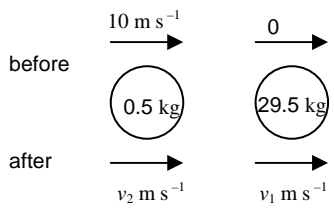
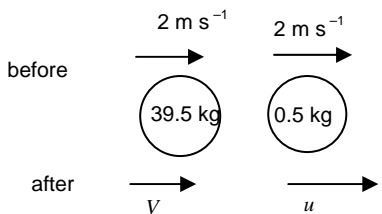
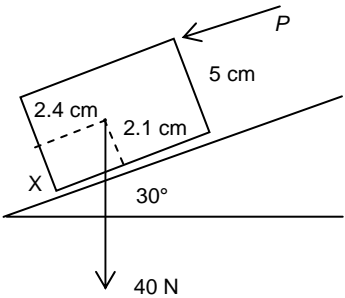


| Q 1         |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     | mark                                   |                                                                                                                                               | sub |
|-------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------------------|-----------------------------------------------------------------------------------------------------------------------------------------------|-----|
| (i)         |  <p>before</p> <p>10 m s<sup>-1</sup> → 0 →</p> <p>0.5 kg 29.5 kg</p> <p>after</p> <p>→ →</p> <p>v<sub>2</sub> m s<sup>-1</sup> v<sub>1</sub> m s<sup>-1</sup></p> <p><math>10 \times 0.5 = 0.5v_2 + 29.5v_1</math></p> <p><math>\frac{v_1 - v_2}{0 - 10} = -0.8</math></p> <p><math>v_1 = 0.3</math> so <math>V_1 = 0.3</math><br/> <math>v_2 = -7.7</math> so <math>V_2 = 7.7</math> m s<sup>-1</sup><br/> in opposite to original direction</p> | M1<br>A1<br>M1<br>A1<br>A1<br>A1<br>F1 | PCLM and two terms on RHS<br>All correct. Any form.<br>NEL<br>Any form<br>Speed. Accept ±.<br>Must be correct interpretation of clear working | 7   |
| (ii)<br>(A) | $10 \times 0.5 = 30V$<br><br>so $V = \frac{1}{6}$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   | M1<br>A1<br>A1                         | PCLM and coalescence<br>All correct. Any form.<br>Clearly shown. Accept decimal equivalence. Accept no direction.                             | 3   |
| (B)         | Same velocity<br>No force on sledge in direction of motion                                                                                                                                                                                                                                                                                                                                                                                                                                                                          | E1<br>E1                               | Accept speed                                                                                                                                  | 2   |
| (iii)       |  <p>before</p> <p>2 m s<sup>-1</sup> → 2 m s<sup>-1</sup> →</p> <p>39.5 kg 0.5 kg</p> <p>after</p> <p>→ →</p> <p>V u</p> <p><math>2 \times 40 = 0.5u + 39.5V</math></p> <p><math>u - V = 10</math><br/>Hence <math>V = 1.875</math></p>                                                                                                                                                                                                          | B1<br>M1<br>A1<br>B1<br>A1             | PCLM, masses correct<br>Any form<br>May be seen on the diagram.<br>Accept no reference to direction.                                          | 5   |
|             |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     | 17                                     |                                                                                                                                               |     |

| Q 2                                                                                                                                                                                                                                                                                                                                                                                                                             | mark                                   | comment                                                                                                                                                                                                                                                                                                                                                                                                                | sub |
|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-----|
| (i) $X = R \cos 30$ (1)<br>$Y + R \sin 30 = L$ (2)                                                                                                                                                                                                                                                                                                                                                                              | B1<br>M1<br>A1                         | Attempt at resolution                                                                                                                                                                                                                                                                                                                                                                                                  | 3   |
| (ii) ac moments about A $R - 2L = 0$<br><br>Subst in (1) and (2)<br>$X = 2L \frac{\sqrt{3}}{2}$ so $X = \sqrt{3}L$<br><br>$Y + 2L \times \frac{1}{2} = L$ so $Y + L = L$ and $Y = 0$                                                                                                                                                                                                                                            | B1<br><br>M1<br>E1<br>E1               | Subst <b>their</b> $R = 2L$ into <b>their</b> (1) or (2)<br>Clearly shown<br>Clearly shown                                                                                                                                                                                                                                                                                                                             | 4   |
