\circ + T \cos 60^\circ = 2.94$  $T = 2.15 \text{ N}$	M1 A1 A1 <b>3</b>	Resolving vertically
<b>(b)</b>	$T \cos 30^\circ + T \cos 60^\circ = 0.3v^2/1.5$ (res. horiz.) $v = 3.83 \text{ m s}^{-1}$	M1 A1 A1 <b>3</b>	calculates $\omega = 2.56$ (Max 2/3)
<b>11</b>			
<b>7 (i)</b>	$0 = (175 \sin \theta)^2 - 2 \times 9.8 \times 650$  $\theta = 40.2^\circ$	M1 A1 A1 <b>3</b>	
<b>(ii)</b>	Attempt at $t_1, t_2, t_{\text{top}}$ or $t_{\text{total}}$ 5.61, 23.65, 14.63, 29.26 $t_2 - t_1$ or $2(t_{\text{top}} - t_1)$ or $t_{\text{total}} - 2t_1$  time difference = 18.0	M1 A1 M1 A1  A1 <b>5</b>	$650 = 175 \sin 55^\circ \cdot t - 4.9t^2$ etc
<b>(iii)</b>	$v_h = 175 \cos 55^\circ$ (100.4) $v_v = 175 \sin 55^\circ - 9.8 \times 5.61$ speed = $\sqrt{(88.4^2 + 100.4^2)}$ $134 \text{ m s}^{-1}$	B1 M1 M1 A1 <b>4</b>	or KE $\frac{1}{2}mv^2$ (B1) PE $mx9.8 \times 650$ $v = \sqrt{(175^2 - 2 \times 9.8 \times 650)}$
<b>12</b>			
<b>8 (i)</b>	$(2 \times 4 \times \sin \Pi/2) / 3 \times \Pi/2$ 1.70	M1 A1 <b>2</b>	or $4r/3\Pi$ <b>AG</b>
<b>(ii)(a)</b>	$\bar{x} \times d(8 \times 20 - \Pi \times 4^2/2) = 10 \times 8 \times 20d - 12 \times \Pi \times 4^2/2 \times d$ $10 \times 8 \times 20(d)$ (1600) $(8 \times 20 - \Pi \times 4^2/2)(d)$ (134.9) $(12 \times \Pi \times 4^2/2)(d)$ (301.6) $\bar{x} = 9.63 \text{ cm}$	M1  A1 A1 A1 A1 <b>5</b>	or $134.9 \bar{x} = 64 \times 4 + 38.9 \times 12 + 32 \times 18$ (1298.8) $64 \times 4$ $38.9 \times 12$ $32 \times 18$ <b>AG</b>
<b>(ii)(b)</b>	$\bar{y} \times d(8 \times 20 - \Pi \times 4^2/2) = 4 \times 8 \times 20d - 1.7 \times \Pi \times 4^2/2 \times d$ $4 \times 8 \times 20(d)$ $1.7d \times \Pi \times 4^2/2$ (13.6\Pi) $\bar{y} = 4.43 \text{ cm}$	M1  A1 A1M1 A1 <b>4</b>	or $64 \times 4 = 42.7 + 38.9 \bar{y}$ $\bar{y} = 5.49$ $135 \bar{y} = 32 \times 4 + 38.9 \times 5.49 + 64 \times 4$
<b>(iii)</b>	$20 \cos 10^\circ \times T$ $15 \cos 10^\circ \times 9.63$ $15 \sin 10^\circ \times 4.43$ $20 \cos 10^\circ \cdot T = 15 \cos 10^\circ \times 9.63 - 15 \sin 10^\circ \times 4.43$ (needs 3 parts) $T = 6.64 \text{ N}$	B1 B1 B1 M1  A1 <b>5</b>	= or 10.6 (A to com) $34.7^\circ \angle \text{comAH}$ $= 15 \times 10.6 \times \cos 34.7^\circ$
<b>16</b>			

## 4729 Mechanics 2

<b>1</b>	$200\cos 35^\circ$ $200\cos 35^\circ \times d = 5000$ $d = 30.5 \text{ m}$	B1 M1 A1 <b>3</b>		<b>3</b>
<b>2</b>	$0.03R = \frac{1}{2} \times 0.009(250^2 - 150^2)$ $0.03R$	M1 B1	$150^2 = 250^2 + 2a \times 0.03$ $a = \pm 2 \times 10^6 / 3$ or $\pm 666,667$ (A1)	
	either K.E. $R = 6000 \text{ N}$	B1 A1 <b>4</b>	$F = 0.009a$ (M1) <b>4</b> unit errors	<b>4</b>
<b>3 (i)</b>	$D = 12000/20$ $12000/20 = k \times 20 + 600 \times 9.8 \times 0.1$ $k = 0.6$	B1 M1 A1 <b>3</b>	<b>AG</b>	
<b>(ii)</b>	$16000/v = 0.6v + 600 \times 9.8 \times 0.1$ $0.6v^2 + 588v - 16000 = 0$ $v = 26.5 \text{ m s}^{-1}$	M1 M1 A1 <b>3</b>	attempt to solve quad. (3 terms)	
<b>(iii)</b>	$16000/32 - 0.6 \times 32 = 600a$ $a = 0.801 \text{ m s}^{-2}$	M1 A1 A1 <b>3</b>	0.80 or 0.8	<b>9</b>
<b>4 (i)</b>	$0 = 35\sin\theta \times t - 4.9t^2$ $t = 35\sin\theta/4.9$ $50\sin\theta/7$ $R = 35\cos\theta \times t$ $aef$  $R = 35^2 \sin\theta \cdot \cos\theta / 4.9$  $R = 125\sin 2\theta$	M1 A1 B1  M1  A1 <b>5</b>	$R = u^2 \sin 2\theta / g$ only ok if proved or $70\sin\theta / g$ aef  their t  eliminate t	
<b>(ii)</b>	$110 = 125\sin 2\theta$ $\theta = 30.8^\circ$ or $59.2^\circ$ $t = 3.66 \text{ s}$ or $6.13 \text{ s}$	M1 A1+1 A1+1 <b>5</b>	<b>AG</b>	<b>10</b>
<b>5 (i)</b>	$3/8 \times 3$ (1.125) $0.53d = 5 \times 0.02 + (10 + 3/8 \times 3) \times 0.5$	B1 M1 A1	c.o.m. hemisphere $0.53e = 3 \times 5/8 \times 0.5 + 8 \times 0.02 + 13 \times .01$ $0.53f = 3 \times 3/8 \times 0.5 - 5 \times 0.02 - 10 \times 0.01$	
<b>(ii)</b>	$d = 10.7$ Attempt to calc a pair relevant to P,G $OP = 0.9$ (pair), $p = 73.3^\circ$ $q = 16.7^\circ$ $r = 76.9^\circ$ $(77.2^\circ)$ , $s = 13.1^\circ$ (12.8°) $AC = 0.86$ , $BC = 0.67$ , $AD = 10.4$ $BD = 10.2$ $r > p$ , $s < q$ , $p + s < 90$ , $0.67 < 0.86$ , $10.2 < 10.4$ it is in equilibrium	A1 <b>4</b> M1 A1  M1 A1 <b>4</b>	<b>AG</b> ( $e = 2.316$ $f = 0.684$ ) distance / angle not a complimentary pair  make relevant comparison $0.7 < 0.9$ ( $OG < OP$ ) $10.7 < 10.9$	<b>8</b>



<p><b>6 (i)</b></p> <p><math>T\cos 60^\circ = S\cos 60^\circ + 4.9</math></p> <p><math>T\sin 60^\circ + S\sin 60^\circ = 0.5 \times 3^2/0.4</math></p> <p><math>(S + 9.8)\sin 60^\circ + S\sin 60^\circ = 45/4</math></p> <p><math>S = 1.60 \text{ N}</math></p> <p><math>T = 11.4 \text{ N}</math></p>	<p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>A1</p> <p><b>7</b></p>	<p>Resolving vertically nb for M1: (must be components – all 4 cases) Res. Horiz. <math>m\omega^2</math> ok if <math>\omega \neq 3</math> If equal tensions <math>2T=45/4</math> M1 only</p>
<p><b>(ii)</b></p> <p><math>T\cos 60^\circ = 4.9</math></p> <p><math>T = 9.8</math></p> <p><math>T\sin 60^\circ = 0.5 \times 0.4\omega^2</math></p> <p><math>\omega = 6.51 \text{ rad s}^{-1}</math></p>	<p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>A1</p> <p>A1</p> <p><b>5</b></p>	<p>Resolving vertically (component)</p> <p>Resolving horiz. (component)</p> <p>or 6.5</p> <p><b>12</b></p>
<p><b>7 (i)</b></p> <p><math>u = 3 \text{ m s}^{-1}</math></p> <p><math>6 = 2x + 3y</math></p> <p><math>e = (y - x) / 3</math></p>	<p>B1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>A1</p> <p><b>6</b></p> <p>B1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p><b>7</b></p>	<p>(<math>e = 2/3</math>) (equus must be consistent)</p> <p><b>AG</b></p> <p>or (B1) <math>\frac{1}{2}mx^2</math></p> <p>(B1) <math>\frac{1}{2}m xv^2</math></p> <p>(B1) <math>mx \cdot 9.8x4</math></p> <p><math>v = \sqrt{(2^2 + 2 \times 9.8x4)}</math></p> <p>or <math>\cos^{-1}(2/9.08)</math></p> <p>12.7° to vertical</p> <p><b>13</b></p>
<p><b>8 (i)</b></p> <p>com of <math>\Delta</math> 3 cm right of C</p> <p><math>(48+27)\bar{x} = 48 \times 4 + 27 \times 11</math></p> <p><math>\bar{x} = 6.52</math></p> <p>com of <math>\Delta</math> 2 cm above AD</p> <p><math>(48+27)\bar{y} = 48 \times 3 + 27 \times 2</math></p> <p><math>\bar{y} = 2.64</math></p>	<p>B1</p> <p>M1</p> <p>A1</p> <p>A1</p> <p>B1</p> <p>M1</p> <p>A1</p> <p>A1</p> <p><b>8</b></p> <p>B1</p> <p>B1</p> <p>B1</p> <p>M1</p> <p>A1</p> <p><b>5</b></p>	<p>can be implied e.g. <math>7/\sin 30^\circ \cdot F</math></p> <p>7.034 (AG) or <math>(6.52 - 2.64 \tan 30^\circ)</math></p> <p>52.0° (GAH) or <math>(\text{above})x \cos 30^\circ</math></p> <p><math>(5.00)x \cos 30^\circ</math> (4.33)</p> <p><math>14F = 3 \times 9.8 \times 7.034 \times \cos 52.0^\circ</math></p> <p><b>13</b></p>
<p><b>(ii)</b></p> <p>14F</p> <p><math>3g \cos 30^\circ \times 6.52</math></p> <p><math>3g \sin 30^\circ \times 2.64</math></p> <p><math>14F = 3g \cos 30^\circ \times 6.52 - 3g \sin 30^\circ \times 2.64</math></p> <p><math>F = 9.09 \text{ N}</math></p>		

## 4729 Mechanics 2

1	$(20 \sin \theta)^2 = 2 \times 9.8 \times 17$	M1	or B2 for $\max ht = v^2 \sin^2 \theta / 2g$
		A1	
	$\sin \theta = \sqrt{(2 \times 9.8 \times 17) \div 20}$	M1	subst. values in above
	$\theta = 65.9^\circ$	A1 4	4

2	$\bar{x} = 8$	B1	
	$T \sin 30^\circ \times 12 = 8 \times 2 \times 9.8$	M1	ok if g omitted
		A1 ft	ft their $\bar{x}$
	$T = 26.1$	A1 4	4

