4762

PMT

01				
(a) (i)	Impulse has magnitude $2 \times 9 = 18$ N s speed is $\frac{18}{6} = 3$ m s ⁻¹ .	B1 B1		2
(ii)	PCLM \rightarrow 3×6-1×2=8v v = 2 so 2 m s ⁻¹ in orig direction of A	M1 A1 E1	Use of PCLM + combined mass RHS All correct Must justify direction (diag etc)	3
(iii)	$\rightarrow 2 \times 2 - 2 \times -1 = 6$ N s	M1 A1	Attempted use of <i>m</i> v - <i>m</i> u for 6 N s dir specified (accept diag)	2
(iv) (A)	$2 \text{ ms}^{-1} \qquad 1.8 \text{ m s}^{-1}$ $AB \qquad C$ $v \text{ ms}^{-1} \qquad 1.9 \text{ m s}^{-1}$	B1	Accept masses not shown	1
(B)	PCLM \rightarrow 2×8+10×1.8 = 8v+10×1.9 v = 1.875	M1 A1 A1	PCLM. All terms present Allow sign errors only	3
(C)	NEL $\frac{1.9 - 1.875}{1.8 - 2} = -e$ so $e = 0.125$	M1 A1 F1	Use of NEL with their v Any form. FT their v FT their v (only for $0 < e \le 1$)	3
(b)	Using $v^2 = u^2 + 2as$ $v = \sqrt{2 \times 10 \times 9.8} = 14$ rebounds at $14 \times \frac{4}{7}$ $= 8 \text{ m s}^{-1}$ No change to the horizontal component Since both horiz and vert components are 8 m s^{-1} the angle is 45°	B1 M1 F1 B1 A1	Allow ±14 Using their <i>vertical</i> component FT from their 14. Allow ± Need not be explicitly stated cao	5
		19		

Q 2				
(i)	$\theta = \frac{\pi}{2}$	B1		
	gives CG = $\frac{\frac{3311}{2}}{\frac{\pi}{2}} = \frac{16}{\pi}$	E1		
	$\left(-\frac{16}{\pi},8\right)$ justified	E1		3
(ii)	$(8\pi + 72) \left(\frac{\overline{x}}{\overline{y}}\right) = 8\pi \left(-\frac{16}{\pi}\right) + 72 \left(\frac{36}{0}\right)$ $\left(\frac{\overline{x}}{\overline{y}}\right) = \left(\frac{25.3673}{2.06997}\right) = \left(\frac{25.37}{2.07}\right) (4 \text{ s. f.})$	M1 B1 A1 E1 E1	Method for c.m. Correct mass of 8 or equivalent 1 st RHS term correct 2 nd RHS term correct [If separate cpts award the A1s for <i>x</i> - and <i>y</i> - cpts correct on RHS]	
(iii)	A α / 25.37 G / 25.37	B1	General position and angle (lengths need not be shown)	0
	$\tan \alpha = \frac{13.93}{25.37}$ $\alpha = 28.7700$ so 28.8° (3 s. f.)	M1 M1 A1 A1	Angle or complement attempted. arctan or equivalent. Attempt to get 16 – 2.0699 Obtaining 13.93 cao Accept use of 2.0699 but not 16. cao	
(iv)	c. w. moments about A $12 \times 13.93 - 16F = 0$	M1 A1	[FT use of 2.0699] Moments about any point, all forces present	5
	so <i>F</i> = 10.4475	A1	(1.5525 if 2.0699 used)	3
		17		

June 2007

Q 3				
(i)	Moments c.w. about B $200 \times 0.6 - 0.8R_A = 0$ $R_A = 150$ so 150 N Resolve or moments $R_B = 50$ so 50 N	M1 A1 M1 F1	Accept about any point. Allow sign errors.	4
(ii)	Moments c.w. about D $-0.8R_{\rm C} + 1.2 \times 200 = 0$ $R_{\rm C} = 300 \uparrow$ Resolve or moments $R_{\rm D} = 100 \downarrow$	M1 A1 M1 A1 E1	Or equiv. Accept about any point. All terms present. No extra terms. Allow sign errors. Neglect direction Or equiv. All terms present. No extra terms. Allow sign errors. Neglect direction Both directions clearly shown (on diag)	5
(iii)	Moments c.w. about P $0.4 \times 200 \cos \alpha - 0.8R_Q = 0$ $R_Q = 96 \text{ so } 96 \text{ N}$ resolve perp to plank $R_P = 200 \cos \alpha + R_Q$ $R_P = 288 \text{ so } 288 \text{ N}$	M1 A1 A1 M1 A1 A1	Or equiv. Must have some resolution. All terms present. No extra terms. Allow sign errors. Correct [No direction required but no sign errors in working] Or equiv. Must have some resolution. All terms present. No extra terms. Allow sign errors. Correct [No direction required but no sign errors in working]	6
(iv)	Need one with greatest normal reaction So at P Resolve parallel to the plank $F = 200 \sin \alpha$ so $F = 56$ $\mu = \frac{F}{R}$ $= \frac{56}{288} = \frac{7}{36}$ (= 0.194 (3 s. f.))	B1 B1 M1 A1	FT their reactions Must use their <i>F</i> and <i>R</i> cao	4

June 2007

Q 4				
(i)	either $0.5 \times 20 \times 0.5^{2} + 20 \times 9.8 \times 4$ = 786.5 J or	M1 B1 B1 A1	KE or GPE terms KE term GPE term cao	
	$a = \frac{1}{32}$ $T - 20g = 20 \times \frac{1}{32}$ T = 196.625 WD is $4T = 786.5$ so 786.5 J	B1 M1 A1 A1	N2L. All terms present.	4
(ii)	$20g \times 0.5 = 10g \text{ so } 98 \text{ W}$	M1 A1 A1	Use of $P = F_V$ or $\Delta WD / \Delta t$ All correct	3
(iii)	GPE lost is $35 \times 9.8 \times 3 = 1029$ J KE gained is $0.5 \times 35 \times (3^2 - 1^2) = 140$ J so WE gives WD against friction is 1029 - 140 = 889 J	B1 M1 A1 M1 A1	ΔKE The 140 J need not be evaluated Use of WE equation cao	5
(iv)	either $0.5 \times 35 \times 3^{2} + 35 \times 9.8 \times 0.1x = 150x$ x = 1.36127 so 1.36 m (3 S. F.) or $25a \times 0.1$, $150 = 25x$	M1 B1 B1 A1 A1	WE equation. Allow 1 missing term. No extra terms. One term correct (neglect sign) Another term correct (neglect sign) All correct except allow sign errors cao	
	$35g \times 0.1 - 150 = 35a$ a = -3.3057 0 = 9 - 2ax x = 1.36127 so 1.36 m (3 S. F.)	M1 A1 A1 M1 A1 17	Use of N2L. Must have attempt at weight component. No extra terms. Allow sign errors, otherwise correct cao Use of appropriate <i>uvast</i> or sequence cao	5