

General Certificate of Education June 2010

Mathematics

MM2B

Mechanics 2B

Mark Scheme

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Key to mark scheme and abbreviations used in marking

M	mark is for method			
m or dM	mark is dependent on one or more M marks and is for method			
A	mark is dependent on M or m marks and is for accuracy			
В	mark is independent of M or m marks and is for method and accuracy			
Е	mark is for explanation			
\checkmark or ft or F	follow through from previous			
	incorrect result	MC	mis-copy	
CAO	correct answer only	MR	mis-read	
CSO	correct solution only	RA	required accuracy	
AWFW	anything which falls within	FW	further work	
AWRT	anything which rounds to	ISW	ignore subsequent work	
ACF	any correct form	FIW	from incorrect work	
AG	answer given	BOD	given benefit of doubt	
SC	special case	WR	work replaced by candidate	
OE	or equivalent	FB	formulae book	
A2,1	2 or 1 (or 0) accuracy marks	NOS	not on scheme	
−x EE	deduct x marks for each error	G	graph	
NMS	no method shown	c	candidate	
PI	possibly implied	sf	significant figure(s)	
SCA	substantially correct approach	dp	decimal place(s)	

No Method Shown

Where the question specifically requires a particular method to be used, we must usually see evidence of use of this method for any marks to be awarded. However, there are situations in some units where part marks would be appropriate, particularly when similar techniques are involved. Your Principal Examiner will alert you to these and details will be provided on the mark scheme.

Where the answer can be reasonably obtained without showing working and it is very unlikely that the correct answer can be obtained by using an incorrect method, we must award **full marks**. However, the obvious penalty to candidates showing no working is that incorrect answers, however close, earn **no marks**.

Where a question asks the candidate to state or write down a result, no method need be shown for full marks.

Where the permitted calculator has functions which reasonably allow the solution of the question directly, the correct answer without working earns **full marks**, unless it is given to less than the degree of accuracy accepted in the mark scheme, when it gains **no marks**.

Otherwise we require evidence of a correct method for any marks to be awarded.

MM2B

Q	Solution	Marks	Total	Comments
1	$v = \frac{\mathrm{d}s}{\mathrm{d}t}$	N/1		M1 for either $\frac{ds}{dt}$ or 1 of 2 terms correct
	di	M1		(ignore signs)
	$= 10t - 12\sin 4t$	A1A1	3	(ignore signs)
	Total		3	
2(a)	Kinetic energy = $\frac{1}{2} \times 3 \times 4^2$	M1		
	= 24 (J)	A1	2	
(b)	PE lost is $= 3 \times g \times 51$	M1		
	= 153g or 1499.4 = 1500 J	A1	2	Accept 1499, 153g
(c)(i)	KE is $24 + 153g$ = 1523.4	M1		M1 '(a)' + '(b)'
	= 1520 J	A1		(if done (c)(i) in (b) 0 marks; if done (b) and then (c)(i) in (b) M1 only)
(ii)	Using KE = $\frac{1}{2}mv^2$			
	$v^2 = 1015.6$	M1		
	Speed of stone is 31.9 ms ⁻¹	A1	4	Accept 31.8 from 1520
				If use constant acceleration formulae in 2D, possible 4 marks in (c) BUT no marks if initial speed is treated as being vertical
(d)	eg Stone is a particle	E1	1	
,	No air resistance			Not no resistance; accept no wind resistance
	Total		9	
3(a)	Symmetry	E1	1	Only accept 'symmetry'
(b)	Moments about <i>B</i> : $0.4 \times 4 + 0.1 \times 8 = 0.5 \times \overline{x}$	M1A1		M1 3 terms, 2 correct
	$\overline{x} = \frac{2.4}{0.5}$			
	= 4.8 cm	A1	3	
	Total		4	

MM2B (cont)