3 (i)	$140 \times X = 40 \times 70$	M1	
	$X = 20 \text{ N}$	A1	
	at $F$ 20 N to the right	B1	inspect diagram
	at $G$ 20 N to the left	B1 4	SR B1 for correct directions only
(ii)	$\bar{d} = (2 \times 40 \sin \Pi / 2) \div 3 \Pi / 2$	M1	must be radians
		A1	
	$\bar{d} = 17.0$	A1	16.98 160/3\Pi (8/15\Pi m)
	$70 \bar{y} = 100 \times 60 + 217 \times 10$	M1	
		A1 ft	ft 200 + their $\bar{d}$ or 2 + their $\bar{d}$ (m)
	$\bar{y} = 117$	A1 6	116.7 10

4 (i)	$P/10 - 800 \times 9.8 \sin 12^\circ - 100k = 800 \times 0.25$	M1	$P/10 = D_1$ ok
		A1	$D_1$ ok
	$P/20 - 400k = 800 \times 0.75$	M1	$P/20 = D_2$ ok
		A1	$D_1 = 2D_2$ needed for this A1
	solving above	M1	
	$k = 0.900$	A1	AG 0.9000395
	$P = 19\,200$	A1 7	or 19.2 kW (maybe in part (ii))
(ii)	$0.9 v^2 = 28\,800/v$	M1	ok if $19200/v$
	solving above	M1 *	$(v^3 = 32\,000)$
	$v = 31.7 \text{ m s}^{-1}$	A1 3	10

5 (i)	$0.8 S$	B1	vert comp of $S$
	$0.6 T$	B1	vert comp of $T$
	$S \cos \alpha = T \cos \beta + 0.2 \times 9.8$	M1	
	$0.8 S = 0.6 T + 1.96$ aef	A1 4	AG $4S = 3T + 9.8$
(ii)	$0.6 S$	B1	
	$0.8 T$	B1	
	$0.2 \times 0.24 \times 8^2$	B1	3.072 384/125
	$S \sin \alpha + T \sin \beta = 0.2 \times 0.24 \times 8^2$	M1	must be $m r \omega^2$
	$6S + 8T = 30.72$	A1	aef
	eliminate $S$ or $T$	M1	
	$S = 3.4 \text{ N}$	A1	3.411
	$T = 1.3 \text{ N}$	A1 8	1.282 12

<b>6 (i)</b>	$x = v \cos \theta t$	B1	
	$y = v \sin \theta t - \frac{1}{2} x 9.8 t^2$	B1	or g
	substitute $t = x/v \cos \theta$	M1	
	$y = x \tan \theta - 4.9 x^2 / v^2 \cos^2 \theta$	A1 <b>4</b>	<b>AG</b>
<b>(ii)</b>	Sub $y = -h$ , $x = h$ , $v = 14$ , $\theta = 30$	M1	signs must be correct
	$-h = h/\sqrt{3} - h^2/30$	A1	aef
	solving above	M1	
	$h = 47.3$	A1 <b>4</b>	
<b>(iii)</b>	$v_v^2 = (14 \sin 30^\circ)^2 - 2 \times 9.8 x (-47.3)$ (double negative needed) ft their -47.3	M1	$14 \cos 30^\circ t = 47.3$ ft & $v_v = 14 \sin 30^\circ - 9.8t$
	$v_v = \pm 31.2$	A1	$t = 3.90$ (or $dy/dx = 1/\sqrt{3} - x/15$ etc ft)
	$\tan^{-1}(31.2/14 \cos 30^\circ)$	A1	$v_v = \pm 31.2$ ( $\tan \alpha = 1/\sqrt{3} - 47.3/15$ )
	$\alpha = 68.8^\circ$ below horiz/21.2° to d'vert.	M1	$\tan^{-1}(31.2/14 \cos 30^\circ)$
<b>(iv)</b>	$\frac{1}{2} m x 14^2 + m x 9.8 x 47.3 = \frac{1}{2} m v^2$	A1 <b>5</b>	68.8°/.....
	$v = 33.5$	M1	ft ( $12.1^2 + 31.2^2$ )
		A1 <b>2</b>	33.5 <b>15</b>

<b>7 (i)</b>	$p = 4 \text{ m s}^{-1}$	B1	P's first speed
	$0.8 = 0.2p_1 + 0.3q_1$	M1	
		A1	
	$0.5 = (q_1 - p_1)/4$	M1	
		A1	
	solving above	M1	
	$q_1 = 2.4 \quad 12/5$	A1	Q's first speed
	$p_1 = 0.4 \quad 2/5$	A1 <b>8</b>	may be in (ii). <b>SR 1</b> for both negative
<b>(ii)</b>	$0.8 = 0.2p_2 + 0.3q_2$	M1	
		A1	
	$0.5 = (p_2 - q_2)/2$	M1	
		A1	
	solving above	M1	
	$p_2 = 2.2 \quad 11/5$	A1	
	$q_2 = 1.2 \quad 6/5$	A1 <b>7</b>	
<b>(iii)</b>	$R = 0.3 \times 1.2^2 / 0.4$	M1	
	$R = 1.08 \text{ N}$	A1 <b>2</b>	<b>17</b>

## 4729 Mechanics 2

<b>1 (i)</b>	$\frac{1}{2} \times 75 \times 12^2$ or $\frac{1}{2} \times 75 \times 3^2$ (either KE) $75 \times 9.8 \times 40$ (PE) $R \times 180$ (change in energy = 24337) $\frac{1}{2} \times 75 \times 12^2 = \frac{1}{2} \times 75 \times 3^2 + 75 \times 9.8 \times 40 - R \times 180$ $R = 135 \text{ N}$	B1 B1 B1 M1 A1	M1 $12^2 = 3^2 + 2a \times 180$ A1 $a = 0.375$ (3/8) M1 $75 \times 9.8 \times \sin\theta - R = 75a$ A1 $R = 135$ (max 4 for no energy)	<b>5</b>
<b>2 (i)</b>	$R = F = P/v = 44\,000/v = 1400$ $v = 31.4 \text{ m s}^{-1}$	M1 A1		<b>2</b>
<b>(ii)</b>	$44\,000/v = 1400 + 1100 \times 9.8 \times 0.05$ $v = 22.7 \text{ m s}^{-1}$	M1 A1 A1	must have g	<b>3</b>
<b>(iii)</b>	$22\,000/10 + 1100 \times 9.8 \times 0.05 - 1400$ $= 1100a$ $a = 1.22 \text{ m s}^{-2}$	M1 A1 A1		<b>3</b>
<b>3 (i)</b>	$\cos\theta = 5/13$ or $\sin\theta = 12/13$ or $\theta = 67.4^\circ$ $0.5 \times F \sin\theta = 70 \times 1.4 + 50 \times 2.8$ $F = 516 \text{ N}$	B1 M1 A1 A1	any one of these moments about A (ok without 70) $0.5 \sin\theta = 0.4615$ <b>SR 1 for 303 (omission of beam)</b>	<b>4</b>
<b>(ii)</b>	$F \sin\theta = 120 + Y$ (resolving vertically) $Y = 356$ ✓ their $F \times 12/13 - 120$ $X = F \cos\theta$ (resolving horizontally) $X = 198$ ✓ their $F \times 5/13$ Force = $\sqrt{(356^2 + 198^2)}$ 407 or 408 N	M1 A1 ✓ M1 A1 ✓ M1 A1	M1/A1 for moments (B) $Y \times 2.8 + 1.4 \times 70 = 2.3 \times 516$ ✓ $\times 12/13$ (C) $0.5 \times Y = 0.9 \times 70 + 2.3 \times 50$ (D) $1.2X = 1.4 \times 70 + 2.8 \times 50$	<b>6</b>
<b>4 (i)</b>	$T = 0.4 \times 0.6 \times 2^2$ $T = 0.96 \text{ N}$	M1 A1		<b>2</b>
<b>(ii)</b>	$S - T$ $S - T = 0.1 \times 0.3 \times 2^2$ $S = 1.08$	B1 M1 A1 A1	may be implied	<b>4</b>
<b>(iii)</b>	$v = r\omega$ $v_P = 0.6$ $v_B = 1.2$ $\frac{1}{2} \times 0.1 \times 0.6^2 + \frac{1}{2} \times 0.4 \times 1.2^2$ 0.306	M1 A1 A1 M1 A1	(0.018 + 0.288) separate speeds	<b>5</b>

<b>5 (i)</b>	$\bar{d} = (2 \times 6 \sin \pi/4) / 3\pi/4$ $\bar{d} = 3.60$	M1 A1 2	must be correct formula with rads AG
<b>(ii)</b>	$\bar{d} \cos 45^\circ = "2.55"$ $5 \bar{x} = 3 \times 3 + 2 \times "2.55"$ $\bar{x} = 2.82$ $5 \bar{y} = 3 \times 6 + 2 \times (12 + "2.55")$ $\bar{y} = 9.42$	B1  M1 A1 A1 M1 A1 A1 7	may be implied moments must not have areas  2kg/3kg misread (swap) gives (2.73, 11.13) $\theta = 21.7^\circ$ (MR - 2) (max 7 for (ii) + (iii)) SR -1 for $\bar{x}$ , $\bar{y}$ swap
<b>(iii)</b>	$\tan \theta = 2.82/8.58$ $\theta = 18.2^\circ$ ✓	M1 A1 2	M0 for their $\bar{x} / \bar{y}$ ✓ their $\bar{x} / (18 - \bar{y})$ <b>11</b>
<b>6 (i)</b>	$I = 0.9 = 6 \times 0.2 - v \times 0.2$ $v = 1.5$	M1 A1 A1 3	needs to be mass 0.2
<b>(ii)</b>	$0.6 = (c - b) / 6$ $6 \times 0.2 = 0.2b + 0.1c$  $b = 2.8$ $0.4 \times 5 + 0.2 \times 1.5 = 0.4a + 0.2 \times 6$ or $I = 0.9 = -0.4a - 0.4 \times 5$ $a = 2.75$ $2.75 < 2.8$ no further collision	M1 A1 M1 A1 A1 M1 A1 M1 A1 10	restitution (allow 1.5 for M1)  momentum (allow 1.5 for M1)  1st collision (needs their 1.5 for M1)  compare v's of A and B (calculated) <b>13</b>
<b>7(i)</b>	$9 = 17 \cos 25^\circ \times t$ $t = 0.584$ (or $9/17 \cos 25^\circ$ ) $d = 17 \sin 25^\circ \times 0.584 + \frac{1}{2} \times 9.8 \times 0.584^2$ (d = ht lost (5.87)) $h = 2.13$	M1 A1 M1 A1 A1 5	B1 $y = x \tan \theta - 4.9x^2/v^2 \cos^2 \theta$ M1/A1 $y = 9 \tan(-25^\circ) - 4.9 \times 9^2 / 17^2 \cos^2 25^\circ$  A1 $y = -5.87$ 2.13
<b>(ii)</b>	$v_h = 17 \cos 25^\circ$ (15.4) $v_v = 17 \sin 25^\circ + 9.8 \times 0.584$ or $v_v^2 = (17 \sin 25^\circ)^2 + 2 \times 9.8 \times 5.87$ $v_v = 12.9$ $\tan \theta = 12.9/15.4$ $\theta = 40.0^\circ$ below horizontal	B1 M1  A1 M1 A1 5	M1/A1 $dy/dx = \tan \theta - 9.8x/v^2 \cos^2 \theta$  A1 $dy/dx = -0.838$ M1 $\tan^{-1}(-.838)$ or $50.0^\circ$ to vertical
<b>(iii)</b>	speed = $\sqrt{(12.9^2 + 15.4^2)}$  $\frac{1}{2}mv^2 = \frac{1}{2}m \times 20.1^2 \times 0.7$ $v = 16.8 \text{ m s}^{-1}$	M1 A1 ✓ M1 A1 4	(20.1)  NB 0.3 instead of 0.7 gives 11.0 (M0) <b>14</b>

