

1		Mark	Comment	
(i)	<p>Hor <math>21t = 60</math></p> <p>so <math>\frac{20}{7}</math> s (2.8571...)</p> <p><b>either</b> <math>0 = u - 9.8 \times \frac{20}{7}</math></p> <p><b>or</b> <math>-u = u - 9.8 \times \left(\frac{40}{7}\right)</math></p> <p><b>or</b> <math>40 = u \times \frac{20}{7} - 4.9 \left(\frac{20}{7}\right)^2</math></p> <p>so <math>u = 28</math> so <math>28 \text{ m s}^{-1}</math></p>	<p>M1</p> <p>A1</p> <p>M1</p> <p>E1</p>	<p>Use of horizontal components and <math>a = 0</math> or <math>s = vt - 0.5at^2</math> with <math>v = 0</math>.</p> <p>Any form acceptable. Allow M1 A1 for answer seen WW.</p> <p>[If <math>s = ut + 0.5at^2</math> and <math>u = 0</math> used without justification award M1 A0]</p> <p>[If <math>u = 28</math> assumed to find time then award SC1]</p> <p>Use of <math>v = u + at</math> (or <math>v^2 = u^2 + 2as</math>) with <math>v = 0</math>.</p> <p><b>or</b> Use of <math>v = u + at</math> with <math>v = -u</math> and appropriate <math>t</math>.</p> <p><b>or</b> Use of <math>s = ut + 0.5at^2</math> with <math>s = 40</math> and appropriate <math>t</math></p> <p>Condone sign errors and, where appropriate, <math>u \leftrightarrow v</math>.</p> <p>Accept signs not clear but not errors.</p> <p>Enough working must be given for 28 to be properly shown.</p> <p>[NB <math>u = 28</math> may be found first and used to find time]</p>	4
(ii)	$y = 28t - 0.5 \times 9.8t^2$	E1	<p><i>Clear &amp; convincing</i> use of <math>g = -9.8</math> in <math>s = ut + 0.5at^2</math> or <math>s = vt - 0.5at^2</math> <b>NB: AG</b></p>	1
(iii)	<p>Start from same height with same (zero) vertical speed at same time, same acceleration</p> <p>Distance apart is <math>0.75 \times 21t = 15.75t</math></p>	<p>E1</p> <p>M1</p> <p>A1</p>	<p>For two of these reasons</p> <p><math>0.75 \times 21t</math> seen <b>or</b> <math>21t</math> and <math>5.25t</math> both seen with intention to subtract.</p> <p>Need simplification - LHS alone insufficient. CWO.</p>	3
(iv) (A)	<p><b>either</b> Time is <math>\frac{20}{7}</math> s by symmetry so <math>15.75 \times \frac{20}{7} = 45</math> so 45 m</p> <p><b>or</b> Hit ground at same time. By symmetry one travels 60 m so the other travels 15 m in this time (<math>\frac{1}{4}</math> speed) so 45 m.</p>	<p>B1</p> <p>B1</p> <p>B1</p> <p>B1</p>	<p>Symmetr or <math>uvast</math></p> <p>FT their (iii) with <math>t = \frac{20}{7}</math></p> <p>[SC1 if 90 m seen]</p>	2
(B)	see next page			

1	continued			
(B)	<p><b>either</b> Time to fall is <math>40 - 10 = 0.5 \times 9.8 \times t^2</math></p> <p><math>t = 2.47435\dots</math> need <math>15.75 \times 2.47435\dots = 38.971\dots</math> so 39.0 (3sf)</p> <p><b>or</b> Need time so <math>10 = 28t - 4.9t^2</math></p> <p><math>4.9t^2 - 28t + 10 = 0</math></p> <p>so <math>t = \frac{28 \pm \sqrt{28^2 - 4 \times 4.9 \times 10}}{9.8}</math> so 0.382784... or 5.33150...</p> <p>Time required is 5.33150... <math>-\frac{20}{7} =</math> 2.47435.. need <math>15.75 \times 2.47435\dots = 38.971\dots</math> so 39.0 (3sf)</p>	<p>M1</p> <p>A1</p> <p>A1</p> <p>A1</p> <p>F1</p> <p>M1</p> <p>M1*</p> <p>A1</p> <p>M1</p> <p>F1</p>	<p>[SC1 if <b>either</b> and <b>or</b> methods mixed to give <math>\pm 30 = 28t - 4.9t^2</math> or <math>\pm 10 = 4.9t^2</math> ]</p> <p>Considering time from explosion with <math>u = 0</math>. Condone sign errors.</p> <p>LHS. Allow <math>\pm 30</math></p> <p>All correct</p> <p>cao</p> <p>FT <b>their</b> (iii) only.</p> <p>Equating <math>28t - 4.9t^2 = \pm 10</math> Dep. Attempt to solve quadratic by a method that could give two roots.</p> <p>Larger root correct to at least 2 s. f. Both method marks may be implied from two correct roots alone (to at least 1 s. f.). [SC1 for either root seen WW]</p> <p>FT <b>their</b> (iii) only.</p>	5
