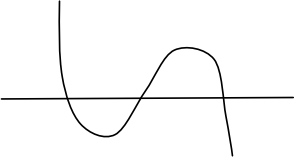


		mark	comment	sub
1(i)	0	B1		1
(ii)	$v = 36 + 6t - 6t^2$	M1 A1	Attempt at differentiation	2
(iii)	$a = 6 - 12t$	M1 F1	Attempt at differentiation	2
(iv)	Take $a = 0$ so $t = 0.5$ and $v = 37.5$ so $37.5 \text{ m s}^{-1}$	M1 A1 A1	Allow table if maximum indicated or implied FT <b>their a</b> cao Accept no justification given that this is maximum	3
(v)	<b>either</b> Solving $36 + 6t - 6t^2 = 0$  so $t = -2$ or $t = 3$ <b>or</b> Sub the values in the expression for $v$ Both shown to be zero A quadratic so the only roots <b>then</b> $x(-2) = -34$ $x(3) = 91$	M1 B1 E1  M1 E1 B1  B1 B1	A method for two roots using <b>their v</b> Factorization or formula or ... of <b>their</b> expression Shown  Allow just 1 substitution shown Both shown Must be a clear argument  cao cao	5
(vi)	$ x(3) - x(0)  +  x(4) - x(3) $ $=  91 - 10  +  74 - 91 $ $= 98$ so 98 m	M1 A1 A1	Considering two parts Either correct cao [SC 1 for $s(4) - s(0) = 64$ ]	3
(vii)	At the SP of $v$  $x(-2) = -34$ i.e. $< 0$ and $x(3) = 91$ i.e. $> 0$ Also $x(-4) = 42 > 0$ and $x(6) = -98 < 0$  	M1    B1  B1	Or any other valid argument e.g. find all the zeros, sketch, consider sign changes. Must have some working. If only a sketch, must have correct shape.  Doing appropriate calculations e.g. find all 3 zeros; sketch cubic reasonably (showing 3 roots); sign changes in range  3 times seen	3
		19		

		mark		Sub
2(i)	$a = 24 - 12t$	M1 A1	Differentiate cao	2
(ii)	Need $24t - 6t^2 = 0$ $t = 0, 4$	M1 A1	Equate $v = 0$ and attempt to factorise (or solve). Award for one root found. Both. cao.	2
(iii)	$s = \int_0^4 (24t - 6t^2) dt$ $= [12t^2 - 2t^3]_0^4$ $(12 \times 16 - 2 \times 64) - 0$  $= 64 \text{ m}$	M1 A1 M1 A1	Attempt to integrate. No limits required.  Either term correct. No limits required  Sub $t = 4$ in integral. Accept no bottom limit substituted or arb const assumed 0. Accept reversed limits. FT <b>their</b> limits. cao. Award if seen. [If trapezium rule used. M1 At least 4 strips: M1 enough strips for 3 s. f. A1 (dep on 2 <sup>nd</sup> M1) One strip area correct: A1 cao]	4
	total	8		

3	(i)	$v = \int (4 - t) dt$ $v = 4t - \frac{1}{2}t^2 + c \quad (t = 0, v = 0 \Rightarrow c = 0)$ $v = 4t - \frac{1}{2}t^2 \text{ for } 0 \leq t \leq 4$ <p>When <math>t = 4</math>, <math>v = 8</math> and for <math>t &gt; 4</math>, <math>a = 0</math> so  <math>v = 8</math> for <math>t &gt; 4</math></p>	M1  A1  B1  <b>[3]</b>	<p>Attempt to integrate</p> <p>Condone no mention of arbitrary constant</p> <p><math>a = 0</math> must be seen or implied</p>	
	(ii)	$s = \int (4t - \frac{1}{2}t^2) dt$ $s = 2t^2 - \frac{1}{6}t^3$ <p>When <math>t = 4</math>, Nina has travelled  <math>2 \times 4^2 - \frac{1}{6} \times 4^3 = 21\frac{1}{3}</math> m</p> <p>When <math>t = 5\frac{1}{3}</math>, Nina has travelled  <math>21\frac{1}{3} + 8 \times 1\frac{1}{3} = 32</math> m</p>	M1  A1  A1  F1  <b>[4]</b>	<p>Again condone no mention of arbitrary constant</p> <p>Allow follow through from their <math>21\frac{1}{3}</math></p> <p>Exact answer required; if rounded to 32, award 0</p>	
	(iii)	<p>When <math>t = 5\frac{1}{3}</math>, Marie has run <math>6 \times 5\frac{1}{3} = 32</math> m.</p> <p>Nina has also run 32 m so caught up Marie</p>	B1  <b>[1]</b>	<p>Allow an equivalent argument that when Marie has run 32 m, <math>t = 5\frac{1}{3}</math>, as for Nina</p> <p>This mark is dependent on an answer 32 in part (ii) but allow this where it is a rounded answer and in this particular case the rounding can be in part (iii)</p>	

		mark	notes
4(i)	For P: the distance is $8T$	B1	Allow – ve. Allow any form.
	For Q: the distance is $\frac{1}{2} \times 4 \times T^2$	B1	Allow – ve. Allow any form.
		2	
(ii)	Require $8T + \frac{1}{2} \times 4 \times T^2 = 90$	M1	For linking correct expressions or <b>their</b> expressions from (i) with 90. Condone sign errors and use of displacement instead of distance. Condone ‘= 0’ implied.
	so $8T + 2T^2 - 90 = 0$	A1	The expression is correct or correctly derived from <b>their</b> (i). Reason not required.
	so $T^2 + 4T - 45 = 0$	E1	Must be established. Do not award if <b>their</b> ‘correct expression’ comes from incorrect manipulation.
	This gives	M1	Solving to find +ve root. Accept $(T + 5)(T - 9)$ .
	$(T - 5)(T + 9) = 0$	A1	Condone 2 <sup>nd</sup> root not found/discussed but not both roots given.
	so $T = 5$ since $T > 0$	5	
		7	

<b>5(i)</b>	$a = 6t - 12$	M1 A1	Differentiating cao	2
<b>(ii)</b>	<p>We need <math>\int_1^3 (3t^2 - 12t + 14)dt</math></p> $= [t^3 - 6t^2 + 14t]_1^3$ <p><b>either</b></p> $= (27 - 54 + 42) - (1 - 6 + 14)$ $= 15 - 9 = 6 \text{ so } 6 \text{ m}$ <p><b>or</b></p> $s = t^3 - 6t^2 + 14t + C$ <p><math>s = 0</math> when <math>t = 1</math> gives</p> $0 = 1 - 6 + 14 + C \text{ so } C = -9$ <p>Put <math>t = 3</math> to give</p> $s = 27 - 54 + 42 - 9 = 6 \text{ so } 6 \text{ m.}$	M1 A1  M1 A1  M1 A1	<p>Integrating. Neglect limits.</p> <p>At least two terms correct. Neglect limits.</p> <p>Dep on 1<sup>st</sup> M1. Use of limits with attempt at subtraction seen.</p> <p>cao</p> <p>Dep on 1<sup>st</sup> M1. An attempt to find <math>C</math> using <math>s(1) = 0</math> and then evaluating <math>s(3)</math>.</p> <p>ca</p>	4
<b>(iii)</b>	<p><math>v &gt; 0</math> so the particle always travels in the same (+ve) direction</p> <p>As the particle never changes direction, the final distance from the starting point is the displacement.</p>	E1 E1	<p>Only award if explicit</p> <p>Complete argument</p>	
				2
				8