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Q 1		mark		Sub
(a) (i)	240 i N s →	B1		1
(ii) (A)	240 i = 70 i +50 v so v = 3.4 i m s ⁻¹	M1 A1	Equating to their 240 i in this part FT 240 i	
(B)	$240 \ \mathbf{i} = 70u \ \mathbf{i} - 50u \ \mathbf{i}$	M1	Must have <i>u</i> in both RHS terms and opposite signs	
	$u = 12 \text{ so } \mathbf{v} = -12 \mathbf{i} \text{ m s}^{-1}$	A1	FT 240 i	
(C)	$240 \; \mathbf{i} = 280(\; \mathbf{i} + \mathbf{j} \;) + 50 \mathbf{v}_{\mathrm{B}}$	M1	FT 240 i Must have all terms present	
	so $\mathbf{v}_{\rm B} = (-0.8 \mathbf{i} - 5.6 \mathbf{j}) \text{m s}^{-1}$	A1	cao	6
(b) (i)	before $\frac{4 \text{ m s}^{-1}}{2 \text{ kg}}$ $\frac{2 \text{ m s}^{-1}}{3 \text{ kg}}$ NEL $\frac{v_2 - v_1}{-2 - 4} = -0.5$ so $v_2 - v_1 = 3$ PCLM $8 - 6 = 2v_1 + 3v_2$ Solving $v_2 = 1.6$ so $1.6 \text{ m s}^{-1} \rightarrow v_1 = -1.4$ so $1.4 \text{ m s}^{-1} \leftarrow 0.5$	M1 A1 M1 A1 A1	NEL Any form PCLM Any form Direction must be clear (accept diagram) Direction must be clear (accept diagram). [Award A1 A0 if v_1 & v_2 correct but directions not clear]	6
(ii)	$1.6~{\rm m~s}^{-1}$ at 60° to the wall (glancing angles both 60°)	B1 B1	FT their 1.6	
	No change in the velocity component parallel to the wall as no impulse No change in the velocity component perpendicular to the wall as perfectly elastic	E1 E1	Must give reason Must give reason	
	total	17		4

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Q 2		mark		Sub
(i)		man n		Dab
(1)	We need $\frac{mgh}{t} = \frac{850 \times 9.8 \times 60}{20} = 24990$	M1	Use of $\frac{mgh}{t}$	
	so approx 25 kW	E1	Shown	
	so approx 23 kW	EI	Silowii	2
(ii)				
	Driving force $-$ resistance $=$ 0	B1	May be implied	
	25000 = 800v	M1	Use of $P = Fv$	
	so $v = 31.25$ and speed is 31.25 m s^{-1}	A1		3
(iii)				
(111)	25000			
	Force is $\frac{25000}{10} = 2500 \text{ N}$	B1		
	N2L in direction of motion			
	2500 - 800 = 850a $a = 2 \text{ so } 2 \text{ m s}^{-2}$	M1	Use of N2L with all terms	
	a = 2 so 2 m s	A1		3
(iv)				3
	$0.5 \times 850 \times 20^2 = 0.5 \times 850 \times 15^2$	M1	W-E equation with KE and power term	
	0.6 1.06 0.12	B1	One KE term correct	
	$+25000 \times 6.90$	B1	Use of Pt .Accept wrong sign	
	-800x	B1	WD against resistance. Accept wrong sign	
	122 (5(2)	A1	All correct	
	x = 122.6562 so 123 m (3 s. f.)	A1	cao	6
(v)	either			
. ,	$0.5 \times 850 \times v^2 = 0.5 \times 850 \times 20^2$	M1	W-E equation inc KE, GPE and WD	
			-	
	$-850 \times 9.8 \times \frac{105}{20}$	M1	GPE term with attempt at resolution	
	20		_	
		A1	Correct. Accept expression. Condone wrong sign.	
	-800×105	B1	WD term. Neglect sign.	
	$v^2 = 99.452$ so 9.97 m s ⁻¹	A1	cao	
	or			
	N2L + ve up plane	3.51	NOT All .	
	$-(800 + 850g \times 0.05) = 850a$	M1	N2L. All terms present. Allow sign errors.	
	a = -1.43117 $v^2 = 20^2 + 2 \times (-1.43117) \times 105$	A1	Accept ±	
	$V = 20 + 2 \times (-1.4511/) \times 105$	M1	Appropriate <i>uvast</i> . Neglect signs.	
		A1	All correct including consistent signs. Need not follow sign of <i>a</i> above.	
	$v^2 = 99.452$ so 9.97 m s ⁻¹	A1	cao	5
	v = 77.432 80 7.7/ III 8	19		3
		17		1

