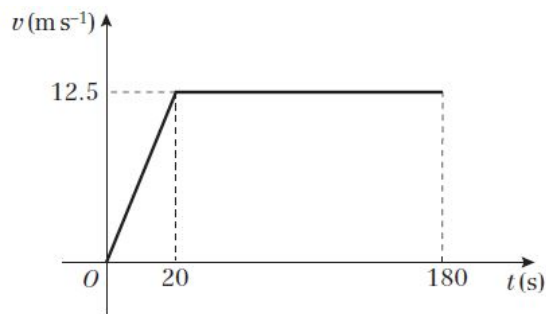


Chapter review 2

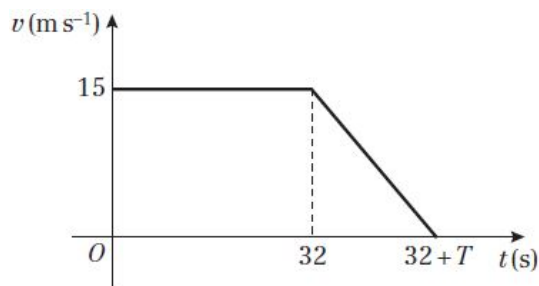
$$\begin{aligned}
 \mathbf{1 \ a} \quad 45 \text{ km h}^{-1} &= \frac{45 \times 1000}{3600} \text{ m s}^{-1} \\
 &= 12.5 \text{ m s}^{-1} \\
 3 \text{ min} &= 180 \text{ s}
 \end{aligned}$$



$$\begin{aligned}
 \mathbf{b} \quad s &= \frac{1}{2}(a+b)h \\
 &= \frac{1}{2}(160+180) \times 12.5 = 2125
 \end{aligned}$$

The distance from *A* to *B* is 2125 m.

2 a



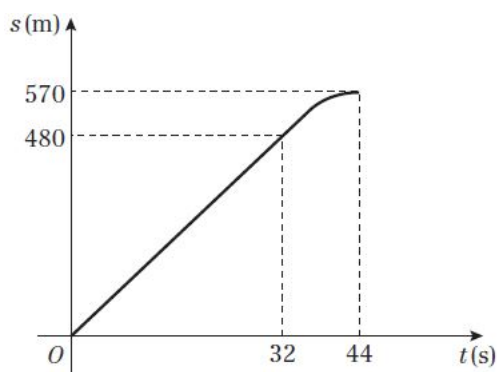
$$\mathbf{b} \quad s = \frac{1}{2}(a+b)h$$

$$\begin{aligned}
 570 &= \frac{1}{2}(32 + 32 + T) \times 15 \\
 \frac{15}{2}(T + 64) &= 570 \\
 T + 64 &= \frac{570 \times 2}{15} = 76 \\
 T &= 76 - 64 = 12
 \end{aligned}$$

$$\mathbf{c} \quad \text{At } t = 32, s = 32 \times 15 = 480$$

$$\begin{aligned}
 \text{At } t = 44, s &= 480 + \text{area of the triangle} \\
 &= 480 + \frac{1}{2} \times 12 \times 15 = 570
 \end{aligned}$$

