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General Certificate of Education

Mathematics 6360

MM2B Mechanics 2B

Mark Scheme

2009 examination - June series

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation meeting attended by all examiners and is the scheme which was used by them in this examination. The standardisation meeting ensures that the mark scheme covers the candidates' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for the standardisation meeting each examiner analyses a number of candidates' scripts: alternative answers not already covered by the mark scheme are discussed at the meeting and legislated for. If, after this meeting, examiners encounter unusual answers which have not been discussed at the meeting they are required to refer these to the Principal Examiner.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of candidates' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

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Key to mark scheme and abbreviations used in marking

M	mark is for method
m or dM	mark is dependent on one or more M marks and is for method
A	mark is dependent on M or m marks and is for accuracy
B	mark is independent of M or m marks and is for method and accuracy
E	mark is for explanation

√or ft or F	follow through from previous incorrect result	MC	mis-copy
CAO	correct answer only	MR	mis-read
CSO	correct solution only	RA	required accuracy
AWFW	anything which falls within	FW	further work
AWRT	anything which rounds to	ISW	ignore subsequent work
ACF	any correct form	FIW	from incorrect work
AG	answer given	BOD	given benefit of doubt
SC	special case	WR	work replaced by candidate
OE	or equivalent	FB	formulae book
A2,1	2 or 1 (or 0) accuracy marks	NOS	not on scheme
–*x* EE	deduct *x* marks for each error	G	graph
NMS	no method shown	c	candidate
PI	possibly implied	sf	significant figure(s)
SCA	substantially correct approach	dp	decimal place(s)

No Method Shown

Where the question specifically requires a particular method to be used, we must usually see evidence of use of this method for any marks to be awarded. However, there are situations in some units where part marks would be appropriate, particularly when similar techniques are involved. Your Principal Examiner will alert you to these and details will be provided on the mark scheme.

Where the answer can be reasonably obtained without showing working and it is very unlikely that the correct answer can be obtained by using an incorrect method, we must award **full marks**. However, the obvious penalty to candidates showing no working is that incorrect answers, however close, earn **no marks**.

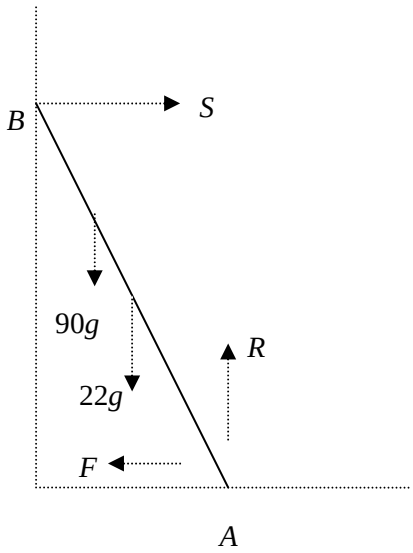
Where a question asks the candidate to state or write down a result, no method need be shown for full marks.

Where the permitted calculator has functions which reasonably allow the solution of the question directly, the correct answer without working earns **full marks**, unless it is given to less than the degree of accuracy accepted in the mark scheme, when it gains **no marks**.

Otherwise we require evidence of a correct method for any marks to be awarded.

Q	Solution	Marks	Total	Comments
1(a)	$\mathbf{a} = \frac{d\mathbf{v}}{dt} = (3t^2 - 15)\mathbf{i} + (6 - 2t)\mathbf{j}$	M1A1 A1	3	A1 (**i** terms) A1 (**j** terms)
(b)(i)	Using $\mathbf{F} = m\mathbf{a}$: Force $= 4 \times \{(3t^2 - 15)\mathbf{i} + (6 - 2t)\mathbf{j}\}$ $= (12t^2 - 60)\mathbf{i} + (24 - 8t)\mathbf{j}$	 M1 A1	 2	 AG
(ii)	When $t = 2$, force $= -12\mathbf{i} + 8\mathbf{j}$ Magnitude of force $= \sqrt{12^2 + 8^2}$ N $= 14.4$ (N)	M1A1 M1 A1	 4	
	Total		**9**	
2(a)	KE $= \frac{1}{2} \times 55 \times 3^2$ $= 247.5$ J	M1 A1	 2	
(b)	Change in PE as slides down: $mgh = 55 \times 9.8 \times 20 \cos 30$ $= 9335.7\ldots$ Using Conservation of Energy: KE at end of slide $= 247.5 + 9335.7$ $= 9580$ J Speed of Anne is $\sqrt{\frac{9583}{\frac{1}{2} \times 55}}$ $= 18.7$ m s^{-1}	 M1 A1 m1 A1 m1 A1	 6	 Need cos 30 or sin 30 ‘a’ + ‘9335.7’ accept 9583
(c)	Anne is a particle; no air resistance	E1	1	
	Total		**9**	

MM2B (cont)

Q	Solution	Marks	Total	Comments
3(a)				
	Resolve vertically: $R = 22g + 90g$ $= 112g$	B1		
	Using $F = \mu R$: $F = 0.6R$ $F = 0.6 \times 112g$	M1 A1		[Needs $0.6\times112g$ or 0.6×1097.6 NOT 0.6×1097 unless 658.56 seen]
	$= 67.2g$ or 658.56 $F = 659$ N	A1	4	AG (659 must be shown from correct working)
(b)	Resolve horizontally: $S = F$	B1		
	Moments about A: $90g \times 5 \times \cos\theta + 22g \times 3 \times \cos\theta$	M1A1		M1 (one term, force × distance × cos or sin)
	$= 67.2g \times 6 \times \sin\theta$ $450g + 66g = 403.2g \tan\theta$ $\tan\theta = \frac{516}{403.2}$	A1		
	$\theta = 52.0°$	A1	5	accept 52 **Alternative**: or moments about B: M1 A2, 1 or 0 for four-term moment equation + M1 for rearranging etc (dep on 4 term) + A1 for answer
	Total		**9**	

