



Please write clearly in block capitals.

Centre number

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Candidate number

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Surname

Forename(s)

Candidate signature

A-level MATHEMATICS

Unit Mechanics 2B

Monday 27 June 2016

Morning

Time allowed: 1 hour 30 minutes

Materials

For this paper you must have:

- the blue AQA booklet of formulae and statistical tables.

You may use a graphics calculator.

Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- Write the question part reference (eg (a), (b)(i) etc) in the left-hand margin.
- You must answer each question in the space provided for that question. If you require extra space, use an AQA supplementary answer book; do **not** use the space provided for a different question.
- Do not write outside the box around each page.
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work that you do not want to be marked.
- The **final** answer to questions requiring the use of calculators should be given to three significant figures, unless stated otherwise.
- Take $g = 9.8 \text{ m s}^{-2}$, unless stated otherwise.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 75.

Advice

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
- You do not necessarily need to use all the space provided.



J U N 1 6 M M 2 B 0 1

PB/Jun16/E3

MM2B

Answer **all** questions.

Answer each question in the space provided for that question.

1 A stone, of mass 0.3 kg , is thrown with a speed of 8 m s^{-1} from a point at a height of 5 metres above a horizontal surface.

(a) Calculate the initial kinetic energy of the stone. **[2 marks]**

(b) (i) Find the kinetic energy of the stone when it hits the surface. **[3 marks]**

(ii) Hence find the speed of the stone when it hits the surface. **[2 marks]**

(iii) State one modelling assumption that you have made. **[1 mark]**

QUESTION
PART
REFERENCE

Answer space for question 1



2 A particle moves in a horizontal plane under the action of a single force, \mathbf{F} newtons.

The unit vectors \mathbf{i} and \mathbf{j} are directed east and north respectively.

At time t seconds, the velocity of the particle, $\mathbf{v} \text{ m s}^{-1}$, is given by

$$\mathbf{v} = (8t - t^4)\mathbf{i} + 6e^{-3t}\mathbf{j}$$

(a) Find an expression for the acceleration of the particle at time t . **[2 marks]**

(b) The mass of the particle is 2 kg.

(i) Find an expression for the force \mathbf{F} acting on the particle at time t . **[2 marks]**

(ii) Find the magnitude of \mathbf{F} when $t = 1$. **[3 marks]**

(c) Find the value of t when \mathbf{F} acts due south. **[2 marks]**

(d) When $t = 0$, the particle is at the point with position vector $(3\mathbf{i} - 5\mathbf{j})$ metres.

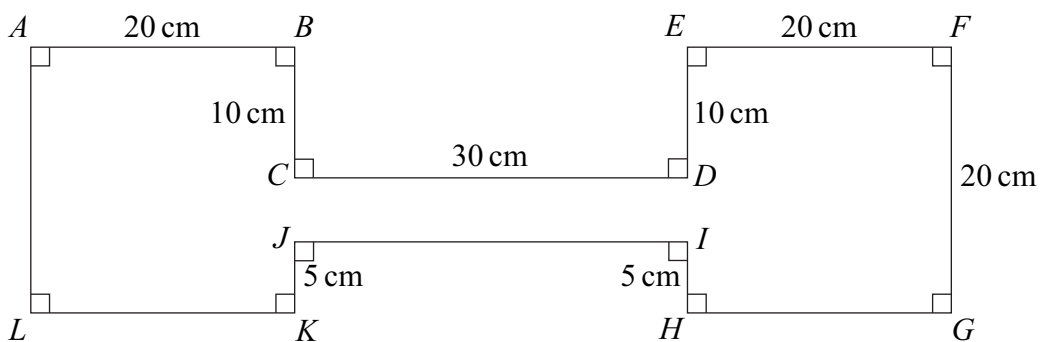
Find an expression for the position vector, \mathbf{r} metres, of the particle at time t . **[4 marks]**

QUESTION
PART
REFERENCE

Answer space for question 2



3 The diagram shows a uniform lamina $ABCDEFGHIJKL$.



- (a) Explain why the centre of mass of the lamina is 35 cm from AL . [1 mark]
- (b) Find the distance of the centre of mass from AF . [4 marks]
- (c) The lamina is freely suspended from A .
Find the angle between AB and the vertical when the lamina is in equilibrium. [3 marks]
- (d) Explain, briefly, how you have used the fact that the lamina is uniform. [1 mark]

QUESTION
PART
REFERENCE

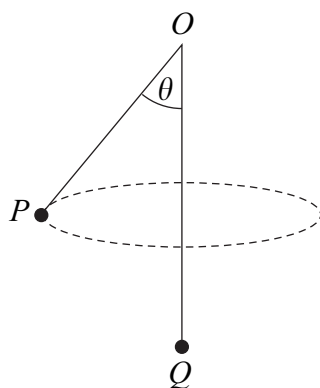
Answer space for question 3



- 4 A particle P , of mass 6 kg , is attached to one end of a light inextensible string. The string passes through a small smooth ring, fixed at a point O . A second particle Q , of mass 8 kg , is attached to the other end of the string.