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<b>1</b>	$75 \times 9.8 \times 40$ $(75 \times 9.8 \times 40) \div 120$ 245 W	B1 M1 A1 [3]	Average Speed = $40 \div 120$ $(75 \times 9.8) \times (\text{Average speed})$	<b>3</b>
<b>2 (i)</b>	$v^2 = 2 \times 9.8 \times 3$ or $2 \times 9.8 \times 1.8$ $v_1 = \sqrt{6g}$ or $\sqrt{58.8}$ or $\frac{7}{5}\sqrt{30}$ or 7.67 $v_2 = \sqrt{3.6g}$ or $\sqrt{35.28}$ or $\frac{21}{5}\sqrt{2}$ or 5.94 $I = \pm 0.2(5.94 + 7.67)$ 2.72	M1 A1 A1 M1 A1ft [5]	Kinematics or energy Speed of impact ( $\pm$ ) Speed of rebound ( $\pm$ ) +ve, ft on $v_1$ and $v_2$	
<b>(ii)</b>	$e = 5.94/7.67$ $0.775$ or $\frac{\sqrt{15}}{5}$	M1 A1ft [2]	Allow 0.774, ft on $v_1$ and $v_2$	<b>7</b>
<b>3 (i)</b>	$\bar{u} = 0.2$ (from vertex) or 0.8 or 0.1 $0.5\bar{d} = 0.2 \times \bar{u} + 0.3 \times 0.65$ $\bar{d} = 0.47$	B1 M1 A1 A1 [4]	com of conical shell <b>AG</b>	
<b>(ii)</b>	$s = 0.5$ $T \sin 80^\circ \times 0.5 = 0.47 \times 0.5 \times 9.8$ $T = 4.68 \text{ N}$	B1 M1 A1 A1 [4]	slant height, may be implied	<b>8</b>
<b>4 (i)</b>	$D - 400 = 700 \times 0.5$ $D = 750 \text{ N}$	M1 A1 [2]	3 terms	
<b>(ii)</b>	$P = 750 \times 12$ 9 000 W or 9 kW	M1 A1ft [2]		
<b>(iii)</b>	$P/35 = 400$ 14 000 W or 14 kW	M1 A1 [2]		
<b>(iv)</b>	$D = 14000/12$ $3500/3 = 400 + 700 \times 9.8 \sin \theta$ $\theta = 6.42^\circ$	B1ft M1 A1 A1 [4]	May be implied 3 terms Their P/12	<b>10</b>

5	$16 - 12 = 2x + 3y$ $4 = 2x + 3y$ $\frac{1}{2} \cdot 2(8)^2 + \frac{1}{2} \cdot 3(4)^2$ or $\frac{1}{2} \cdot 2x^2 + \frac{1}{2} \cdot 3y^2$ or $\pm \frac{1}{2} \cdot 2(8^2 - x^2)$ or $\pm \frac{1}{2} \cdot 3(4^2 - y^2)$ $\frac{1}{2} \cdot 2(8)^2 + \frac{1}{2} \cdot 3(4)^2 - \frac{1}{2} \cdot 2x^2 - \frac{1}{2} \cdot 3y^2 = 81$ $2x^2 + 3y^2 = 14$ Attempt to eliminate x or y from a linear and a quadratic equation $15y^2 - 24y - 12 = 0$ or $10x^2 - 16x - 26 = 0$ Attempt to solve a three term quadratic $x = -1$ (or $x = 2.6$ ) $y = 2$ (or $y = -2/5$ ) $x = -1$ and $y = 2$ only speeds 1, 2 away from each other	M1 A1 B1 M1 A1 M1 A1 A1 A1 A1 A1 <b>[12]</b>	aef  aef  aef  <b>12</b>
6 (i)	$30^2 = V_1^2 \sin^2 \theta_1 - 2 \times 9.8 \times 250$ $V_1^2 \sin^2 \theta_1 = 5800$ AEF $V_1 \cos \theta_1 = 40$ $V_1 = 86.0$ $\theta_1 = 62.3^\circ$	M1 A1 B1 A1 A1 <b>[5]</b>	$\frac{1}{2} m V_1^2 = \frac{1}{2} m 50^2 + m \times 9.8 \times 250$  <b>AG</b> <b>AG</b>
(ii)	$0 = \sqrt{5800} t_p - 4.9 t_p^2$ $t_p = 15.5$  $-\sqrt{5800} = 30 - 9.8 t_q$  $t_q = 10.8$	M1 A1  M1  A1 <b>[4]</b>	$30 = V_1 \sin \theta_1 - 9.8 t$  $t = 4.71$
(iii)	$R = 40 \times 15.5$ $R = 621$ $V_2 \cos \theta_2 \times 10.8 = 621$ $0 = V_2 \sin \theta_2 \times 10.8 - 4.9 \times 10.8^2$ $V_2 \sin \theta_2 = 53.1$ or $53.0$ Method to find a value of $V_2$ or $\theta_2$ $\theta_2 = 42.8^\circ$ $V_2 = 78.2 \text{ m s}^{-1}$ or $78.1 \text{ m s}^{-1}$	M1 A1 B1 M1 A1 M1 A1 A1 <b>[8]</b>	(620, 622) $V_2 \cos \theta_2 = 57.4$  (52.9, 53.1)  $42.6^\circ$ to $42.9^\circ$ or $78.1^\circ$  <b>17</b>
7 (i)	$\cos \theta = 3/5$ or $\sin \theta = 4/5$ or $\tan \theta = 4/3$ or $\theta = 53.1^\circ$ $R \cos \theta = 0.2 \times 9.8$ $R = 3.27 \text{ N}$ or $49/15$	B1  M1 A1 <b>[3]</b>	$\theta = \text{angle to vertical}$
(ii)	$r = 4$ $R \sin \theta = 0.2 \times 4 \times \omega^2$  $\omega = 1.81 \text{ rad s}^{-1}$	B1 M1 A1 A1 <b>[4]</b>	

(iii)	$\varphi = 26.6^\circ$ or $\sin \varphi = \frac{1}{\sqrt{5}}$ or $\cos \varphi = \frac{2}{\sqrt{5}}$ or $\tan \varphi = 0.5$ $T = 0.98$ or $0.1g$ $N \cos \theta = T \sin \varphi + 0.2 \times 9.8$ $N \times 3/5 = 0.438 + 1.96$ $N = 4.00$ $N \sin \theta + T \cos \varphi = 0.2 \times 4 \times \omega^2$ $4 \times 4/5 + 0.98 \cos 26.6^\circ = 0.8 \omega^2$ $\omega = 2.26 \text{ rad s}^{-1}$	B1  B1 M1 A1 A1 M1 A1 A1 [8]	$\varphi = \text{angle to horizontal}$  Vertically, 3 terms may be implied Horizontally, 3 terms  <b>15</b>
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<b>1</b>	$v^2 = 2 \times 9.8 \times 10$ $v = 14 \text{ m s}^{-1}$ speed = $\sqrt{7^2 + 14^2}$ 15.7 or $7\sqrt{5} \text{ m s}^{-1}$ $\tan^{-1}(14/7)$ or $\tan^{-1}(7/14)$ 63.4° to the horizontal	M1 A1 M1 A1 M1 A1 <b>6</b>	Using $v^2 = u^2 + 2as$ with $u = 0$  Method to find speed using their “v”  Method to find angle using their “v” 26.6° to vertical <b>6</b>
<b>2 (i)</b>	$(6\sin \Pi/2) \div (\Pi/2)$ 3.82	M1 A1 <b>2</b>	Use of correct formula <b>AG</b>
	<b>(ii)</b>	M1 A1 A1 M1 A1 <b>5</b>	Method to find centre of mass  Attempt to find the required angle <b>7</b>
<b>3 (i)</b>	$D = 128\,000/80 (= 1600)$ $k(80)^2 = 128\,000/80$  $k = 1/4$ $R = 900 \text{ N}$	B1 M1 A1 A1 B1 <b>5</b>	Driving force = resistance  FT on their k ( $R = 3600k$ )
	<b>(ii)</b>	B1 B1 M1 A1 <b>4</b>	4 terms required <b>9</b>
<b>4 (i)</b>	$4T\cos 20^\circ = 5 \times g \times 2.5$  $T = 32.6 \text{ N}$	M1 A1 A1 <b>3</b>	Using moments; allow sin/cos mix Allow with omission of g
	<b>(ii)</b>	M1 A1 M1 A1 M1 A1 A1 A1 <b>7</b>	allow sin/cos mix FT their T  FT their T, but not from omission of g $X \neq 0, Y \neq 0$  or 31.2° to left of vertical <b>10</b>

5 (i)	$T\cos 45^\circ + R\sin 45^\circ = mg$ $T\sin 45^\circ - R\cos 45^\circ = m\sin 45^\circ \omega^2$ $2T = \sqrt{2}mg + ml\omega^2$ $T = m/2(\sqrt{2}g + l\omega^2)$	*M1 A1 *M1 A1 Dep*M1 A1 6	3 terms 3 terms; $a = r\omega^2$ Method to eliminate R <b>AG</b> www
5 (ii)	$R = 0$ $2R = \sqrt{2}mg - ml\omega^2$ or $T\cos 45^\circ = mg$ or $T = ml\omega^2$ Solve to find $\omega$ $\omega = 4.16 \text{ rad s}^{-1}$	B1 B1  M1  A1 4	may be implied    <b>10</b>
6 (i)	$2mu = 2mv + 3mv$ $v = 2/5 u$	M1 A1 A1 3	Conservation of momentum Must be $v =$
6 (ii)	$e = (3v - v) / u$ $e = 4/5$	M1 A1 2	Using restitution <b>AG</b>
6 (iii)	Initial K.E. = $9mv^2 / 2 = 18mu^2 / 25$ Final K.E. = $9mv^2 / 8 = 9mu^2 / 50$ $\frac{1}{2} m (V)^2 = \text{Final K.E.}$ $V = 3u / 5$	B1 FT B1 FT M1 A1 4	FT on their $v$ from (i) FT on their $v$ from (i)  <b>AG</b>
6 (iv)	$4mu / 5 - 3mu / 5 = 2mx + my$ $u / 5 = 2x + y$ $e = 4/5 = (y - x) / u$ $4u = 5y - 5x$ solving 2 relevant equations $x = -u/5$ $y = 3u/5$ $y = 3u/5$ away from wall (x) + towards wall (y)	M1 A1 FT M1 FT A1 M1 A1 A1 A1 8	Conservation of momentum FT on their $v$ from (i); aef Using restitution FT on their $v$ from (i); aef  both <b>17</b>