MM2B (cont)

Q	Solution	Marks	Total	Comments
4(a)	Resolving vertically:			
	$T\cos 60 + T\cos 40 = mg$	M1A1		
	$1.266\,T = 6g$	M1		
	$T = 46.4$ N	A1	4	AG no marks if g deleted
(b)	Radius of circle is $0.6\tan 60$	B1		$r = 1.039$ or 1.04
	Horizontally:			
	$\frac{mv^2}{r} = T\cos 50 + T\cos 30$	M1		Accept sin instead of cos for M1
	$\frac{6v^2}{1.039} = 46.4\cos 50 + 46.4\cos 30$ or 70.01	A1		
	$v^2 = 12.123$			
	Speed is 3.48 m s^{-1}	A1	4	
	Total		**8**	
5	Force acting against gravity is $mg\sin\theta$	M1		Or 147000
	Force acting against gravity and resistance is $mg\sin\theta + 200\,000$	m1		200 000 + 'mg sin θ'
	$= 600\,000g\sin\theta + 200\,000$			
	$= 347\,000$	A1		
	Using power = force × velocity	M1		
	= 347000 × 24	A1F		
	= 8330 kW	A1	6	
	Total		**6**	
6(a)	$\text{EPE} = \frac{\lambda x^2}{2l}$			
	$= \frac{180\times 0.8^2}{2\times 1.2}$	M1		
	= 48 J	A1	2	
(b)	Using initial EPE = KE when string becomes slack:	M1		
	$48 = \frac{1}{2}\times 5\times v^2$	A1F		
	$v = \sqrt{\frac{96}{5}}$			
	= 4.38 m s^{-1}	A1F	3	ft $\sqrt{\frac{'a'}{2.5}}$
(c)	Normal reaction is $5g$ or 49	M1		
	Frictional force is $5g\times\mu$	m1A1		
	Work done by frictional force is $5\mu g\times 2$	m1		
	$= 10\mu g$	A1		
	Stops at wall $\Rightarrow 10\mu g = 48$	m1		m1 $10\mu g = 'a'$
	$\mu = 0.490$	A1	7	accept $\frac{24}{49}$ OE
	Total		**12**	

MM2B (cont)

Q	Solution	Marks	Total	Comments
7(a)	By conservation of energy to point where *QP* makes an angle θ with upward vertical:			
	$\frac{1}{2}mv^2 = \frac{1}{2}mu^2 - mga(1+\sin\theta)$	M1 A1		for 3 terms, 2 KE and 1 PE $mga\ (1+\sin\theta)$ term
	$v^2 = u^2 - 2ag(1+\sin\theta)$	A1		
	Resolve radially			
	$R = \frac{mv^2}{a} - mg\sin\theta$	M1A1		M1 for 3 terms, include $\sin\theta$ or $\cos\theta$
	$= \frac{mu^2}{a} - 3mg\sin\theta - 2mg$	A1	6	AG
(b)	When particle leaves the track, $R = 0$	M1		
	$0 = 3mg - 3mg\sin\theta - 2mg$	A1		
	$\sin\theta = \frac{1}{3}$	M1		SC3 $\sin^{-1}\frac{1}{3}$
	θ = 19.5°	A1	4	accept 19.4° or $\theta = 0.340^c$
	Total		**10**	
8(a)	Using $F = ma$:			
	$-\lambda m v^{\frac{3}{2}} = m\frac{dv}{dt}$	M1		
	$\therefore \frac{dv}{dt} = -\lambda v^{\frac{3}{2}}$	A1	2	AG
(b)	$\int \frac{dv}{v^{\frac{3}{2}}} = -\lambda\int dt$	M1		
	$-\frac{2}{v^{\frac{1}{2}}} = -\lambda t + c$	A1		Condone no '+c'
	When $t = 0$, $v = 9 \Rightarrow c = -\frac{2}{3}$	M1 A1		Dep. on correct integration (accept sign or '$\frac{1}{2}$' error)
	$\frac{2}{\sqrt{v}} = \lambda t + \frac{2}{3}$	A1		
	$\frac{\sqrt{v}}{2} = \frac{1}{\lambda t + \frac{2}{3}}$			
	$v = \left(\frac{6}{2+3\lambda t}\right)^2$	m1		Needs correct algebra
	$v = \frac{36}{(2+3\lambda t)^2}$	A1	7	AG
(c)	When $v = 4$,			**or** $\frac{36}{(2+3\lambda t)^2} = 4$ M1
	$\frac{2}{\sqrt{v}} = \lambda t + \frac{2}{3} \Rightarrow 1 = \lambda t + \frac{2}{3}$	M1A1		$(2+3\lambda t)^2 = 9$ A1
	$t = \frac{1}{3\lambda}$	A1	3	$t = \frac{1}{3\lambda}$ A1 needs statement why $2+3\lambda t \neq -3$
	Total		**12**	
	TOTAL		**75**	