Q Q	Solution	Marks	Total	Comments
4(a)	Using $\mathbf{F} = m\mathbf{a}$,	14161179	Total	Comments
I (u)	$400\cos\frac{\pi}{2} \ t \ \mathbf{i} + 600t^2 \ \mathbf{j} = 200 \ \mathbf{a}$	M1		
	$\mathbf{a} = 2\cos\frac{\pi}{2} t \mathbf{i} + 3t^2 \mathbf{j}$	A1	2	
(b)	$\mathbf{v} = \int a dt$	M1		M1 for either $\int a dt$ or 1 of 2 terms correct
	$\mathbf{v} = \int a dt$ $= \frac{4}{\pi} \sin \frac{\pi}{2} t \mathbf{i} + t^3 \mathbf{j} + \mathbf{c}$	A1m1		m1 for + \mathbf{c}
	When $t = 4$, $\mathbf{r} = -3\mathbf{i} + 56\mathbf{j}$, $64\mathbf{j} + \mathbf{c} = -3\mathbf{i} + 56\mathbf{j}$	m1		
	$\mathbf{c} = -3\mathbf{i} - 8\mathbf{j}$ $\mathbf{v} = (\frac{4}{\pi}\sin\frac{\pi}{2}t - 3)\mathbf{i} + (t^3 - 8)\mathbf{j}$	A1	5	Do not accept $\frac{2}{\frac{\pi}{2}}$ Accept 1.27 for $\frac{4}{\pi}$
(c)	When particle is moving due west, northerly component is zero $\therefore t^3 - 8 = 0$	M1 A1√		
	t = 2	A1	3	
(d)	When $t = 2$, $\mathbf{v} = -3\mathbf{i} + 0\mathbf{j}$ Speed of particle is 3 m s ⁻¹	B1√ B1	2	B1 for change –3 to +3
	Total		12	
5		M1		
	$\frac{\mathrm{d}v}{\mathrm{d}t} = -\frac{\lambda}{v^{\frac{1}{4}}}$ $\int v^{\frac{1}{4}} \mathrm{d}v = -\int \lambda \mathrm{d}t$	m1		Condone one of $v^{-\frac{1}{4}}$, $+\int \lambda dt$, $\frac{1}{\lambda}$
	$\frac{4}{5}v^{\frac{5}{4}} = -\lambda t + c$ $t = 0, \ v = u \ \therefore \ c = \frac{4}{5}u^{\frac{5}{4}}$	A1A1 m1		$m1 ext{ for } + c$
	$t = 0, v = u :: c = \frac{4}{5}u^{\frac{5}{4}}$	A1		
	$\therefore v^{\frac{5}{4}} = u^{\frac{5}{4}} - \frac{5}{4}\lambda t$			
	$v = \left(u^{\frac{5}{4}} - \frac{5}{4}\lambda t\right)^{\frac{4}{5}}$ $v = \left(u^{\frac{5}{4}} - \frac{5}{4}\lambda t\right)^{\frac{4}{5}}$	A1	7	
	Total		7	

MM2B (cont)