2 c



3 a i Gradient of line = $\frac{v-u}{t}$

$$a = \frac{v-u}{t}$$

Rearranging: $v = u + at$

ii Shaded area is a trapezium

$$\text{area} = \left(\frac{u+v}{2} \right) t$$

$$s = \left(\frac{u+v}{2} \right) t$$

b i Rearrange $v = u + at$

$$t = \frac{v-u}{a}$$

Substitute into $s = \left(\frac{u+v}{2} \right) t$

$$s = \left(\frac{u+v}{2} \right) \left(\frac{v-u}{a} \right)$$

$$2as = v^2 - u^2$$

$$v^2 = u^2 + 2as$$

ii Substitute $v = u + at$ into $s = \left(\frac{u+v}{2} \right) t$

$$s = \left(\frac{u+u+at}{2} \right) t$$

$$s = \left(\frac{2u}{2} + \frac{at}{2} \right) t$$

$$s = ut + \frac{1}{2}at^2$$

3 b iii Substitute $u = v - at$ into $s = ut + \frac{1}{2}at^2$

$$s = (v - at)t + \frac{1}{2}at^2$$

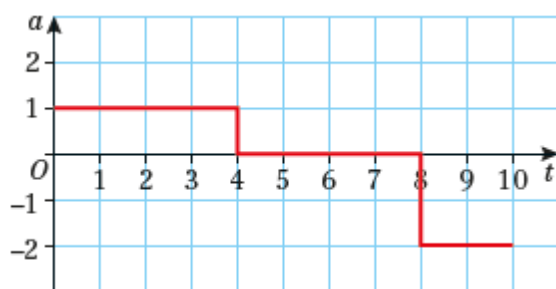
$$s = vt - \frac{1}{2}at^2$$

4 $s = \frac{1}{2}(a + b)h$

$$152 = \frac{1}{2}(15 + 23)u = 19u$$

$$u = \frac{152}{19} = 8$$

5



6 $40 \text{ km h}^{-1} = \frac{40 \times 1000}{3600} \text{ m s}^{-1} = \frac{100}{9} \text{ m s}^{-1}$

$$24 \text{ km h}^{-1} = \frac{24 \times 1000}{3600} \text{ m s}^{-1} = \frac{20}{3} \text{ m s}^{-1}$$

$$u = \frac{100}{9}, v = \frac{20}{3}, s = 240, a = ?$$

$$v^2 = u^2 + 2as$$

$$\left(\frac{20}{3}\right)^2 = \left(\frac{100}{9}\right)^2 + 2 \times a \times 240$$

$$a = \frac{\left(\frac{20}{3}\right)^2 - \left(\frac{100}{9}\right)^2}{2 \times 240} = -0.165 \text{ (to 2 s.f.)}$$

The deceleration of the car is 0.165 m s^{-2} .

7 a $a = -2.5, u = 20, t = 12, s = ?$

$$s = ut + \frac{1}{2}at^2$$

$$= 20 \times 12 - \frac{1}{2} \times 2.5 \times 12^2$$

$$= 240 - 180 = 60$$

$$OA = 60 \text{ m}$$

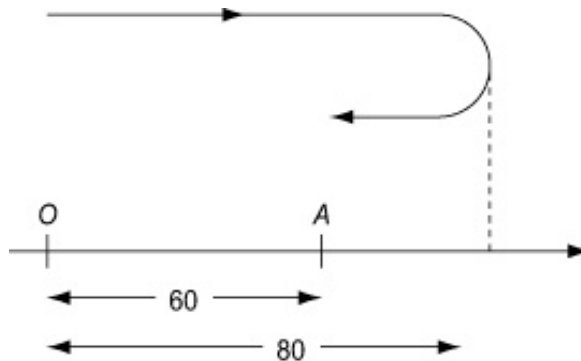
7 b The particle will turn round when $v = 0$

$$a = -2.5, u = 20, v = 0, s = ?$$

$$v^2 = u^2 + 2as$$

$$0^2 = 20^2 - 5s \Rightarrow s = 80$$

The total distance P travels is $(80 + 20) \text{ m} = 100 \text{ m}$



8 $u = 6, v = 25, a = 9.8, t = ?$

$$v = u + at$$

$$25 = 6 + 9.8t$$

$$t = \frac{25 - 6}{9.8} = 1.9 \text{ (to 2 s.f.)}$$

The ball takes 1.9 s to move from the top of the tower to the ground.

9 Take downwards as the positive direction.

a i $u = 0, s = 82, a = 9.8, t = ?$

$$s = ut + \frac{1}{2}at^2$$

$$82 = 0 + 4.9t^2$$

$$t = \sqrt{\frac{82}{4.9}} = 4.1 \text{ (to 2 s.f.)}$$

The time taken for the ball to reach the sea is 4.1 s.

a ii $u = 0, s = 82, a = 9.8, v = ?$

$$v^2 = u^2 + 2as$$

$$= 0 + 2 \times 9.8 \times 82 = 1607.2$$

$$v = \sqrt{1607.2} = 40 \text{ (to 2 s.f.)}$$

The speed at which the ball hits the sea is 40 m s^{-1} .