| (iii) (Below all are taken as tensions e. g. $T_{AB}$ in AB)                                                                                                                                                                                                                                                                                                                                                                    | B1<br>B1                               | Attempt at all forces (allow one omitted)<br>Correct. Accept internal forces set as tensions or thrusts or a mix                                                                                                                                                                                                                                                                                                       | 2   |
| (iv) $\downarrow$ A $T_{AD} \cos 30$ ( $-Y$ ) = 0<br><br>so $T_{AD} = 0$                                                                                                                                                                                                                                                                                                                                                        | M1<br>E1                               | Vert equilibrium at A attempted. $Y = 0$ need not be explicit                                                                                                                                                                                                                                                                                                                                                          | 2   |
| (v) Consider the equilibrium at pin-joints<br><br>A $\rightarrow$ $T_{AB} - X = 0$ so $T_{AB} = \sqrt{3}L$ (T)<br><br>C $\downarrow$ $L + T_{CE} \cos 30 = 0$<br>so $T_{CE} = \frac{-2L}{\sqrt{3}}$ so $\frac{2L}{\sqrt{3}} \left( = \frac{2L\sqrt{3}}{3} \right)$ (C)<br><br>C $\leftarrow$ $T_{BC} + T_{CE} \cos 60 = 0$<br>so $T_{BC} = - \left( -\frac{2\sqrt{3}L}{3} \right) \times \frac{1}{2} = \frac{\sqrt{3}L}{3}$ (T) | M1<br>B1<br>B1<br>B1<br>B1<br>B1<br>F1 | At least one relevant equilb attempted<br>(T) not required<br>Or equiv from <b>their</b> diagram<br>Accept any form following from <b>their</b> equation. (C) not required.<br>Or equiv from <b>their</b> diagram<br>FT <b>their</b> $T_{CE}$ or equiv but do not condone inconsistent signs even if right answer obtained. (T) not required.<br>T and C consistent with <b>their</b> answers and <b>their</b> diagram | 7   |
| (vi) $\downarrow$ B $T_{BD} \cos 30 + T_{BE} \cos 30 = 0$<br>so $T_{BD} = -T_{BE}$ so mag equal and opp sense                                                                                                                                                                                                                                                                                                                   | M1<br>E1                               | Resolve vert at B<br>A statement required                                                                                                                                                                                                                                                                                                                                                                              | 2   |
|                                                                                                                                                                                                                                                                                                                                                                                                                                 | 20                                     |                                                                                                                                                                                                                                                                                                                                                                                                                        |     |

| Q3    |                                                                                                                                                                                                                                                           | mark                             |                                                                                                                                                                                                                                                                                        | sub |
|-------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-----|
| (i)   | (10, 2, 2.5)                                                                                                                                                                                                                                              | B1                               |                                                                                                                                                                                                                                                                                        | 1   |
| (ii)  | By symmetry<br>$\bar{x} = 10,$<br>$\bar{y} = 2$<br>$(240 + 80)\bar{z} = 80 \times 0 + 240 \times 2.5$<br>so $\bar{z} = 1.875$                                                                                                                             | B1<br>B1<br>B1<br>M1<br>A1       | Total mass correct<br>Method for c.m.<br>Clearly shown                                                                                                                                                                                                                                 | 5   |
| (iii) | $\bar{x} = 10$ by symmetry<br>$(320 + 80) \begin{pmatrix} \bar{x} \\ \bar{y} \\ \bar{z} \end{pmatrix} = 320 \begin{pmatrix} 10 \\ 2 \\ 1.875 \end{pmatrix} + 80 \begin{pmatrix} 10 \\ 4 \\ 3 \end{pmatrix}$<br>$\bar{y} = 2.4$<br>$\bar{z} = 2.1$         | E1<br>M1<br>B1<br>B1<br>E1<br>E1 | Could be derived<br>Method for c.m.<br>y coord c.m. of lid<br>z coord c.m. of lid shown<br>shown                                                                                                                                                                                       | 6   |