<p><b>7 (i)</b></p> <p><b>Or</b> last 4 marks of (i)</p>	<p><math>R = 0.2 \times 9.8 \times \cos 30^\circ (= 1.70)</math>  <math>F = 0.1 \times 9.8 \times \cos 30^\circ (= 0.849)</math> FT</p> <p><math>\frac{1}{2} \times 0.2 \times 11^2 - \frac{1}{2} \times 0.2 v^2 =</math>  <math>0.2 \times 9.8 \times 5 \sin 30 + 5 \times 0.849</math>  <math>v = 5.44 \text{ m s}^{-1}</math></p> <p><math>F + 0.2g \sin 30 = \pm 0.2a</math>  <math>a = \pm 9.1</math>  <math>v^2 = 11^2 + 2 \times a \times 5</math>  <math>v = 5.44 \text{ m s}^{-1}</math></p>	<p>B1 B1 M1 A1 A1 A1 <b>6</b></p> <p>M1 A1 M1 A1</p>	<p>FT on their R, but not <math>R = 0.2g</math> Use of conservation of energy</p> <p><b>AG</b></p> <p>Use of N2L, 3 terms</p> <p>Complete method to find v</p>
<p><b>(ii)</b></p> <p><b>Or</b> first 5 marks of (ii)</p>	<p><math>t = 5 \cos 30^\circ / 5.44 \cos 30^\circ</math>  <math>t = 0.919 \text{ s}</math>  <math>u = 5.44 \sin 30^\circ (= 2.72)</math>  <math>s = 2.72 \times 0.919 - 4.9 \times 0.919^2</math>  <math>s = -1.6</math> (or better)            Ht drop to C = <math>5 \sin 30^\circ = 2.5 \text{ m}</math>            Ball does not hit the roof</p> <p><math>y = x \tan \theta - gx^2 \sec^2 \theta / 2V^2</math>            substitute values  <math>V = 5.44 \quad \theta = 30^\circ \quad x = 5 \cos 30^\circ</math>  <math>y = 2.5 - 9.8 \times 25 \times 3 / 4 \times 4 / 3 / (2 \times 5.44^2)</math>  <math>y = -1.6</math> (or better)</p>	<p>M1 A1 B1 M1 A1 B1 A1 <b>7</b></p> <p>B1 M1 A1 A1</p>	<p>time to lateral position over C</p> <p>Ht dropped</p> <p><b>13</b></p> <p>all 3 correct</p>
<p><b>OR (ii)</b></p>	<p><math>u = 5.44 \sin 30^\circ (= 2.72)</math>  <math>-2.5 = 5.44 \sin 30 t - 4.9 t^2</math></p> <p><math>t = 1.04</math>  <math>x = 5.44 \cos 30 \times 1.04 = 4.9</math> (or better)            Horizontal distance from B to C =  <math>5 \cos 30 = 4.3</math> (or better)            Ball does not hit the roof</p>	<p>B1 M1 A1 A1 A1</p> <p>B1 A1 <b>7</b></p>	<p>aef time to position level with AC</p>
<p><b>OR (ii)</b></p>	<p><math>y = x \tan \theta - gx^2 \sec^2 \theta / 2V^2</math>            substitute values  <math>-2.5 = 0.577x - 0.221x^2</math>            Attempt to solve quadratic for x  <math>x = 4.9</math> (or better)            Horizontal distance from B to C =  <math>5 \cos 30 = 4.3</math> (or better)            Ball does not hit the roof</p>	<p>B1 M1 A1 M1 A1</p> <p>B1 A1 <b>7</b></p>	<p>aef</p>
<p><b>OR (ii)</b></p>	<p><math>u = 5.44 \sin 30^\circ = 2.72</math>  <math>-2.5 = 5.44 \sin 30 t - 4.9 t^2</math></p> <p><math>t = 1.0</math> (or better)  <math>T = 5 \cos 30^\circ / 5.44 \cos 30^\circ</math>  <math>T = 0.92</math> (or better)            Ball does not hit the roof</p>	<p>B1 M1 A1 A1 M1 A1 A1 <b>7</b></p>	<p>aef time to position level with AC time to lateral position over C</p>

<b>OR (ii)</b>	Attempt at equation of trajectory $y = 0.577x - 0.221x^2$ $y = -0.577x$ Solving their quadratic and linear equations to get at least x or y $x = 5.2$ (or better) or $y = -3.0$ (or better) Horizontal distance from B to C = $5\cos 30 = 4.3$ (or better) Or Ht drop to C = $5\sin 30^\circ = 2.5$ Ball does not hit the roof	M1 A1 B1  M1 A1  B1 A1 <b>7</b>	Equation of BC     Must be the one needed for comparison
<b>OR (ii)</b>	Attempt at equation of trajectory $y = 0.577x - 0.221x^2$ $y = -0.577x$ Solving their quadratic and linear equations $x = 5.2$ (or better) and $y = -3.0$ (or better) Distance = 6.0 (or better)  Ball does not hit the roof	M1 A1 B1  M1 A1  B1 A1 <b>7</b>	Distance from B to point of intersection

Question		Expected Answer	Mark	Rationale/Additional Guidance
1	(i)	$3x_G = 2 \times 0.3 + 1 \times 0.6$ OR $3x_G = 2 \times 0.3 + 0$ OR $3x_G = 4 \times 0.3$ OR $3y_G = 1 \times 0.3 + 1 \times 0.6 + 0$ OR $3y_G = 4 \times 0.3 - 1 \times 0.3$ $x_G = 0.4$ (from AD) OR $x_G = 0.2$ (from BC) $y_G = 0.3\text{m}$ from AB or CD $AG^2 = 0.4^2 + 0.3^2$ $AG = 0.5\text{ m}$	M1 A1 A1 M1 A1 <b>[5]</b>	Table of moments idea. M0 for reducing to 1D problem. Masses/weights may be included.  Pythagoras with 2 appropriate distances. This may only be seen in (ii), allow M1A1 in this case.
	(ii)	$v = 0.5 \times 3$ $v = 1.5\text{ ms}^{-1}$	M1 A1 <b>[2]</b>	Allow use of candidate's 0.2, 0.4, 0.3, 0.5
2	(i)	$(k25^{3/2}) \times 25 = 15000$ $k = 4.8$ <p style="text-align: center;"><b>AG</b></p>	M1 A1 A1 <b>[3]</b>	Tractive force x speed = power
	(ii)	$R = 4.8 \times 16^{3/2}$  $T - 4.8 \times 16^{3/2} + 700g \times 1/15 = 700 \times 0.3$ $P = 59.9 \times 16$ $P = 958\text{ W}$	B1 M1 A1 M1 A1 <b>[5]</b>	307.2 N2L, 4 terms to find tractive force (T) Allow cv(R), R not 600; (T = 59.866..) 16xTractive force

3	(i)	$T_A \cos 30 + T_B \cos 60 = 0.4g$ $2T \cos 30 + T \cos 60 = 0.4g$ $T_B = 1.76 \text{ N}$ $T_A = 3.51 \text{ N}$	M1 A1 A1 A1 <b>[4]</b>	Resolves vertically, 3 terms $T = 1.756$ . Watch for MR of $T \cos 30 + 2T \cos 60 = 0.4g$  Accept 3.52
	(ii)	$r = 0.5 \sin 30 (= 0.25)$  $3.51 \sin 30 + 1.76 \sin 60 = 0.4 \omega^2 0.5 \sin 30$ $\omega = 5.72 \text{ rad s}^{-1}$	B1 M1 A1ft A1 <b>[4]</b>	N2L radial, 3 terms cv(1.76, 3.51, 0.25) Accept 5.73
4	(i)	$WD = 100 \cos 20 \times 30$  $WD = 2820 \text{ J}$	M1  A1 <b>[2]</b>	Product of 3 relevant elements. Angle could be 5, 25 or complements 2819.1...
	(ii)	$PE = 25g \times 30 \sin 5$ $PE = 641$	M1 A1 <b>[2]</b>	Product of weight and vertical height. Allow without g 640.6
	(iii)	<b>OR</b> $2819.1 = 640.6$ $+ 30 \times 70 + 25v^2/2$ $v = 2.51 \text{ ms}^{-1}$  $25a = 100 \cos 20 - 70 - 25g \sin 5$ $a = 0.105$ $v^2 = 2 \times 30 \times 'a'$ $v = 2.51$	M1 A1ft A1 A1 <b>[4]</b> *M1 A1 dep*M1 A1 <b>[4]</b>	4 term energy equation ft(cv 2820 and cv 641)  cao  4 term equation Allow 0.1 here Or equivalent complete method cao

5	(i)		$x_H = 3 \times 0.6 / 8$ $\pi(0.6^2 \times 0.6)(0.6/2) - (0.6^3 \times 2\pi/3)0.225$ $= \pi \times 0.6^3(1+2/3)x_G$ $x_G = 0.09 \text{ m}$	B1 M1 A1 A1 A1 <b>[5]</b>	CoM hemisphere ( $x_H = 0.225$ ), may be implied Use of table of moments idea SC Volume of sphere used, max B1M1A1, moment equation fully correct for A1 (3/5) Accept -0.09
	(ii)	(a)	$mg(0.09\cos 45) =$ $2(0.6+0.6\cos 45+0.6\sin 45)$ $m = 4.65\text{kg}$	M1 A1 A1 A1 <b>[4]</b>	Attempt at moments (must resolve), allow without g $2(0.6+\sqrt{[0.6^2+0.6^2]})$ (4.6451...)
	(ii)	(b)	$2/4.6451g$ $\mu \geq 0.0439$	M1 A1 A1 <b>[3]</b>	Ratio force/weight cv(4.65) Correct inequality sign, accept 0.044
6	(i)		$0 = (14\sin 30)^2 - 2gh$ $h = 2.5 \text{ m}$	M1 A1 <b>[2]</b>	$h = (14\sin 30)x1/1.4 - g(1/1.4)^2/2$ or use $(u^2\sin^2\theta)/2g$
	(ii)		$0.4 \times 15 = 0.4(14\cos 30) + I$ $I = 1.15$	M1 A1 A1 <b>[3]</b>	Impulse = change in momentum Not 14 or 0 for horizontal speed before impulse aef
	(iii)		$v^2 = (14\sin 30)^2 + 15^2$ $v = 16.6 \text{ ms}^{-1}$ $\tan\theta = 14\sin 30/15$ OR $\tan\psi = 15/14\sin 30$ $\theta = 25(.0)^\circ$ OR $\psi = 65(.0)^\circ$	M1 A1 M1 A1 <b>[4]</b>	Not $(14\sin 30)^2 + (14\cos 30)^2$ Allow $\sqrt{274}$ Correct trig to find an appropriate angle; not $14\cos 30$ for 15
	(iv)		$t = 14\sin 30/g (= 1/1.4 = 0.7142..)$ $T = 1.43 \text{ s}$ $R = 14\cos 30/1.4 + 15/1.4$ $R = 19.4 \text{ m}$	M1 A1 M1A1 A1 <b>[5]</b>	Rise or fall time (not to be given in (i)) Accept 10/7 $(14^2\sin(2 \times 30) + 16.6^2\sin(2 \times 25))/2g$ . 14 resolved, 15 not

7	(i)		<p><math>b + a = 1.8e</math></p> <p><math>0.7b - 0.2a = 0.2 \times 1.8</math></p> <p><math>b = 0.4(1+e)</math>  <math>a = 1.4e - 0.4</math>  <math>1.4e - 0.4 &gt; 0.4 + 0.4e</math>  <math>e &gt; 0.8</math></p> <p><b>OR Last 5 marks</b></p> <p>Using <math>a &gt; b</math>  <math>a &gt; 0.72</math>  <math>b &gt; 0.72</math>  <math>1.8e &gt; 0.72 + 0.72</math>  <math>e &gt; 0.8</math></p> <p><b>OR Last 5 marks</b></p> <p>Using <math>a = b</math> to find <math>a</math> or <math>b</math>  <math>a</math> (or <math>b</math>) = <math>0.9e</math> and <math>a</math> (or <math>b</math>) = <math>0.72</math>  <math>e = 0.8</math>  Convincing argument for correct inequality  <math>e &gt; 0.8</math></p> <p><b>OR Last 5 marks</b></p> <p><math>a = 1.4e - 0.4</math> or <math>b = 0.4(1+e)</math>  Using <math>a &gt; b</math>  <math>a &gt; 0.9e</math> or <math>b &lt; 0.9e</math>  <math>e &gt; 0.8</math></p>	<p>M1 A1 M1 A1 M1 A1 A1 M1 A1 [9] M1 A1 A1 M1 A1 M1 A1 M1 A1 M1 A1 M1 A1</p>	<p>Uses restitution  <math>b - a = 1.8e</math>  Uses momentum  <math>0.7b + 0.2a = 0.2 \times 1.8</math>, signs consistent with first eqn  Solves 2 simultaneous equations (eliminate <math>a</math> or <math>b</math>)</p> <p><math>a = 0.4 - 1.4e</math>  Using <math>a &gt; b</math>, correct signs in <math>a</math> essential</p> <p>correct signs in <math>a</math> essential</p> <p>Solves 2 simultaneous equations (eliminate <math>a</math> or <math>b</math>)  <math>aef</math> or multiples thereof  correct signs in <math>a</math> essential  <math>aef</math> or multiples thereof</p>
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	(ii)	$c - (\pm 0.25) = 1 \times 0.75$ $c = 0.5, 1$ $0.75 \times 0.7 = 0.25 \times 0.7 + m(x1)$ <i>OR</i> $0.75 \times 0.7 = -0.25 \times 0.7 + 0.5m$ $m = 0.35$ (from first equation) $m = 1.4$ (from second equation)	M1 A1A1  M1 A1 A1 <b>[6]</b> B1 M1 A1 M1 A1 A1	Uses restitution with $e = 1$ , either Or $0.75 \pm 0.25$ Uses momentum conservation with correct combination of sign and $c$ value <i>OR</i> $m \times (0.75 \pm 0.25) \pm 0.7 \times 0.25 = 0.75 \times 0.7$  $\frac{1}{2}$ may not be seen At least one momentum equation $mc = 0.35$ and $0.7$
		<b>Total</b>	<b>[72]</b>	