b Air resistance/wind/turbulence

10 a distance = area of triangle + area of rectangle + area of trapezium

$$\begin{aligned} 451 &= \frac{1}{2} \times 8 \times 2u + 12 \times 2u + \frac{1}{2} \times (u + 2u) \times 6 \\ &= 8u + 24u + 9u = 41u \\ u &= \frac{451}{41} = 11 \end{aligned}$$

b The particle is moving with speed less than $u \text{ m s}^{-1}$ for the first 4 s

$$s = \frac{1}{2} \times 4 \times 11 = 22$$

The distance moved with speed less than $u \text{ m s}^{-1}$ is 22 m.

11 a From O to P , $u = 18$, $t = 12$, $v = 24$, $a = ?$

$$u = 18, t = 12, v = 24, a = ?$$

$$v = u + at$$

$$24 = 18 + 12a$$

11 a $a = \frac{24 - 18}{12} = \frac{1}{2}$

From O to Q , $u = 18$, $t = 20$, $a = \frac{1}{2}$, $v = ?$

$$v = u + at$$

$$= 18 + \frac{1}{2} \times 20 = 28$$

The speed of the train at Q is 28 m s^{-1} .

b From P to Q

$$u = 24, v = 28, t = 8, s = ?$$

$$s = \left(\frac{u + v}{2} \right) t = \left(\frac{24 + 28}{2} \right) \times 8 = 208$$

The distance from P to Q is 208 m.

12 a $s = 104$, $t = 8$, $v = 18$, $u = ?$

$$s = \left(\frac{u + v}{2} \right) t$$

$$104 = \left(\frac{u + 18}{2} \right) \times 8 = (u + 18) \times 4 = 4u + 72$$

$$u = \frac{104 - 72}{4} = 8$$

The speed of the particle at X is 8 m s^{-1}

12 b $s = 104$, $t = 8$, $v = 18$, $a = ?$

$$s = vt - \frac{1}{2}at^2$$

$$104 = 18 \times 8 - \frac{1}{2}a \times 8^2 = 144 - 32a$$

$$a = \frac{144 - 104}{32} = 1.25$$

The acceleration of the particle is 1.25 m s^{-2} .

c From X to Z , $u = 8$, $v = 24$, $a = 1.25$, $s = ?$

$$v^2 = u^2 + 2as$$

$$24^2 = 8^2 + 2 \times 1.25 \times s$$

$$s = \frac{24^2 - 8^2}{2.5} = 204.8$$

$$XZ = 204.8 \text{ m}$$

13 a Take upwards as the positive direction.

$$u = 21$$
, $s = -32$, $a = -9.8$, $v = ?$

$$v^2 = u^2 + 2as$$

$$= 21^2 + 2 \times (-9.8) \times (-32) = 441 + 627.2 = 1068.2$$

$$v = \sqrt{1068.2} = \pm 33 \text{ (to 2 s.f.)}$$

The velocity with which the pebble strikes the ground is -33 m s^{-1} .

The speed is 33 m s^{-1} .

b 40 m above the ground is 8 m above the point of projection.

$$u = 21$$
, $s = 8$, $a = -9.8$, $t = ?$

$$s = ut + \frac{1}{2}at^2$$

$$8 = 21t - 4.9t^2$$

$0 = 4.9t^2 - 21t + 8$, so using the quadratic formula,

$$t = \frac{21 \pm \sqrt{21^2 - 4 \times 4.9 \times 8}}{9.8} = \frac{21 \pm \sqrt{284.2}}{9.8} = 3.86, 0.423 \text{ (to 3 s.f.)}$$

The pebble is above 40 m between these times: $3.863... - 0.423... = 3.44$ (to 3 s.f.)

The pebble is more than 40 m above the ground for 3.44 s.

13 c Take upwards as the positive direction.

$$u = 21, a = -9.8$$

$$v = u + at = 21 - 9.8t \Rightarrow t = \frac{21 - v}{9.8}$$

From part **a**, the pebble hits the ground when $v = -33$.