| (iv)  |  <p>c.w moments about X<br/> <math>40 \times 0.024 \cos 30 - 40 \times 0.021 \sin 30</math><br/> <math>= 0.41138... \text{ so } 0.411 \text{ N m (3 s. f.)}</math></p> | B1<br>B1<br>E1                   | Award for correct use of dimensions 2.1 and 2.4 or equivalent<br><br>1 <sup>st</sup> term o.e. (allow use of 2.4 and 2.1)<br>2 <sup>nd</sup> term o.e. (allow use of 2.4 and 2.1)<br>Shown<br>[Perpendicular method: M1 Complete method:<br>A1 Correct lengths and angles<br>E1 Shown] | 4   |
| (v)   | $0.41138... - 0.05P = 0$<br>$P = 8.22768... \text{ so } 8.23 \text{ (3 s. f.)}$                                                                                                                                                                           | M1<br>A1                         | Allow use of 5<br>Allow if cm used consistently                                                                                                                                                                                                                                        | 2   |
|       |                                                                                                                                                                                                                                                           | 18                               |                                                                                                                                                                                                                                                                                        |     |

| Q 4         |                                                                                                                                                                                                                                                                                                                  | mark                                           |                                                                                                                                                                                                                                | sub |
|-------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------------------------------------------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-----|
| (i)         | $F_{\max} = \mu R$<br>$R = 2g \cos 30$<br>so $F_{\max} = 0.75 \times 2 \times 9.8 \times \cos 30 = 12.730\dots$<br>so 12.7 N (3 s. f.)<br><br><b>either</b><br>Weight cpt down plane is $2g \sin 30 = 9.8$ N<br>so no as $9.8 < 12.7$<br><b>or</b><br>Slides if $\mu < \tan 30$<br>But $0.75 > 0.577\dots$ so no | M1<br>B1<br>A1<br><br>B1<br>E1<br><br>B1<br>E1 | Must have attempt at $R$ with $mg$ resolved<br><br>[Award 2/3 retrospectively for limiting friction seen below]<br><br>The inequality must be properly justified<br><br>The inequality must be properly justified              | 5   |
| (ii)<br>(A) | Increase in GPE is<br>$2 \times 9.8 \times (6 + 4 \sin 30) = 156.8$ J                                                                                                                                                                                                                                            | M1<br>B1<br>A1                                 | Use of $mgh$<br>$6 + 4 \sin 30$                                                                                                                                                                                                | 3   |
| (B)         | WD against friction is<br>$4 \times 0.75 \times 2 \times 9.8 \times \cos 30 = 50.9222\dots$ J                                                                                                                                                                                                                    | M1<br>A1                                       | Use of $WD = Fd$                                                                                                                                                                                                               | 2   |
| (C)         | Power is $10 \times (156.8 + 50.9222\dots) / 60$<br>$= 34.620\dots$ so 34.6 W (3 s. f.)                                                                                                                                                                                                                          | M1<br>A1                                       | Use $P = WD/t$                                                                                                                                                                                                                 | 2   |
| (iii)       | $0.5 \times 2 \times 9^2$<br><br>$= 2 \times 9.8 \times (6 + x \sin 30)$<br>$+ 0.5 \times 2 \times 4^2$<br>$- 90$<br><br>so $x = 3.8163\dots$ so 3.82 (3 s. f.)                                                                                                                                                  | M1<br><br>B1<br>A1<br>A1<br>A1                 | Equating KE to GPE and WD term. Allow sign errors and one KE term omitted. Allow 'old' friction as well.<br><br>Both KE terms. Allow wrong signs.<br>All correct but allow sign errors<br>All correct, including signs.<br>cao | 5   |
|             |                                                                                                                                                                                                                                                                                                                  | 17                                             |                                                                                                                                                                                                                                |     |