[END]

1	PE = 70x3g KE change = 70x(2.1 <sup>2</sup> - 1.4 <sup>2</sup> )/2 PE change + KE change 2143.75 J	B1 B1 M1 A1 [4]	2058 85.75 Must include evaluation Accept 2140. Allow all values to be negative.
ii	20(90 + T) = 2143.75 T = 17.1875 N	M1 A1ft A1 [3]	Work done = Energy change used ft(cv(2143.75)) accept 17.2
<b>OR</b>	70g.0.15 - 90 - T = 70.(-0.06125) T = 17.1875 N	M1 A1 A1 [3]	Use of v <sup>2</sup> =u <sup>2</sup> + 2as to find a AND use of N2 law(4 terms) accept 17.2
2	21000/25	B1	Use of force = power/speed
i	0 = 21000/25 - 25k - 1250gsin2 k = 16.5	M1 A1 A1 [4]	3 terms cv(21000/25)
ii	21000/v = 16.5v v = 35.7 ms <sup>-1</sup>	M1 A1ft A1 [3]	ft on cv(k)
3	- (8cos30/3)(8 <sup>2</sup> sin60/2) + (4)(8 <sup>2</sup> ) = (8 <sup>2</sup> + 8 <sup>2</sup> sin60/2)(x <sub>G</sub> ) x <sub>G</sub> = 2.09 cm	M1 A1 A1 A1 A1 [5]	Table of moments idea, may include g and/or density. -2.309 x 27.7
ii	tanθ = (2.09/4) θ = 27.6°	M1 A1ft [2]	ft cv(x <sub>G</sub> )

4 ia	If reversed $2.9 + 2 = e(3 + 1.5)$ $e > 1$ impossible	M1 A1 [2]	Award B1 if no explicit numerical justification
b	$2.9 - 2 = e(3 + 1.5)$ $e = 0.2$	M1 A1 [2]	May be seen in ia
ii	$3m - 0.2 \times 1.5 = 2m + 0.2 \times 2.9$ $m = 0.88$	M1 A1 A1 [3]	Conservation of momentum Accept with g included consistently Do not award if g used
iii	$0.68 = 0.2v + 0.2 \times 2.9$ $v = 0.5$ $e = 0.5/2.9$ $e = 0.172$	M1 A1 M1 A1 [4]	Impulse = change in momentum  Separation speed not 2.9 Allow 5/29
5 i	$x = (7\cos 30)t$ $y = (7\sin 30)t - gt^2/2$  $y = x \tan 30 - gx^2/(2 \times 7^2 \cos^2 30)$	B1 B1 M1 A1 [4]	Attempt to eliminate t $y = x/\sqrt{3} - 2x^2/15$ or $y = 0.577x - 0.133x^2$ aef
ii	$2x^2/15 - x/\sqrt{3} + 0.6 = 0$ or $9.8t^2 - 7t + 1.2 = 0$ $x = 1.73$ m or $\sqrt{3}$ m $2.6(0)$ m or $3\sqrt{3}/2$ m	M1 M1 A1 A1 [4]	Create a 3 term Q.E. in x or t with $y = 0.6$ Solve 3 term Q.E. for x or t
iii  OR	$v^2 = (7\sin 30)^2 - 2 \times 9.8 \times 0.6$ $v = 0.7 \text{ ms}^{-1}$ $\tan \theta = 0.7/(7\cos 30)$ $\theta = 6.59^\circ$ to horizontal or $83.4^\circ$ to vertical  Attempt to differentiate equation of trajectory $\tan 30 - gx/(7^2 \cos^2 30)$ Substitute $x = \sqrt{3}$ and equate to $\tan \theta$ $\theta = 6.59^\circ$ to horizontal or $83.4^\circ$ to vertical	M1 A1 M1 A1 [4] M1 A1 M1 A1 [4]	Using $v^2 = u^2 - 2gs$ with u a component of 7; can find t first from their x in (i), and then use $v = u + at$ . Use component of 7  Allow $1/\sqrt{3} - 4x/15$ or $y' = 0.577 - 0.267x$

6 i	$R\sin 30 = 0.3g$  $R\cos 30 = 0.3\omega^2 \times 0.12$ $\omega = 11.9 \text{ rads}^{-1}$	M1 A1 M1 A1 A1 [5]	$R = 5.88$ or $0.6g$  accept $v^2/0.12$ for acceleration cao
ii	$S + R\cos 30 = 0.3 \times 2.1^2 / 0.2$ $R = 5.88$ $S = 1.52 \text{ N}$	M1 A1 B1ft A1 [4]	Resolve and use N2L on sphere Q, 3 terms needed  ft $cv(R)$ from (i)
iii	$v_P = 11.9 \times 0.12$ , or $h = 0.2/\tan 30$ or $0.12/\tan 30$ or $0.08/\tan 30$ $\pm(Q - P) =$ $0.5 \times 0.3(2.1^2 - (11.9 \times 0.12)^2)$ $+ (0.2/\tan 30 - 0.12/\tan 30) \times 0.3g$ $Q - P = \pm 0.763 \text{ J}$	B1 M1 A2ft  A1 [5]	$cv(\omega)$ from (i) Attempt to calculate KE or PE for both particles KE difference (ft on $cv(\omega)$ ) or PE difference  $Q - P = \pm(0.3556 + 0.4074)$
7 i	$F \times 0.8 =$ $0.6\cos 60 \times 550$ $F = 206.25$	M1 A1 A1 A1 [4]	Attempt at moments  Accept 206, cao
ii	$T \times 2 \times 0.8/\tan 30$ $=$ $550 \times (0.8/\sin 30 - 0.6\cos 60)$ $T = 258$  $R = 550 - T\cos 30$ $F_r = T\sin 30$ $\mu = 129/326.6$ $\mu = 0.395$	M1* A1 M1* A1 A1 M1* A1 B1* M1dep* A1 [10]	Moment of T about P $T \times 2.77$ Moment of weight about P $550 \times (1.6 - 0.3)$ Accept to 2sf Resolving vertically, 3 terms needed Value for T not required Value for T not required; accept $<$ or $\leq$ For correct use of $F = \mu R$ , $R \neq 550$

<p><b>OR</b></p>	$T \times 0.8/\tan 30 + 550 \times 0.6\cos 60 = R \times 0.8/\cos 60$ $R = 550 - T\cos 30$ <p>Solve for T or R</p> $T = 258 \text{ or } R = 326.5625$ $Fr = T\sin 30$ $\mu = 129/326.6$ $\mu = 0.395$	<p>M1*</p> <p>A2</p> <p>M1*</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>B1*</p> <p>M1dep*</p> <p>A1</p> <p>[10]</p>	<p>Moments about V, 3 terms needed</p> <p>A1 for two terms correct</p> <p>Resolving vertically, 3 terms needed</p> <p>Accept to 2sf</p> <p>Value for T not required; accept <math>&lt;</math> or <math>\leq</math></p> <p>For correct use of <math>F = \mu R</math>, <math>R \neq 550</math></p>
<p><b>OR</b></p>	$Fr \times 1.6\cos 30 + 550 \times (1.6\sin 30 + 0.6\sin 30) =$ $R \times (1.6 + 1.6\sin 30)$ $R = 550 - T\cos 30$ $Fr = T\sin 30$ <p>Solving for at least one of R, Fr, or T</p> <p>Either <math>R = 326.5625</math>, or <math>Fr = 129(.0017008)</math>, or <math>T = 258</math></p> $\mu = 129/326.6$ $\mu = 0.395$	<p>M1*</p> <p>A2</p> <p>M1*</p> <p>A1</p> <p>B1*</p> <p>M1</p> <p>A1</p> <p>M1dep*</p> <p>A1</p> <p>[10]</p>	<p>Moments about Q, 3 terms needed</p> <p>A1 for two terms correct</p> <p>Resolving vertically, 3 terms needed</p> <p>accept <math>&lt;</math> or <math>\leq</math></p> <p>Only one needed. Accept to 2sf.</p> <p>For correct use of <math>F = \mu R</math>, <math>R \neq 550</math></p>

Question		Answer	Marks	Guidance
1		$v_x = 40\cos 35$ $v_y = 40\sin 35 - 9.8 \times 3$ $v = \sqrt{32.8^2 + 6.46^2}$ or $\tan \theta = 6.46/32.8$ $v = 33.4 \text{ ms}^{-1}$ $\theta = 11.1^\circ$ below horizontal	B1 B1 M1 A1 A1 [5]	Expect 32.8, need not be evaluated. Expect -6.46, need not be evaluated. Use of Pythagoras or relevant trig on cv( $v_x$ ) and cv( $v_y$ )  AEF; allow 11.2
2	(i)	$h = r \tan \alpha$  $x(\frac{2}{3}\pi r^3 + \frac{1}{3}\pi r^2 h) = \frac{1}{3}\pi r^2 h \times \frac{h}{4} - \frac{2}{3}\pi r^3 \times \frac{3}{8}r$  $x = \frac{r(\tan^2 \alpha - 3)}{8 + 4 \tan \alpha}$	B1 M1 A1 A1 [4]	Seen anywhere and in any form. Table of values idea.  <b>AG</b> www
2	(ii)	$x < 0$ Solve $\tan^2 \alpha - 3 < 0$ $\alpha < 60$	B1 M1 A1 [3]	May be implied. Condone = Condone $\leq$ throughout. SC Use of = or > throughout. Max B0 M1 A0
3	(i)	$P \times 1.6 = 10g\cos 60 \times 1.2$ $P = 36.75 \text{ N}$	M1 A1 A1 [3]	Moments about A.  Allow 36.8
3	(ii)	$R + 36.75\sin 30 = 10g$ $F = 36.75\cos 30$  $\mu = 31.8/79.6$ $\mu = 0.4(00)$	M1 A1 FT B1 FT  M1 A1 [5]	Attempt at resolving vertically or taking moments. May be implied. $R = 79.6(25)$ Expect 31.8. Or second correct equation involving $F$ or $R$ or both. For use of (their) $F = \mu(\text{their})R$ $R$ not = $10g$ or their $P$ from (i). AWRT www. Allow inequality

Question			Answer	Marks	Guidance
4	(i)	(a)	$\sin\theta = \frac{1}{2}$ or $\theta = 30$  $T\cos\theta = 0.2 \times 1.2\cos\theta \times 2.5^2$ $T = 1.5 \text{ N}$	B1  M1 A1 A1 [4]	$\theta$ is angle with horizontal. May have angle with vertical. May be seen later. Attempt at resolving horizontally. cv( $r$ ) but not $r = 1.2$ Rounding to 1.5
4	(i)	(b)	$R + T\sin\theta = 0.2g$ $R = 1.21 \text{ N}$	M1 A1 FT A1 [3]	Attempt at resolving vertically. FT on cv( $T$ )
4	(ii)		$r = \sqrt{1.2^2 - 0.6^2} = 1.2\cos\theta$ $R = 0$ $T_1\sin\theta = 0.2g$ $T_1\cos\theta = 0.2 \times v^2/r$ or $0.2 \times r\omega^2$ $v = 4.2 \text{ ms}^{-1}$	B1 B1 B1 M1 A1 [5]	May be seen in (i), must be used in here. May be implied. Attempt at resolving.
5	(i)		25000/10 1500g sin 5  $2500 - 750 - 1500g\sin 5 = 1500a$ $a = 0.313$	B1 B1 M1 A1 A1 [5]	1281.1 Attempt at N2L with 4 terms. cv(1500g sin 5); cv(2500) not 25000. Allow 0.31
5	(ii)		WD against resistance = 750d WD by engine = 25000 × 28 (= 700000) Change in PE = 1500g × d sin 5 Change in KE = $\pm \frac{1}{2} \times 1500 \times (20^2 - 10^2)$  $25000 \times 28 = \frac{1}{2} \times 1500 \times (20^2 - 10^2) + 750d + 1500g \times d \sin 5$ $d = 234$	B1 B1 B1 B1 M1  A1  A1 [7]	750h/sin 5  1500g × h Use of correct formula for KE. Use conservation of energy, at least 3 used including WD by engine.

