## GCE Examinations Advanced Subsidiary / Advanced Level

# Mechanics Module M1

### Paper B

### **MARKING GUIDE**

This guide is intended to be as helpful as possible to teachers by providing concise solutions and indicating how marks should be awarded. There are obviously alternative methods that would also gain full marks.

Method marks (M) are awarded for knowing and using a method.

Accuracy marks (A) can only be awarded when a correct method has been used.

(B) marks are independent of method marks.



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#### M1 Paper B - Marking Guide

- $\mathbf{a} = \frac{\Delta \mathbf{v}}{t} = \frac{1}{2} \left[ (4\mathbf{i} 7\mathbf{j}) (-2\mathbf{i} + \mathbf{j}) \right] = 3\mathbf{i} 4\mathbf{j}$ 1.
- M1 A1

 $F = ma = 5(3\mathbf{i} - 4\mathbf{j})$ (b) mag. of  $\mathbf{F} = 5\sqrt{3^2 + 4^2} = 25 \text{ N}$  M1M1 A1

req'd angle =  $\tan^{-1} \frac{3}{4} = 37^{\circ}$  to nearest degree

- M1 A1 **(7)**
- cons. of mom: 3mu 2mu = 2mv (dir<sup>n</sup> of B after coll. taken as +ve) 2. *(a)*  $mu = 2mv : v = \frac{1}{2}u$ 
  - M2 A<sub>1</sub> **B**1
  - hence, speed of B halved and change of sign means dir<sup>n</sup> has reversed
  - (b) impulse =  $\Delta$  mom: i.e. for A, 9m = 0 - (-3mu)

M2

9m = 3mu : u = 3

**A**1 **(7)** 

- 3.
  - resolve  $\uparrow$ : 3T = 180g(a)

M1 **A**1

T = 60g, so tension in cable at P = 120g.

- M2 A1
- moments about *P*: 100gx + 60g(1.25) + 20g(1.5) = 3T(b) 100gx = 75g, so x = 0.75 and hence BP = 0.75m
- M1 A1

(i) weight acts at middle of platform (c) platform doesn't bend (ii)

- **B**1
- **B**1

**(9)** 

- use of  $s = ut + \frac{1}{2} at^2$  for OL (54m, t = 1) and OM (144m, t = 4) 4.
- M2

to give  $54 = u + \frac{1}{2}a$  and 144 = 4u + 8a

**A**1

solve simult. to give  $a = -12 \text{m s}^{-2}$ 

M1 A1

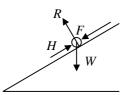
(b) for *ON*, u = 60, a = 12, v = 0 $v^2 = u^2 + 2as$ , so 0 = 3600 - 24s

M1 M1

s = 150m, so MN = 150 - 144 = 6m.

M1 A1 **(9)** 

5. (a)



B2

- resolve perp. to plane:  $R 2g\cos 30^\circ = 0$  :  $R = g\sqrt{3}$ (b)
- M1 A1

 $F = \mu R = \frac{1}{\sqrt{3}} g\sqrt{3} = g$ 

M1 A1

resolve // to plane:  $H - F - 2g\sin 30^\circ = 0$ 

M1

H-g-g=0 : H=2gF: H = g: 2g = 1:2

- A<sub>1</sub> A1
- (c) friction varies between  $\mu R$  up plane (to prevent movement down plane) and  $\mu R$  down plane (to prevent movement up plane)
- B<sub>2</sub> (11)

6.

$$R_{v}$$
  $T$   $D$ 

 $acc^{n} = \frac{25-0}{20} = \frac{5}{4} m s^{-2}$ M1 A1 for car and van, eqn. of motion is  $D - 1200 = 2000 \times \frac{5}{4}$ M1 D = 3700 N**A**1 1200 divided in ratio 1.25: 0.75 i.e. 5:3 (b) M1 car resistance =  $\frac{5}{8} \times 1200 = 750 \text{ N}$ , so caravan resistance is 450 N **A**1 for car, eqn. of motion is  $3700 - 750 - T = 1250 \times \frac{5}{4}$ M1 T = 1387.5 N**A**1 for van,  $^{-}450 = 750a$  :  $a = ^{-\frac{3}{5}}$  ms<sup>-2</sup> (c) M1A1 u = 25, v = 0,  $a = -\frac{3}{5}$  use  $v^2 = u^2 + 2as$ M1 $0 = 625 - \frac{6}{5}s$  : s = 520.8 m M1 A1 e.g. caravan may nose down at front, may not stay in a straight line (d)**B**1 so dist. likely to be less than that calculated in (c)**B**1 (15)7. dist. between Alison and Bill =  $\sqrt{(-5)^2 + 12^2}$  = 13 km M1 A1 *(a)*  $|3\mathbf{i} + \mathbf{j}| = \sqrt{10}$ ; speed =  $2\sqrt{10}$ (b) M1  $\therefore \mathbf{v} = 2(3\mathbf{i} + \mathbf{j}) = 6\mathbf{i} + 2\mathbf{j}$ M1 A1 after t hours, Alison is at  $(2t)\mathbf{i} + (5t)\mathbf{j}$ (c) M1 A1 Bill is at  $(6t - 5)\mathbf{i} + (2t + 12)\mathbf{j}$ **A**1 rel to A, pos<sup>n</sup> vector of B is  $(6t - 5 - 2t)\mathbf{i} + (2t + 12 - 5t)\mathbf{j}$ M1  $= (4t - 5)\mathbf{i} + (12 - 3t)\mathbf{j}$  km **A**1  $d^{2} = (4t - 5)^{2} + (12 - 3t)^{2}$ = 16t<sup>2</sup> - 40t + 25 + 144 - 72t + 9t<sup>2</sup> = 25t<sup>2</sup> - 112t + 169 (*d*) M1 A1  $d^2 < 121$  ::  $25t^2 - 112t + 169 < 121$   $25t^2 - 112t + 48 < 0$ , so (25t - 12)(t - 4) < 0(e) M1 A1 M1 suitable method to get  $\frac{12}{25} < t < 4$ **A**1 length of time =  $3\frac{13}{25}$  hours = 3 hours 31 minutes (to nearest minute) **A**1 **(17)** 

Total (75)

#### Performance Record – M1 Paper B

Question no.	1	2	3	4	5	6	7	Total
Topic(s)	<b>i</b> , <b>j</b> vectors, <i>F</i> = <i>ma</i>	cons. of mom., impulse	moments, modelling	uniform accel.	statics incl. friction	connected bodies	speed, rel. posn.	
Marks	7	7	9	9	11	15	17	75
Student								