Q Q	Solution	Marks	Total	Comments
6(a)	Using power = force \times velocity			
	$Power = (30 \times 48) \times 48$	M1		
	= 69120 watts	A1	2	AG
(b)	When speed is 40 m s ⁻¹ ,			
	max force exerted is $\frac{69120}{40}$			
	= 1728 N	B1		
	Accelerating force is '1728' – 1200 N	M1		
	Using $F = ma$:	1,11		
	528 = 1200a	m1		
	$a = 0.44 \text{ m s}^{-2}$	A1	4	
(c)	Force exerted by engine is $\frac{69120}{v}$	B1		
	Force exerted by the engine $= 30v - mg \sin 3$	M1		(Use of cos3 delete A1,A1 of 3 A terms)
	$30v - 615.47$ (or $1200g\sin 3$)= $\frac{69120}{v}$	A1A1		A2 All terms correct A1 Two terms correct
	$30v^2 - 615.47v - 69120 = 0$	A1		SC3 for $30v^2 + 615.47v - 69120 = 0$
	$v = \frac{615.47 \pm \sqrt{615.47^2 + 4 \times 30 \times 69120}}{20.000}$	M1		
	2×30 Speed is 59.3 m s ⁻¹	A1	7	
	Total		13	
7(a)	R F			
	† _ ▼	В2	2	D1 for C and C (in connect alone)
		D2	2	B1 for <i>S</i> and 6 <i>g</i> (in correct place) B1 for <i>R</i> and <i>F</i> or combined vertical force
	s			at C
	\uparrow \downarrow			
	6g			
(b)	Moments about <i>C</i> :			
	$3 \times S \times \cos 20 = 6g \times 1 \times \cos 20$	M1A1		M1 2 terms, 1 term correct
	S = 19.6 N or 2g	A1	3	
				R, F not correct 0 marks in (c)(i) and
(c)(i)	Moments about A:			(c)(ii) Or
(C)(1)	$2 \times 6g \times \cos 20 = R \times 3$	M1A1		Moments about mid-point of rod:
	R = 36.8 N	A1		$2 \times S \times \cos 20 = P \times 1 \times \cos 20$
	(or resolving, $R = 6g \cos 20 - S \cos 20$			P = 39.2 N or 4g
	$=4g\cos 20)$			(Or resolving vertically $P = 4g$)
(ii)	Resolve parallel to AB :	3.61		$R = P \times \cos 20$ M1 A1
	$S \cos 70 + F = 6g \cos 70$	M1		$= 36.8 \text{ N} \qquad \qquad \text{A1}$ $E = R \times \sin 20 \qquad \qquad \text{M1}$
	$F = 4g\cos 70$ $= 13.4 \text{ N}$	A1	5	$F = P \times \sin 20$ M1 = 13.4 N A1
	-13.4 N (or $F = 6g \sin 20 - S \sin 20 = 4g \sin 20$)	AI	3	-13.71V A1
(d)	Using $F = \mu R$:	M1		M1 '(c)(ii)' = μ '(c)(i)'
	$13.4 = \mu \times 36.8$			
	$\mu = 0.364$ or tan 20	A1√	2	(condone ≥)
	Total		12	

MM2B (cont)

Q Q	Solution	Marks	Total	Comments
8(a)	Using conservation of energy:			
	$\frac{1}{2}mv^2 = 3mg(1-\cos\theta)$	M1A1		$M1 \frac{1}{2} mv^2 = mgh$
	$v^2 = 6g(1 - \cos 15)$	m1		
	$v = (6g[1 - \cos 15])^{\frac{1}{2}}$			
	= 1.42	A1	4	SC3: 1.41
(b)	When particle is at rest,			2
	resolve radially $T = mg \cos 15$	M1A1		M1 $T - mg \cos 15 = \frac{mv^2}{r}$ or $T = mg \sin 15$
	$22 = mg \cos 15$			
	m = 2.32 Total	A1	<u>3</u>	
	_			or
9	As particle moves, $T = \frac{mv^2}{r}$	M1		using unknown as extension:
	If radius is r , extension is $r - 1.2$	B1		If extension is x , radius is $1.2 + x$ B1
	Using $T = \frac{\lambda x}{l}$:			Using $T = \frac{\lambda x}{l}$:
	$T = \frac{192(r-1.2)}{1.2}$	M1		$T = \frac{192x}{1.2}$ M1
	= 160(r - 1.2)	A1		= 160x A1
	$= 160(r - 1.2)$ $T = \frac{mv^{2}}{r} \Rightarrow 160(r - 1.2) = \frac{8 \times 3^{2}}{r}$	M1		$T = \frac{mv^2}{r} \Rightarrow 160x = \frac{8 \times 3^2}{1.2 + x}$ M1
				M1
	$160r^{2} - 192r = 72$ (or $192r^{2} - 230.4r = 86.4$)	A1		$192x + 160x^2 = 72$ A1
	$(01192r - 250.4r = 80.4)$ $20r^2 - 24r - 9 = 0$			$20x^2 + 24x - 9 = 0$
	(10r+3)(2r-3) = 0	M1		(10x-3)(2x+3) = 0 M1
	r = 1.5 or -0.3			x = 0.3 or -1.5
	Radius is 1.5	A1	8	Radius is 1.5 A1
	Total		8	
	TOTAL		75	