Question		Answer	Marks	Guidance
6	(i)	$v^2 = 2 \times 9.8 \times 3.136$ $v = 7.84$ Rebound speed = $7.84e$ $I = \pm 0.5(7.84 + 7.84e) = \pm 3.92(1 + e)$	M1 A1 B1 FT B1 FT [4]	Uses $v^2 = u^2 + 2as$ or energy with $u = 0$ . Signs must be consistent. Ignore -ve. AEF seen. FT on $cv(v)$ .
6	(ii)	$-7.84e = 7.84e - gt$ $t = 1.6e$	AG M1 A1 [2]	Uses a complete method to find $t$ .
6	(iii)	(a) $t_2 = 1.6e^2$ (b) $t_3 = 1.6e^3$	B1 B1 [2]	
6	(iv)	Time to first bounce is 0.8 s Identify total time is sum of a GP in $e$ $\frac{1.6e}{1-e} = 4.2$ $e = 0.724$	B1 B1 M1 A1 A1 [5]	Indication of the sum of at least to term in $e^4$ Equate 3.4 or 4.2 or 5 or 5.8 with attempt at use of formula for sum to infinity of a GP. Allow 21/29
7	(i)	For P $4.9t^2 = 60$ $t = 3.5(0)$ For Q $0 = 25\sin\theta \times t - \frac{1}{2} \times 9.8 \times t^2$ $\theta = 43.3$ $PQ = (25\cos\theta - 15) \times t_c$ $= 11.2$	M1 A1 M1 A1 M1 A1 [6]	Signs must be consistent. aef



Question		Answer	Marks	Guidance
7	(ii)	$25\cos\theta(t) = 15(t)$ and solving for $\theta$ $\theta = 53.1$ <i>For Q</i> $s_{y1} = 25\sin\theta \times t - \frac{1}{2} \times 9.8 \times t^2$ <i>For P</i> $s_{y2} = \pm \frac{1}{2} \times 9.8 \times t^2$ Using $s_{y1} + s_{y2} = 60$ Solving for $t$ $t = 3$ $v = 25\sin\theta - 9.8 \times 3$ $v = -9.4$ therefore falling.	M1 A1 B1 B1 *M1 M1dep* A1 M1 A1 [9]	Equating horizontal components of velocity (or displacement) and solving for $\theta$ .  Other methods include finding time to max height for Q.
OR	(ii)	$25\cos\theta(t) = 15(t)$ and solving for $\theta$ $\theta = 53.1$ <i>For Q</i> $y = x \tan\theta - \frac{gx^2}{2 \times (25)^2 \cos^2\theta}$ <i>For P</i> $y = (60 -) \frac{gx^2}{2 \times (15)^2}$ Equate $y$ and solve for $x$ Use $x = u\cos\theta t$ to find $t$ $t = 3$ $v = 25\sin\theta - 9.8 \times 3$ $v = -9.4$ therefore falling.	M1 A1 B1 B1 *M1 M1dep* A1 M1 A1 [9]	Equating horizontal components of velocity (or displacement) and solving for $\theta$ .  Must include 60.  Other methods include finding time to max height for Q.

Question		Answer	Marks	Guidance
1	(i)	Speed = $1.2 \text{ ms}^{-1}$ Impulse = $0.8 \times \pm (4 - -1.2)$ $\pm 4.16 \text{ Ns}$	B1 M1 A1 [3]	May be seen anywhere, even in (ii); allow -1.2 Difference between momenta, allow $0.8 \times \pm (4 - 1.2)$
1	(ii)	KE lost = $\frac{1}{2} \times 0.8 \times (4^2 - (\pm 1.2)^2)$ 5.82(4) J	M1 A1 [2]	Allow -5.82(4)
2	(i)	Driving Force = $20000/20 (= 1000)$  $20000/20 - 800 = 1600a$ $a = 0.125 \text{ ms}^{-2}$	B1 M1  A1 A1 [4]	Attempt at N2L with 3 terms. Signs may not be correct at this stage. Using their 20000/20, but not 20000 Allow $\frac{1}{8}$
2	(ii)	$20000/v$  $DF - 800 - 1600g\sin 4 = 0$ $v = 10.6 \text{ ms}^{-1}$	B1 M1  A1 A1 [4]	3 terms with attempt at resolving weight; g can be omitted at this stage; if F = ..... then F = 0 somewhere to award M aef
3	(i)	$T\cos 30 \times 1.5\sin 30 = 15g \times 2$ $T = 453$	M1 A1 A1 [3]	Attempt at moments about A, g can be omitted at this stage
3	(ii)	$X = T_c\sin 30 (=226)$  $Y + T_c\cos 30 = 15g$  $R = \sqrt{(226^2 + 245^2)}$ or $\tan \theta = 245/226$ $R = 334$ $\theta = 47.3$ below horizontal (to the left)	B1ft M1 A1ft   M1 A1 A1 [6]	Using their value $T$ or taking moments about $P$ Attempt to resolve vertically or taking appropriate moments Using their value $T$ ; expect $Y = -245$ or better Either or both of these equations can be replaced with moments about an appropriate point eg $P, Q, B, c$ of m of beam. Any relevant angle Allow 333 Allow 47.2, 42.7 to the downward vertical SC: If 392 in (i) leading to $Y = \pm 245$ only in (ii) max M1A1

Question		Answer	Marks	Guidance
4	(i)	$\frac{1}{2} \times 9.8 \times t^2 = 0.2$ $t = 0.2(02)$ $s = 14.4 \times t_c$ $s = 2.91 \text{ m}$	M1 A1 M1 A1 <b>[4]</b>	Using SUVAT to find t, consistent signs for g and 0.2 aef Using their value of t
		OR Use equation of trajectory  $-0.2 = x \tan \theta - g x^2 \sec^2 \theta / (2 \times 14.4^2)$ Solve quadratic for x $x = 2.91$	M1  A1 M1 A1 <b>[4]</b>	B1 for correct equation of the trajectory seen anywhere but award in part (ii) unless different method seen; consistent signs for g and 0.2
4	(ii)	$U \sin 15 \times t - \frac{1}{2} \times 9.8 \times t^2 = -0.2$ $U \cos 15 \times t = 6$ Eliminate t Attempt to solve to find U $U = 10.2 \text{ ms}^{-1}$	*M1 A1 B1 Dep*M1 Dep*M1 A1 <b>[6]</b>	Using $s = ut + \frac{1}{2} at^2$ with $s = \pm 0.2$ and $a = \pm g$  Eliminate U Attempt to solve to find t(=0.607)
		OR $y = x \tan \theta - g x^2 \sec^2 \theta / 2U^2$ Substitute values for y, x, $\theta$ $-0.2 = 6 \tan 15 - g.6^2 \sec^2 15 / 2U^2$ Attempt to solve for U $U = 10.2 \text{ ms}^{-1}$	*B1 Dep*M1 A1 Dep*M2 A1 <b>[6]</b>	

Question		Answer	Marks	Guidance
5	(i)	$\sin\theta = 0.8$ or $\cos\theta = 0.6$ or $\tan\theta = 4/3$ or $\theta = 53.1$  $T_A\cos\theta + T_B\cos\theta = 2 \times 1.2 \times 4^2$  $T_A\sin\theta = T_B\sin\theta + 2g$ Solve simultaneously to get at least $T_A$ or $T_B$ $T_A = 44.25$ and $T_B = 19.75$	B1 *M1  A1 *M1 A1 Dep*M1 A1 [7]	$\theta$ is angle AP makes with horizontal Attempt to resolve horizontally and use N2L with a version of acceleration, not just $a$ . Allow $T_A = T_B$ for M1 only.  Use their $\theta$ Attempt to resolve vertically Use their $\theta$  For both. Allow 44.2, 44.3, 19.7, 19.8
5	(ii)	$T_B = 0$  $T_A\cos\theta = 2v^2/1.2$ $T_A\sin\theta = 2g$ Solve for $v$ or $\omega$ $v = 2.97$	B1 *M1  A1 B1 Dep*M1 A1 [6]	May be implied Attempt to resolve horizontally and use N2L with a version of acceleration, not just $a$  Use their $\theta$ Use their $\theta$
6	(i)	$0.2 \times 1.8 = 0.2v_A + 0.4v_B$  $v_B - v_A = \frac{1}{3} \times 1.8$ Solve for $v_A$ or $v_B$ $v_B = 0.8 \text{ m s}^{-1}$ and $v_A = 0.2 \text{ m s}^{-1}$ <b>AG</b>	*M1 A1 *M1 A1 Dep*M1 A1 [6]	Attempt at conservation of momentum  Attempt at restitution aef

Question		Answer	Marks	Guidance
6	(ii)	$0.4 \times 0.8 + 0.6 \times 0.2 = 0.4v_{B'} + 0.6v_C$ $v_C - v_{B'} = e(0.8 - 0.2)$ Use two relevant equations to eliminate $v_C$ State $v_{B'} \geq 0.2$ Set up (in)equality in $e$ and their $v_A$ $0.44 - 0.36e \geq 0.2$ or $0.44 - 0.36e = 0.2$ $e \leq 2/3$ or $0.667$	B1 B1 *M1 B1 dep*M1 A1 A1 [7]	aef  soi, Allow $v_{B'} > 0.2$ Condone incorrect inequality sign for M1 only Allow $0.44 - 0.36e > 0.2$
		OR $0.4 \times 0.8 + 0.6 \times 0.2 = 0.4v_{B'} + 0.6v_C$ $v_C - v_{B'} = e(0.8 - 0.2)$ State $v_{B'} \geq 0.2$ Sub $v_{B'}$ in momentum equation & solve for $v_C$ ( $v_C =$ ) $0.6$ Set up (in)equality in $e$ and their $v_A$  $e \leq 2/3$ or $0.667$	B1 B1 B1 *M1 A1 dep*M1  A1 [7]	aef soi, Allow $v_{B'} > 0.2$  eg $0.6 - e(0.8 - 0.2) \geq 0.2$ , Condone incorrect inequality sign for M1 only

Question		Answer	Marks	Guidance
7	(i)	$\frac{1}{3}a$ $(25 + 2.5a)x_G = 25 \times 2.5 + 2.5a \times (5 + \frac{1}{3}a)$ $x_G = \frac{a^2 + 15a + 75}{3(a+10)}$	B1 M1 A1 A1 A1  [5]	Centre of mass of triangle Table of values idea, using any fixed axis  Relative to the axis they are using
7	(ii)	$\frac{a^2 + 15a + 75}{3(a+10)} = 5$ Solving for $a$ $a = 8.66$ or $5\sqrt{3}$	*M1  dep*M1 A1 [3]	Substitute $x_G$ as 5  $a \leq 8.66$
7	(iii)	$(25 + 2.5a)y_G = 25 \times 2.5 + 2.5a \times (\frac{2}{3} \times 5)$  $y_G = \frac{10a + 75}{3(a+10)}$ or 2.89 $\tan \theta = x_G / y_G$ $= 5 / y_G$ $\theta = 60$	*M1 A1ft  A1ft  dep*M1 A1ft A1 [6]	Method to find centre of mass from $AB$ (or $CD$ ) with or without $a$ substituted.  ft their $a$ from (ii), from $CD$ $y_G=2.11$  Using trig to find an appropriate angle, eg complement of $\theta$ . ft their $a$ from (ii), but not an incorrect $y_G$ $\theta \leq 60$ (anything that rounds to 60)