(v)	<p>Horiz (<math>x =</math>) <math>21t</math> Elim <math>t</math> between <math>x = 21t</math> and <math>y = 28t - 4.9t^2</math></p> <p>so <math>y = 28\left(\frac{x}{21}\right) - 4.9\left(\frac{x}{21}\right)^2</math></p> <p>so <math>y = \frac{4x}{3} - \frac{0.1x^2}{9} = \frac{1}{90}(120x - x^2)</math></p>	<p>B1</p> <p>M1</p> <p>A1</p> <p>E1</p>	<p>Intention must be clear, with some attempt made.</p> <p><math>t</math> completely and correctly eliminated from their expression for <math>x</math> and correct <math>y</math>. Only accept wrong notation if subsequently explicitly given correct value e.g <math>\frac{x^2}{21}</math> seen as <math>\frac{x^2}{441}</math>.</p> <p>Some simplification must be shown.</p> <p>[SC2 for 3 points shown to be on the curve. Award more only if it is made clear that (a) trajectory is a parabola (b) 3 points define a parabola]</p>	4
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2		mark		sub
(i)	Using $s = ut + 0.5at^2$ with $u = 10$ and $a = -10$	E1	Must be clear evidence of derivation of $-5$ . Accept one calculation and no statement about the other.	1
(ii)	<b>either</b> $s = 0$ gives $10t - 5t^2 = 0$ so $5t(2 - t) = 0$ so $t = 0$ or $2$ . Clearly need $t = 2$ <b>or</b> Time to highest point is given by $0 = 10 - 10t$ Time of flight is $2 \times 1 = 2$ s  horizontal range is $40$ m as $40 < 70$ , hits the ground	B1 M1 A1  M1 M1 A1  B1 E1	Factorising Award 3 marks for $t = 2$ seen WWW  Dep on 1 <sup>st</sup> M1. Doubling <b>their</b> $t$ . Properly obtained  FT $20 \times$ <b>their</b> $t$ Must be clear. FT <b>their</b> range.	5
(iii)	need $10t - 5t^2 = -15$ Solving $t^2 - 2t - 3 = 0$  so $(t - 3)(t + 1) = 0$ and $t = 3$  range is $60$ m	M1 M1 A1  M1 A1	[May divide flight into two parts] Equate $s = -15$ or equivalent. Allow use of $\pm 15$ . Method leading to solution of a quadratic. Equivalent form will do. Obtaining $t = 3$ . Allow no reference to the other root. [Award SC3 if $t = 3$ seen WWW] Range is $20 \times$ <b>their</b> $t$ ( provided $t > 0$ ) cao. CWO.	5
(iv)	Using (ii) & (iii), since $40 + 60 > 70$ , paths cross (For $0 < t \leq 2$ ) both have same vertical motion so B is always $15$ m above A	E1  E1	Must be convincing. Accept sketches.  Do not accept evaluation at one or more points alone. That B is <i>always</i> above A must be clear.	2
(v)	Need x components summing to $70$ $20 \times 0.75 + 20 \times 2.75 = 15 + 55 = 70$ so true  Need y components the same  $10 \times 2.75 - 5 \times 2.75^2 + 15 = 4.6875$  $10 \times 0.75 - 5 \times 0.75^2 = 4.6875$	M1 E1  M1 B1 E1	May be implied. Or correct derivation of $0.75$ s or $2.75$ s  Attempt to use $0.75$ and $2.75$ in two vertical height equations (accept same one or wrong one) $0.75$ and $2.75$ each substituted in the appropriate equn Both values correct. [Using cartesian equation: B1, B1 each equation: M1 solving: A1 correct point of intersection: E1 Verify times]	5
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