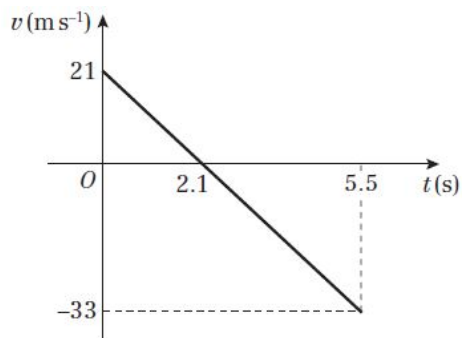
$$t = \frac{21 - v}{9.8} = \frac{21 - (-33)}{9.8} = \frac{54}{9.8} = 5.5 \text{ (to 2 s.f.)}$$

This is shown on the graph at point $(5.5, -33)$

The graph crosses the t -axis when $v = 0$.

$$t = \frac{21 - v}{9.8} = \frac{21 - 0}{9.8} = \frac{21}{9.8} = 2.1 \text{ (to 2 s.f.)}$$

So the graph passes through point $(2.1, 0)$



14 a $u = 12, v = 32, s = 1100, t = ?$

$$s = \left(\frac{u + v}{2} \right) t$$

$$1100 = \left(\frac{12 + 32}{2} \right) t = 22t \Rightarrow t = \frac{1100}{22} = 50$$

The time taken by the car to move from A to C is 50 s.

14 b Find a first.

From A to C , $u = 12$, $v = 32$, $t = 50$, $a = ?$

$$v = u + at$$

$$32 = 12 + a \times 50$$

$$a = \frac{32 - 12}{50} = 0.4$$

From A to B , $u = 12$, $s = 550$, $a = 0.4$, $v = ?$

$$v^2 = u^2 + 2as$$

$$= 12^2 + 2 \times 0.4 \times 550 = 584 \Rightarrow v = 24.2 \text{ (to 3 s.f.)}$$

The car passes B with speed 24.2 m s^{-1} .

15 Take upwards as the positive direction.

At the top:

$$u = 30, v = 0, a = -9.8, t = ?$$

$$v = u + at$$

$$0 = 30 - 9.8t \Rightarrow t = \frac{30}{9.8}$$

The ball spends 2.4 seconds above h , thus (by symmetry) 1.2 seconds rising between h and the top.

So it passes h 1.2 seconds earlier, at $t = \frac{30}{9.8} - 1.2 = 1.86$ (to 3 s.f.)

At h , $u = 30$, $a = -9.8$, $t \approx 1.86$, $s = ?$

$$s = ut + \frac{1}{2}at^2$$

$$= 30 \times 1.86 + \frac{1}{2}(-9.8) \times 1.86^2 = 39 \text{ (to 2 s.f.)}$$

16 a $u = 20$, $a = 4$, $s = 78$, $v = ?$

$$v^2 = u^2 + 2as$$

$$= 20^2 + 2 \times 4 \times 78 = 1024$$

$$v = \sqrt{1024} = 32$$

The speed of B when it has travelled 78 m is 32 m s^{-1} .

16 b Find time for B to reach the point 78 m from O .

$$v = 32, u = 20, a = 4, t = ?$$

$$v = u + at$$

$$32 = 20 + 4t \Rightarrow t = \frac{32 - 20}{4} = 3$$

For A , distance = speed \times time

$$s = 30 \times 3 = 90$$

The distance from O of A when B is 78 m from O is 90 m.

c At time t seconds, for A , $s = 30t$

$$\text{for } B, s = ut + \frac{1}{2}at^2 = 20t + 2t^2$$

On overtaking the distances are the same.

$$20t + 2t^2 = 30t$$

$$t^2 - 5t = t(t - 5) = 0$$

$$t = 5 \text{ (at } t = 0, A \text{ overtakes } B)$$

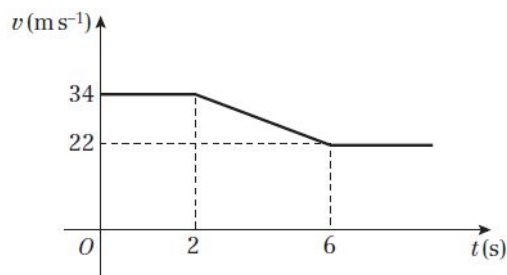
B overtakes A 5 s after passing O .