Question		Answer	Marks	Guidance
1	(i)	$18\cos 15 \times 6$ 104 J	M1 A1 A1 [3]	Force component x distance
1	(ii)	$18\cos 15 \times 6/5$ or ans(i)/5 20.9 W	M1 A1 [2]	Force component x distance/5 Allow 20.8
2	(i)	$DF = 15000/15$  $DF - k \times 15^{1/2} = 1500 \times 0.4$ $k = 103$	B1 M1 A1 A1 [4]	N2L, 3 terms and attempt at DF. Numerical DF Allow $80\sqrt{15}/3$
2	(ii)	$P/30 = k30^{1/2}$ $P = 17000W$	M1 A1 A1 [3]	Using cv(k) Allow 17(.0)kW, 16900W, 16.9kW, $12000\sqrt{2}W$
3	(i)	$a = g\sin 30$  $1+u = 0.4(2+2g\sin 30)$ $u = 3.72 \text{ ms}^{-1}$	B1 M1 A1 A1 [4]	Using NEL with $u_A$ from cv(a), $u_A \neq 0$ cwo
3	(ii)	Use $v^2 = u^2 - 2(g\sin 30)s$ $s = 1.41 \text{ m}$	M1 A1 [2]	Using $v = 0$ , cv(a) from (i) or correct a SC If a not found in (i), allow $a=g$ for M1A0.
3	(iii)	Use of conservation of momentum $0.5 \times 2g\sin 30 - 2m = m - 0.5 \times 3.72$ $m = 2.25$	M1 A1ft A1 [3]	Using cv(a) ft cv(u) from (i) Aef(raction) eg $2^{19/75}$ or $169/75$

Question		Answer	Marks	Guidance
4	(i)	$(2 \times 3\sin(\pi/2))/(3\pi/2)$ or equivalent  $3 \times 6^2$ $-(\pi \times 3^2/2) \times (6 - 4/\pi)$ $= (6^2 - \pi \times 3^2/2)x_G$ $x_G = 1.88 \text{ cm}$	B1 M1 A1 A1 A1 A1 <b>[6]</b>	Centre of mass of semicircle; $4/\pi$ Table of moments idea about any axis.
4	(ii)	$\tan\theta = 1.88/3$ $\theta = 32.1^\circ$	M1 A1ft <b>[2]</b>	Attempt at a relevant angle allow $180-\theta$ & radians (0.561 or 0.560)
5	(i)	Use of moments $2.5R = 3g\cos 60 \times 2$ $R = 11.76 \text{ N}$	M1 A1 A1 <b>[3]</b>	Trig with $3g$ , no trig with $R$ unless using 2 components.  Allow 11.8
5	(ii)	$R' + R\cos 60 = 3g$ $F = R\cos 30$ Use $F = \mu R'$ $\mu = 0.433$	M1 A1ft B1ft M1 A1 <b>[5]</b>	Resolve vertically, 3 terms, comp (R). Using $\cos(R)$ Using $\cos(R)$ Not $R' = 3g$ for method Allow 0.435 from use of $R = 11.8$
6	(i)	Use $I = mv$ $3.6 \text{ ms}^{-1}$	M1 A1 <b>[2]</b>	-3.6 gets A0
6	(ii)	$\pm(1/2 \times 0.5 \times 3.6^2 - 1/2 \times 0.5 \times v^2)$ $0.5 \times g \times 0.3$ Use of conservation of energy $v = 2.66 \text{ ms}^{-1}$	B1 B1 M1 A1 <b>[4]</b>	Three terms



Question		Answer	Marks	Guidance
	<b>OR</b>	$a = -g\sin\theta$ $s = 0.3/\sin\theta$ Use $v^2 = u^2 + 2as$ $v = 2.66 \text{ ms}^{-1}$	B1 B1 M1 A1	$\theta$ angle of plane to horizontal  $a \neq -g, s \neq 0.3.$
<b>6</b>	<b>(iii)</b>	Change in energy = $\pm(1/2 \times 0.5 \times 3^2 - 0.5 \times g \times 0.2)$ Equate to force $\times$ distance 3.175 N	M1 A1  M1 A1 <b>[4]</b>	Difference of KE and PE  Attempt at $0.2/\sin 30$ for dist, 3 terms Allow 3.18
	<b>OR</b>	Using $v^2 = u^2 + 2as$ to find $a$ Resolve parallel to plane $0.5g\cos 60 + F = 0.5 \times cv(11.25)$ $F = 3.175$	M1 M1 A1 A1	Use $v = 0$ , attempt at $s = 0.2/\sin 30$ N2L used with $cv(11.25)$ , 3 terms Consistent signs Allow 3.18
<b>7</b>	<b>(i)</b>	$x = u\cos\theta t$ $y = u\sin\theta t - 1/2gt^2$ Eliminate $t$ Get $y = x\tan\theta - gx^2\sec^2\theta/2u^2$ <b>[AG]</b>	B1 B1 M1 A1 <b>[4]</b>	www
<b>7</b>	<b>(ii)</b>	Substitute $x = 22, y = -2.1$ and $u = 14$ Use $\sec^2\theta = 1 + \tan^2\theta$ Tidy to $12.1\tan^2\theta - 22\tan\theta + 10 = 0$ <b>[AG]</b>  Solve QE for $\tan\theta$ $\theta = 42.3$	M1 B1 A1  M1 A1 <b>[5]</b>	May start again of course  www  allow in radians (0.738)
<b>7</b>	<b>(iii)</b>	$t = 22/14\cos\theta$ $t = 2.12s$	M1 A1 <b>[2]</b>	May work vertically, but must solve for $t$ to get M1

Question			Answer	Marks	Guidance
8	(i)	(a)	$0.8F + 0.6R = 0.4g$ $4F + 3R = 19.6$ [AG]	M1 A1 [2]	Attempt to resolve vertically www
8	(i)	(b)	$0.8R - 0.6F = 0.4 \times 4.5^2/3$ Solve for R or F $F = 1.516$ $R = 4.512$ Use $\mu = F/R$ to get $\mu = 0.336$ [AG]	M1 A1 M1 A1 A1 B1 [6]	Attempt with three terms. aef including cos, sin correct angle Use 2 relevant resolutions.
8	(ii)		$0.6R - 0.8F = 0.4g$ $R = 11.8$ or $F = 3.98$  $0.8R + 0.6F = 0.4 \times 3 \times \omega^2$ $\omega = 3.14 \text{ rad s}^{-1}$	M1 A1 A1 M1 A1 A1 [6]	Resolve vertically, three terms  N2L, resolve horizontally, three terms

Question		Answer	Marks	Guidance
1	(i)	$0.75 \times g \times 8$ 58.8 J	M1 A1 [2]	Weight $\times$ distance Allow -58.8
1	(ii)	$\pm(\frac{1}{2} \times 0.75 \times v^2 - \frac{1}{2} \times 0.75 \times 2^2)$ $\frac{1}{2} \times 0.75 \times v^2 - \frac{1}{2} \times 0.75 \times 2^2 = 58.8$ $v = 12.7 \text{ m s}^{-1}$	*M1 A1 dep*M1 A1 [4]	Attempt at change in KE Equate their change in KE to their PE from (i)
	OR (ii)	$a = g \sin \theta$ $s = \frac{8}{\sin \theta}$ $v^2 = 2^2 + 2 \times g \sin \theta \times \frac{8}{\sin \theta}$ $v = 12.7 \text{ m s}^{-1}$	B1 B1 M1 A1 [4]	$\theta$ is angle of slope to horizontal.  Not $a = g$ , not $s = 8$
2	(i)	20000/32 $R = 20000/32$ $R = 625 \text{ N}$	B1 M1 A1 [3]	cao
2	(ii)	$F + 1500g \sin 2 - 625 = 1500 \times 0.1$ Power = $32 \times F$ Power = 8380 W or 8.38 kW	M1 A1ft M1 A1 [4]	Using Newton 2, all forces used. ft their $R$ from (i) SC $F - 1500g \sin 2 - 625 = 1500 \times 0.1$ Using their $F$ . 8383.27.... SC 41200 W or 41.2 kW (41216.7...)
3	(i)	$x_G = (2 \times 2) / \pi$  $P(\text{or } X) \times 4 = 0.3g \times x_G$ $Y = 0.3g$ Use $R^2 = X^2 + Y^2$ to find $R$ $R = 3.09 \text{ N}$	B1 *M1 A1ft B1 dep*M1 A1 [6]	$x_G = 1.2732$ .... May be seen in (ii), <b>mark only once</b> . Take moments about $A$ or $B$ $P = 0.9358$ .... ft their $x_G$ for this mark.

Question		Answer	Marks	Guidance
3	(ii)	$P \times 4 =$ $0.3g \times (2\sin 30 + x_G \sin 60)$ $P = 1.55$	M1 A1 A1 A1 <b>[4]</b>	Attempt at moments, force $\times$ distance = $0.3g \times$ distance  $0.3g \times 2.1026\dots\dots$ $1.545453\dots\dots$
4	(i)	$4.4x_G = 4 \times \frac{1}{4} \times 8$ $- 0.4 \times \frac{1}{3} \times 10$ $x_G = 1.52 \text{ cm}$	M1 A1 A1 A1 <b>[4]</b>	Table of moments idea. Moments about other axes acceptable  Allow $\frac{50}{33}$
4	(ii)	$T_{\text{shell}} \times 18 = 4.4g \times (8 - 1.52)$ or $T_{\text{cone}} \times 18 = 4.4g \times (10 + 1.52)$ $T_{\text{shell}} + T_{\text{cone}} = 4.4g$ $T_{\text{shell}} = 15.5$ and $T_{\text{cone}} = 27.6$	M1 A1ft M1 A1 <b>[4]</b>	Or any other correct moment equation. ft on $x_G$ from (i) May use a second moments equation For both
5	(i)	Vertical force = $mg$ Horizontal force = $m \times 0.4 \times 7^2$ Uses vertical force = $\mu \times$ horizontal force $\mu = 0.5$	*B1 *M1A1 dep*M1 A1 <b>[5]</b>	Dependent on B1 and M1 If a value for $m$ used B0M1A0M1A0 max.
5	(ii)	$mg = T \times 0.3/0.5$  $m \times 0.4 \omega^2 = T \times 0.4/0.5$ Solve for $\omega$ or $v$ $\omega = 5.72 \text{ rad s}^{-1}$	B1 *M1 A1 dep*M1 A1 <b>[5]</b>	Resolve $T$ and equate to mass $\times (r\omega^2$ or $v^2/r)$  allow $7\sqrt{6}/3$ If a value for $m$ and/or $T$ used B0M1A0M1A0 max.

Question		Answer	Marks	Guidance
6	(i)	$4 - 4(1 - e + e^2) = -e(u - 4)$ $u = 4e$ $mu + 0.2 \times 4 = 0.2 \times 4(1 - e + e^2) + 4m$ $m = 0.2e$	M1 A1 A1 M1 A1 A1 <b>[6]</b>	Use of restitution, may have sign errors, must be correct ratio ( $v/u$ ) oe Use of conservation of momentum oe
6	(ii)	Valid method to find $e$ that gives the least speed Get $e = \frac{1}{2}$  $\frac{1}{2} \times 0.2 \times 4^2 + \frac{1}{2} \times 0.1 \times 2^2 - (\frac{1}{2} \times 0.2 \times 3^2 + \frac{1}{2} \times 0.1 \times 4^2)$ (+/-) 0.1 J	M1 A1 M1 A1 A1 <b>[5]</b>	Differentiate $v_A$ and equate to 0 or complete the square on $v_A$ www Difference of KE with 4 terms Must have found the value of $e$ from a legitimate method. www SCM1A1 Loss of KE = $8e(1 - e)^3/5$ or $8e(1 - 3e + 3e^2 - e^3)/5$ or $8e/5 - 24e^2/5 + 24e^3/5 - 8e^4/5$
6	(iii)	$0.2e(4 - 4e) = 0.192$ or $0.2(4 - (4 - 4e + 4e^2)) = 0.192$ Solve three term QE in $e$ $e = 0.4$ or $0.6$	*M1 A1 dep*M1 A1 <b>[4]</b>	Attempt to use impulse = change in momentum on one particle method should lead to 2 real values for $e$ For both
7	(i)	$u \cos \theta = 14 \cos 20$ $-14 \sin 20 = u \sin \theta - 1.4g$ $u^2 = (1.4g - 14 \sin 20)^2 + (14 \cos 20)^2$ $u = 15.9$ <b>AG</b> $\tan \theta = (1.4g - 14 \sin 20)/14 \cos 20$ $\theta = 34.2$	B1 M1 A1 M1 A1 M1 A1 <b>[7]</b>	$U_x = 13.15...$ Horizontal component of initial velocity, could use $U_x$ Complete method to find vertical component of initial velocity, could use $U_y$ $U_y = 8.9317.....$ Method to find $u$ cwo Method to find $\theta$ or a relevant angle SC M1A1 for $-\tan 20 = (u \sin \theta - 1.4g)/u \cos \theta$ <b>OR</b> $14^2 = (u \sin \theta - 1.4g)^2 + (u \cos \theta)^2$ B1M1A1 for both.