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Q3		mark		Sub
(i)	$28\left(\frac{\overline{x}}{\overline{y}}\right) = 16\left(\frac{2}{2}\right) + 2\left(\frac{5}{0}\right) + 2\left(\frac{6}{1}\right) + 2\left(\frac{5}{2}\right)$ $+ 2\left(\frac{0}{5}\right) + 2\left(\frac{1}{6}\right) + 2\left(\frac{2}{5}\right)$ $\overline{x} = 2.5$ $\overline{y} = 2.5$	M1 B1 B1	Complete method Total mass correct 3 c. m. correct (or 4 <i>x</i> - or <i>y</i> -values correct)	
			[Allow A0 A1 if only error is in total mass] [If $\bar{x} = \bar{y}$ claimed by symmetry and only one component worked replace final A1, A1 by B1 explicit claim of symmetry A1 for the 2.5]	5
(ii)	$\overline{x} = \overline{y}$ $28\overline{x} = 16 \times 2 + 6 \times 4 + 2 \times 0 + 2 \times 1 + 2 \times 2$ $\overline{x} = \frac{31}{14} (2.21428)$	B1 M1 A1	Or by direct calculation Dealing with 'folded' parts for \overline{x} or for \overline{z} At least 3 terms correct for \overline{x}	
	$\overline{z} = \frac{8 \times (-1) + 4 \times (-2)}{28} = -\frac{4}{7} (-0.57142)$	A1 A1	All terms correct allowing sign errors	
	Distance is $\sqrt{\left(\frac{31}{14}\right)^2 + \left(\frac{31}{14}\right)^2 + \left(\frac{4}{7}\right)^2}$ = 3.18318 so 3.18 m (3 s. f.)	M1 F1	Use of Pythagoras in 3D on their c.m.	8
(iii)	A	M1	c.m. clearly directly below A	
	3.18318 centre of mass	В1	Diagram showing α and known lengths (or equivalent). FT their values. Award if final answer follows their values.	
	$\sin \alpha = \frac{4}{7}/3.18318$ so $\alpha = 10.3415$ so 10.3° (3 s. f.)	M1 A1	Appropriate expression for α . FT their values.	
	· ´			4
	total	17		

Q 4		mark		Sub
(a)	Moments c.w. about A			
(i)	2R = 5L so R = 2.5L	E1		
	Resolve $\rightarrow U = 0$	E1		
	Resolve \uparrow $V + R = L$	M1	Resolve vertically or take moments about B (or C)	
	so $V = -1.5L$	E1		
	30 V = 1.3L	LI		4
(ii)	$A \bigcirc \longrightarrow T_{AC}$			
	45°			
		M1	Equilibrium at a pin-joint	
	$1.5 L$ T_{AB}			
		3.//1	Assume the second state of	
	For equilibrium at A	M1	Attempt at equilibrium at A or C including resolution with correct angle	
	$\uparrow T_{AB}\cos 45 + 1.5L = 0$		with correct angle	
	so $T_{AB} = -\frac{3\sqrt{2}L}{2}$ so $\frac{3\sqrt{2}L}{2}$ N (C) in AB	A1	(2.12 <i>L</i> (3 s. f.))	
	$\rightarrow T_{AC} + T_{AB} \cos 45 = 0$			
		F21	(1.51)	
	so $T_{AC} = \frac{3L}{2}$ so $\frac{3L}{2}$ N (T) in AC	F1	(1.5L)	
	At C $\downarrow L + T_{BC}\cos\theta = 0$	M1	Must include attempt at angle	
	$\tan \theta = 3/2 \Rightarrow \cos \theta = 2/\sqrt{13}$	B1		
	so $T_{BC} = -\frac{\sqrt{13}L}{2}$ so $\frac{\sqrt{13}L}{2}$ N (C) in BC	A1	(1.80 <i>L</i> (3 s. f.))	
	so $I_{BC} = -\frac{1}{2}$ so $\frac{1}{2}$ N (C) in BC			
		F1	Award for T/C correct from their internal forces. Do not award without calcs	8
(b)	F		DO HOUR WALLS WILLIAM CALLS	
(i)	$\int_{\Gamma}^{F} \int_{\Gamma}^{R}$			
	G S		A11 C	
	A \(\sigma'\)	B1	All forces present with arrows and labels. Angles and distances not required.	
	$B \theta$		Angles and distances not required.	
	W •			
/···				1
(ii)	c.w.moments about B $R \times 3 - W \times 1 \cos \theta = 0$	M1	If moments about other than B, then need to resolve	
	$ \Lambda \wedge J - W \wedge I \cos \sigma - U $	1411	perp to plank as well	
		A1	Correct	
	so $R = \frac{1}{3}W\cos\theta$	A1		
	3" 2000	111		
(j;;)	Pacalya parallal to plank			3
(iii)	Resolve parallel to plank $F = W \sin \theta$	B1		
		וע		
	$\mu = \frac{F}{R} = \frac{W \sin \theta}{\frac{1}{3} W \cos \theta} = 3 \tan \theta$	M1	Use of $F = \mu R$ and their F and R	
	$\frac{1}{3}W\cos\theta$	1,11	,	
		A1	Accept any form.	
				3
	total	19		