17 a To find time decelerating:

$$u = 34, v = 22, a = -3, t = ?$$

$$v = u + at$$

$$22 = 34 - 3t \Rightarrow t = \frac{34 - 22}{3} = 4$$

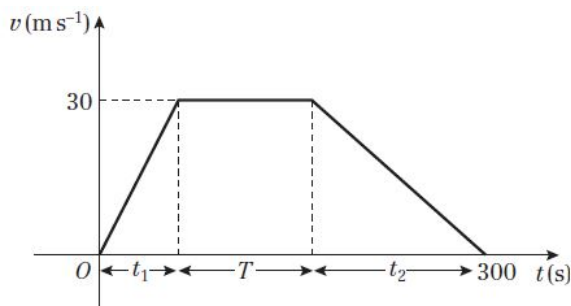


17 b distance = rectangle + trapezium

$$\begin{aligned} s &= 34 \times 2 + \frac{1}{2}(22 + 34) \times 4 \\ &= 68 + 112 = 180 \end{aligned}$$

Distance required is 180 m.

18 a



b Acceleration is the gradient of a line.

$$\text{For the first part of the journey, } 3x = \frac{30}{t_1} \Rightarrow t_1 = \frac{30}{3x} = \frac{10}{x}$$

$$\text{For the last part of the journey, } -x = -\frac{30}{t_2} \Rightarrow t_2 = \frac{30}{x}$$

$$t_1 + T + t_2 = 300$$

$$\frac{10}{x} + T + \frac{30}{x} = 300 \Rightarrow \frac{40}{x} + T = 300, \text{ as required}$$

c $s = \frac{1}{2}(a + b)h$

$$6000 = \frac{1}{2}(T + 300) \times 30 = 15T + 4500$$

$$T = \frac{6000 - 4500}{15} = 100$$

Substitute into the result in part b:

$$\frac{40}{x} + 100 = 300 \Rightarrow \frac{40}{x} = 200$$

$$x = \frac{40}{200} = 0.2$$

d From part c, $T = 100$

$$\text{At constant velocity, distance} = \text{velocity} \times \text{time} = 30 \times 100 = 3000 \text{ (m)}$$

The distance travelled at a constant speed is 3 km.

18 e From part **b**, $t_1 = \frac{10}{x} = \frac{10}{0.2} = 50$

Total distance travelled = 6 km (given) so halfway = 3 km = 3000 m

While accelerating, distance travelled is $(\frac{1}{2} \times 50 \times 30)$ m = 750 m.

At constant velocity, the train must travel a further 2250 m.

$$\text{At constant velocity, time} = \frac{\text{distance}}{\text{velocity}} = \frac{2250}{30} \text{ s} = 75 \text{ s}$$

Time for train to reach halfway is $(50 + 75)$ s = 125 s

Challenge

Find the time taken by the first ball to reach 25 m below its point of projection (25 m above the ground). Take upwards as the positive direction.

$$u = 10, \quad s = -25, \quad a = -9.8, \quad t = ?$$

$$s = ut + \frac{1}{2}at^2$$

$$-25 = 10t - 4.9t^2$$

$$0 = 4.9t^2 - 10t - 25$$

$$t = 10 \pm \frac{\sqrt{102 + 4 \times 4.9 \times 25}}{9.8}$$

$$= 3.5 \text{ (to 2 s.f.)}$$

As we discard the negative solution. Find the time taken by the second ball to reach 25 m below its point of projection. Take downwards as the positive direction.

$$u = 0, \quad s = 25, \quad a = 9.8, \quad t = ?$$

$$s = ut + \frac{1}{2}at^2$$

$$25 = 4.9t^2$$

$$t = 2.3 \text{ (to 2 s.f.)}$$

Combining the two results:

$$T = 3.4989... - 2.2587... = 1.2 \text{ (to 2 s.f. using exact figures)}$$