Question		Answer	Marks	Guidance
7	(ii)	$\frac{1}{2} m(15.9^2 - 14^2) = mgy$ $y = 2.9 \text{ m}$	M1 A1 A1 [3]	Method to find Level of $P$ above $A$
	OR (ii)	$(14\sin 20)^2 = (15.9\sin \theta)^2 - 2gs$ or $s = 15.9\sin \theta \times 1.4 - \frac{1}{2}g \times 1.4^2$ $s = 2.9 \text{ m}$	M1 A1ft A1 [3]	Use constant acc formulae, a complete method needed. ft their $\theta$ from (i). no $\theta$ value used then M1A0.
7	(iii)	$-2.9 = v\sin 20.t - 9.8t^2/2$ $2.9\tan 20 = v\cos 20.t$ Eliminate $t$ to obtain equation in $v$ only Solve for $v$ $v = 1.37$	B1ft B1ft M1 M1 A1 [5]	ft their 2.9 ft their 2.9 Eliminate $v$ to obtain equation in $t$ only and solve for $t$ Substitute $t$ to find $v$
	OR (iii)	$-2.9 = (2.9\tan 20) \times \tan 20 - g(2.9\tan 20)^2/2v^2\cos^2 20$ Solve for $v$ $v = 1.37$	M2 A1ft M1 A1 [5]	Using equation of trajectory method.
	OR (iii)	$2.9/\cos 20 = \frac{1}{2}g\cos 20 \times t^2$ $0 = vt - \frac{1}{2}g\sin 20 \times t^2$ Eliminate $t$ Solve for $v$ $v = 1.37$	B1ft B1 M1 M1 A1 [5]	$t = 0.817$
7	(iv)	$e = 0.098$	B1ft [1]	ft their $v$ from (iii), must be $v/14$ .

Question		Answer	Marks	Guidance
1	(i)	$(20\sin\theta)^2 - 2g(2.44) = 0$ $\theta = 20.2$	M1 A1 [2]	Use $v^2 = u^2 + 2as$ vertically with $v = 0$ $\theta = 20.22908\dots$
	(ii)	$20 \sin cv(\theta)t - 1/2gt^2 = 0$ AND range = $20 \cos cv(\theta)t$  Range = 26.5 m	M1  A1 [2]	Use $s = ut + \frac{1}{2}at^2$ vertically with $s = 0$ OR use $v = u + at$ and doubles $t$ AND horizontally with time found from vertical. ( $t = 1.4113\dots$ s or $1.4093\dots$ s (from 20.2)) Range = 26.48541... m or 26.45387...m (from 20.2)
	OR	$\frac{20^2 \sin(2 \times cv(\theta))}{g}$ Range = 26.5 m	M1  A1 [2]	Use of range formula  Range = 26.48541... m or 26.45387...m (from 20.2)
2	(i)	$r/6 = \tan 21$ $r = 2.3(0)$	M1 A1 A1 [3]	Attempt to use trigonometry to form equation for $r$  $r = 2.30318\dots$
	(ii)	$\mu < cv(r)/6$ or $\mu mg \cos 21 < mg \sin 21$ $\mu < 0.384$ or $\tan 21$	M1 A1 [2]	Attempt comparison between weight comp and max friction. $\mu < 0.38386\dots$ or $0.38333\dots$ (from 2.3); allow $\leq$
3	(i)	CoM of triangle = $\frac{1}{3} \times cv(12)$ from $BD$  $(80 + 60)x_G = 4(80) + 12(60)$ $x_G = 7.43$ cm	B1 M1 A1 A1 A1 [5]	OR $\frac{2}{3} \times cv(12)$ from C. CoM of triangle Table of values idea  $7.42857\dots$ or $\frac{52}{7}$ cm
	(ii)	$\tan\theta = (8 - x_G)/5$ $\tan\theta = 0.5714\dots/5$ $\theta = 6.52^\circ$	M1 A1ft A1 [3]	Using $\tan$ to find a relevant angle fit their $x_G$ to target angle with the vertical $6.5198\dots$ Allow $6.5(0)$ from $x_G = 7.43$

Question		Answer	Marks	Guidance
4	(i)	$18(10) - T(20\sin\theta) + 3(6) = 0$ $T = 16.5 \text{ N}$	M1 A1 A1 [3]	Moments about $P$ Need a value for $\sin\theta$ or $\theta$ Exact
	(ii)	$X = T\cos\theta$  $Y + T\sin\theta - 18 - 3 = 0$ $R = \sqrt{(13.2^2 + 11.1^2)} = 17.2 \text{ N}$	B1ft  M1 A1ft A1 [4]	ft candidates value of $T$ . Resolve horizontally ( $X = 13.2 \text{ N}$ ) or moments; Need a value for $\cos\theta$ or $\theta$ Resolve vertically or moments ft candidates value of $T$ . $Y = 11.1 \text{ N}$ ; Need a value for $\sin\theta$ or $\theta$ $R = 17.2467\dots$
	(iii)	$\mu = cv( Y )/cv( X ) = 11.1/13.2$ $\mu = 0.841$	M1 A1 [2]	Use of $Fr = \mu R$ $\mu = 0.8409\dots$ ; allow $^{37}/_{44}$
5	(i)	Driving Force = $10000/20$ (= 500)  $cv(10000/20) - 1300 + 800g\sin\alpha = 0$  $\sin\alpha = 5/49$	B1 M1 A1  A1 [4]	Attempt at N2L with 3 terms  <b>AG</b> at least one more line of correct working (at least e.g. $-800+800g\sin\alpha=0$ ); allow verification (e.g. $500 - 1300 + 800 = 0$ )
	(ii)	$800(22.1)g\sin\alpha$  $800(22.1)g\sin\alpha + 1300(22.1) + \frac{1}{2}(800)(8^2)$  $t = 3.6(0) \text{ s}$	B1 M1 A1 M1 A1 [5]	Work done against weight; Need a value for $\sin\alpha$ or $\alpha$ Total work done, 3 terms needed Need a value for $\sin\alpha$ or $\alpha$ ; (72010 J) Time = work done(from at least one correct energy term)/power 'Exact' is 3.6005
6	(i)	$(2m)(4) - (3m)(2) = 2mv_A + 3mv_B$  $(v_B - v_A)/(4 - -2) = 0.4$  Speed $A = 1.04 \text{ m s}^{-1}$ , Speed $B = 1.36 \text{ m s}^{-1}$	*M1 A1 *M1 A1 Dep**M1 A1 [6]	Attempt at use of conservation of momentum  Attempt at use of coefficient of restitution  Solving for $v_A$ and $v_B$ Final answers must be positive



Question		Answer	Marks	Guidance
	(ii)	Energy before = $\frac{1}{2}(2m)(4^2) + \frac{1}{2}(3m)(2^2)$ Energy after = $\frac{1}{2}(2m)(1.04^2) + \frac{1}{2}(3m)(1.36^2)$  $22m - 3.856m$  $18.1m$	B1ft B1ft  M1  A1 <b>[4]</b>	Energy before or Loss in A's KE Energy after or Loss in B's KE  Difference of total OR sum of differences (total kinetic energy must decrease) $18.144m$ (Exact)
	OR	$\frac{1}{2} \frac{m_1 m_2}{m_1 + m_2} (1 - e^2) A^2$  $\frac{1}{2} \frac{(2m)(3m)}{2m + 3m} (1 - 0.4^2)(4 + 2)^2$ $18.1m$	*B1  Dep*M1  A1 A1 <b>[4]</b>	Loss of kinetic energy formula, where A = approach speed  Substitution of values into quoted formula  $18.144m$ (Exact)
	(iii)	$2m(4) - 2m(-1.04) = 2.52$ $m = 0.25$	M1 A1ft A1 <b>[3]</b>	Attempt at change in momentum and equate to impulse. Must use 2m or 3m Or $3m(2) - 3m(-1.36) = 2.52$ Exact
7	(i)	$T \cos 30 + T \cos 45 = 0.4g$ $T = 2.49 \text{ N}$	M1 A1 A1 <b>[3]</b>	Resolve vertically (3 terms); may be different T's at this stage  $T = 2.4918\dots$
	(ii)	$cv(T) \sin 30 + cv(T) \sin 45 = 0.4v^2/0.5$ $v = 1.94 \text{ m s}^{-1}$	M1 A1 A1 <b>[3]</b>	Resolve horizontally (3 terms); may be different T's at this stage Or use acceleration = $0.5 \omega^2$ $v = 1.93904\dots$
	(iii)	$(2AP =) \frac{0.5}{\sin 45} + \frac{0.5}{\sin 30}$ $AP = 0.854 \text{ m}$	M1 A1 <b>[2]</b>	Reasonable attempt to use trigonometry to find total length of string <b>AG</b> ( $AP = 0.85355\dots \text{m}$ )

Question		Answer	Marks	Guidance
	(iv)	$2T\sin\theta = 0.4(0.854\sin\theta)(3.46^2)$ $T = 2.04 \text{ N}$ $2T\cos\theta = 0.4g$ $\theta = 16.5^\circ \text{ or } 16.6^\circ$	M1 A1 M1 A1 <b>[4]</b>	$\theta$ angle with vertical. Resolve horizontally. Allow with T only. $r =$ component of 0.854 $T = 2.04474\dots \text{ N}$ using $AP = 0.854 \text{ m}$ , $T = 2.04367\dots \text{ N}$ using exact $AP$ $\theta$ angle with vertical. Resolve vertically. Allow with T only $\theta = 16.55377\dots^\circ$ using $AP = 0.854 \text{ m}$ , $\theta = 16.4526\dots^\circ$ using exact $AP$ <b>SC M1A0M1A1</b> for use of T instead of 2T throughout
8	(i)	$v_x = 12\cos 20$ $8 = 12t \cos 20$ $v_y = 12\sin 20 - gcv(t)$ $\tan\theta = v_y / v_x$ $14.2^\circ$ below horizontal	*B1 B1 *M1 A1 Dep**M1 A1 <b>[6]</b>	$11.27631\dots$ Using suvat to find expression in $t$ only. ( $t = 0.70945\dots$ ) Attempt at use of $v = u + at$ $-2.84838\dots$ Use trig to find a relevant angle $14.1763\dots$ ( $75.8^\circ$ downward vertical)
	(ii)	$8 = Vt\cos 20$ $1.5 = Vt\sin 20 - gt^2/2$ Eliminate $t$ Attempt to solve a quadratic for $V$ $V = 15.9$	B1 *M1 A1 dep*M1 dep*M1 A1 <b>[6]</b>	Attempt at use of $s = ut + \frac{1}{2}at^2$ OR Eliminate $V$ and solve for $t$ AND Sub value for $t$ and solve for $V$ $V = 15.8606\dots$
	OR	$y = x\tan\theta - gx^2 \sec^2 \theta / 2u^2$ Substitute values for $y, x, \theta$ $1.5 = 8\tan 20 - g8^2 \sec^2 20 / 2V^2$ Attempt to solve a quadratic for $V$ $V = 15.9$	*B1 dep*M1 A1 dep*M2 A1 <b>[6]</b>	Use equation of trajectory  SC M1 for solving for $V^2$ $V = 15.8606\dots$