The particle Q hangs at rest vertically below the ring, and the particle P moves with speed 5 m s^{-1} in a horizontal circle, as shown in the diagram.

The angle between OP and the vertical is θ .



- (a) Find the tension in the string. [1 mark]
- (b) Find θ . [3 marks]
- (c) Find the radius of the horizontal circle. [4 marks]

QUESTION
PART
REFERENCE

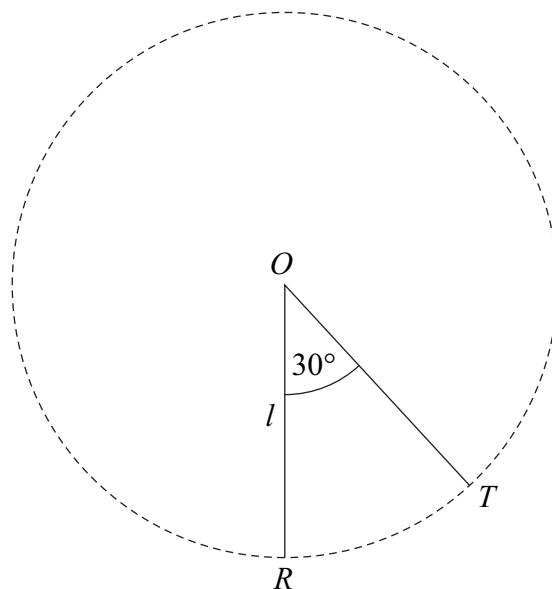
Answer space for question 4



5 A particle of mass m is suspended from a fixed point O by a light inextensible string of length l . The particle hangs in equilibrium at the point R vertically below O .

The particle is set into motion with a horizontal velocity u so that it moves in a complete vertical circle with centre O .

The point T on the circle is such that angle ROT is 30° , as shown in the diagram.



- (a) Find, in terms of g , l and u , the speed of the particle at the point T . [3 marks]
- (b) Find, in terms of g , l , m and u , the tension in the string when the particle is at the point T . [3 marks]
- (c) Find, in terms of g , l , m and u , the tension in the string when the particle returns to the point R . [2 marks]
- (d) The particle makes complete revolutions.
Find, in terms of g and l , the minimum value of u . [4 marks]

QUESTION
PART
REFERENCE

Answer space for question 5



6 A stone, of mass m , falls vertically downwards under gravity through still water. At time t , the stone has speed v and it experiences a resistance force of magnitude λmv , where λ is a constant.

(a) Show that

$$\frac{dv}{dt} = g - \lambda v$$

[2 marks]

(b) The initial speed of the stone is u .

Find an expression for v at time t .

[6 marks]

QUESTION
PART
REFERENCE

Answer space for question 6



7 A uniform ladder, of weight W , rests with its top against a rough vertical wall and its base on rough horizontal ground.

The coefficient of friction between the wall and the ladder is μ and the coefficient of friction between the ground and the ladder is 2μ .

When the ladder is on the point of slipping, the ladder is inclined at an angle of θ to the horizontal.

(a) Draw a diagram to show the forces acting on the ladder.

[2 marks]

(b) Find $\tan \theta$ in terms of μ .

[7 marks]

QUESTION
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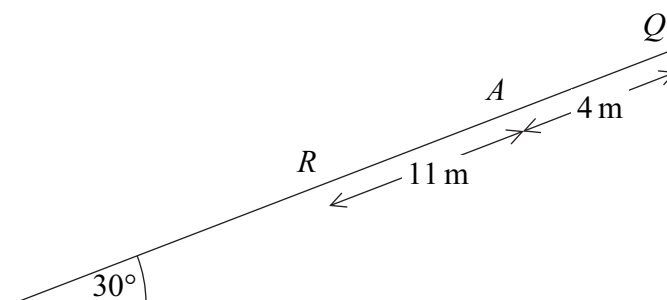
Answer space for question 7



8 A particle, P , of mass 5 kg is placed at the point A on a rough plane which is inclined at 30° to the horizontal.

The points Q and R are also on the surface of the inclined plane, with $QR = 15$ metres. The point A is between Q and R so that $AQ = 4$ metres and $AR = 11$ metres.

The three points Q , A and R are on a line of greatest slope of the plane.



The particle is attached to two light elastic strings, PQ and PR .

One of the strings, PQ , has natural length 4 metres and modulus of elasticity 160 N, the other string, PR , has natural length 6 metres and modulus of elasticity 120 N.

The particle is released from rest at the point A .

The coefficient of friction between the particle and the plane is 0.4 .

Find the distance of the particle from Q when it is next at rest.

[8 marks]

QUESTION
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Answer space for question 8



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