

## Exercise 3C

$$\begin{aligned}
 1 \text{ a Speed} &= |3\mathbf{i} + 4\mathbf{j}| \\
 &= \sqrt{3^2 + 4^2} \\
 &= \sqrt{9 + 16} \\
 &= \sqrt{25} \\
 &= 5 \text{ m s}^{-1}
 \end{aligned}$$

$$\begin{aligned}
 \text{b Speed} &= |24\mathbf{i} - 7\mathbf{j}| \\
 &= \sqrt{24^2 + (-7)^2} \\
 &= \sqrt{576 + 49} \\
 &= \sqrt{625} \\
 &= 25 \text{ km h}^{-1}
 \end{aligned}$$

$$\begin{aligned}
 \text{c Speed} &= |5\mathbf{i} + 2\mathbf{j}| \\
 &= \sqrt{5^2 + 2^2} \\
 &= \sqrt{25 + 4} \\
 &= \sqrt{29} \\
 &= 5.39 \text{ m s}^{-1} \text{ (3 s.f.)}
 \end{aligned}$$

$$\begin{aligned}
 \text{d Speed} &= |-7\mathbf{i} + 4\mathbf{j}| \\
 &= \sqrt{(-7)^2 + 4^2} \\
 &= \sqrt{49 + 16} \\
 &= \sqrt{65} \\
 &= 8.06 \text{ cm s}^{-1} \text{ (3 s.f.)}
 \end{aligned}$$

$$\begin{aligned}
 2 \text{ a Distance} &= \text{speed} \times \text{time} \\
 &= \sqrt{8^2 + 6^2} \times 5 \\
 &= 5 \times \sqrt{64 + 36} \\
 &= 5 \times \sqrt{100} \\
 &= 50 \text{ km}
 \end{aligned}$$

$$\begin{aligned}
 \text{b Distance} &= \text{speed} \times \text{time} \\
 &= \sqrt{5^2 + (-1)^2} \times 10 \\
 &= 10 \times \sqrt{25 + 1} \\
 &= 10 \times \sqrt{26} \\
 &= 51.0 \text{ m (3 s.f.)}
 \end{aligned}$$

$$\begin{aligned}
 2 \text{ c Distance} &= \text{speed} \times \text{time} \\
 &= \sqrt{6^2 + 2^2} \times 0.75 \\
 &= 0.75 \times \sqrt{36 + 4} \\
 &= 0.75 \times \sqrt{40} \\
 &= 4.74 \text{ km (3 s.f.)}
 \end{aligned}$$

$$\begin{aligned}
 \text{d Distance} &= \text{speed} \times \text{time} \\
 &= \sqrt{(-4)^2 + (-7)^2} \times 120 \\
 &= 120 \times \sqrt{16 + 49} \\
 &= 120 \times \sqrt{65} \\
 &= 967 \text{ cm (3 s.f.)}
 \end{aligned}$$

$$\begin{aligned}
 3 \text{ a Speed} &= \sqrt{(-3)^2 + 4^2} \\
 &= \sqrt{9 + 16} \\
 &= \sqrt{25} \\
 &= 5 \text{ m s}^{-1}
 \end{aligned}$$

$$\text{Distance} = 5 \times 15 = 75 \text{ m}$$

$$\begin{aligned}
 \text{b Speed} &= \sqrt{2^2 + 5^2} \\
 &= \sqrt{4 + 25} \\
 &= \sqrt{29} \\
 &= 5.39 \text{ m s}^{-1} \text{ (3 s.f.)}
 \end{aligned}$$

$$\text{Distance} = 3 \times 5.39 = 16.2 \text{ m (3 s.f.)}$$

$$\begin{aligned}
 \text{c Speed} &= \sqrt{5^2 + (-2)^2} \\
 &= \sqrt{25 + 4} \\
 &= \sqrt{29} \\
 &= 5.39 \text{ km h}^{-1} \text{ (3 s.f.)}
 \end{aligned}$$

$$\text{Distance} = 3 \times 5.39 = 16.2 \text{ km (3 s.f.)}$$

$$\begin{aligned} 3 \text{ d Speed} &= \sqrt{12^2 + (-5)^2} \\ &= \sqrt{144 + 25} \\ &= \sqrt{169} \\ &= 13 \text{ km h}^{-1} \end{aligned}$$

$$\text{Distance} = 0.5 \times 13 = 6.5 \text{ km}$$