

4761

Mark Scheme

June 2012

Question		Answer	Marks	Guidance
1	(A)	False This is a speed-time graph not one for displacement-time	M1 A1	<p>Notice that the runner may have returned to his starting place or may not; the graph does not contain the information to tell you which is the case.</p> <p>Accept statements only if they are true and relevant, e.g.:</p> <ul style="list-style-type: none"> There is no information about direction of travel There is no evidence to suggest he has turned round Distance is given by the area under the graph but this is not the same as displacement Speed is not a vector and so the area under the graph says nothing about the direction travelled It just (or only) shows speed-time <p>Do not accept statements that are, or may be, untrue: eg The particle moves only in the positive direction</p> <p>Do not accept statements that are true but irrelevant: eg The distance travelled is the area under the graph</p> <p>Condone This is a speed time graph not one for distance-time</p>
1	(B)	True	B1	Ignore subsequent working
1	(C)	True	B1	Ignore subsequent working
1	(D)	False The area under the graph is 420 not 400	M1 A1 [6]	<p>Accept area up to time 55 s is 400 m</p> <p>The calculation in the false example must be correct</p>

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2	(i)	$v = \int (6t - 12) dt$ $v = 3t^2 - 12t + c$ $c = 9$ $t = 3 \Rightarrow v = 3 \times 3^2 - 12 \times 3 + 9 = 0$	M1 A1 A1 E1 [4]	Attempt to integrate Condone no c if implied by subsequent working (eg adding 9 to the expression) Or by showing that $(t - 3)$ is a factor of $3t^2 - 12t + 9$
2	(ii)	$s = \int (3t^2 - 12t + 9) dt$ $s = t^3 - 6t^2 + 9t - 2$ When $t = 2$, $s = 0$. (It is at the origin.)	M1 A1 B1 [3]	Attempt to integrate Ft from part (i) A correct value of c is required. Ft from part (i). Cao
3	(i)	P + Q + R = 0i + 0j	B1 [1]	Accept answer zero (ie condone it not being in vector form)
3	(ii)	(A) The particle is in equilibrium (B) The hiker returns to her starting point	B1 B1 [2]	If “equilibrium” is seen give B1 and ignore whatever else is written. Allow, instead, “acceleration is zero”, “the particle has constant velocity” and other equivalent statements. Do not allow “The forces are balanced”, “The particle is stationary” as complete answers Do not allow “The hiker’s displacement is zero”

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4	(i)	At C: $s = ut + \frac{1}{2}at^2$ $500 = 5 \times 20 + 0.5 \times a \times 20^2$ $a = 2 \text{ (ms}^{-2}\text{)}$	M1 A1 [2]	M1 for a method which if correctly applied would give a . Cao Special case If 800 is used for s instead of 500, giving $a = 3.5$, treat this as a misread. Annotate it as SC SC and give M1 A0 in this part
4	(ii)	At B: $v^2 - u^2 = 2as$ $v^2 - 5^2 = 2 \times 2 \times 300$ $v = 35$ Speed is 35 m s^{-1} At B: $v = u + at$ $35 = 5 + 2 \times t$ $t = 15$ Time is 15 s	M1 A1 A1 [3]	M1 for a method which if correctly applied would give either v or t Apply FT from incorrect a from part (i) for the M mark only Cao. No FT from part (i) except for SC1 for 46.2 following $a = 3.5$ after the use of $s = 800$. Cao. No FT from part (i) except for SC1 for 11.7 following $a = 3.5$ after the use of $s = 800$.

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5	(i)		B2 [2]	<p>Subtract one mark for each error, omission or addition down to a minimum of zero. Each force must have a label and an arrow.</p> <p>Accept T for 50 N.</p> <p>Units not required.</p> <p>If a candidate gives the tension in components: Accept if the components are a replacement for the tension Treat as an error if the components duplicate the tension However, accept dotted lines for the components as not being duplication</p>
5	(ii)	<p>Horizontal equilibrium :</p> $R = 50 \sin 30^\circ = 25$	M1 A1 [2]	<p>May be implied. Allow sin-cos interchange for this mark only</p> <p>Award both marks for a correct answer after a mistake in part (i) (eg omission of R)</p>
5	(iii)	<p>Vertical equilibrium</p> $N + 50 \cos 30^\circ = 10g$ $N = 54.7 \text{ to 3 s.f.}$	M1 A1 [2]	<p>Relationship must be seen and involve all 3 elements. No credit given in the case of sin-cos interchange</p> <p>Cao</p>
5	(iv)	$\text{Resultant} = \sqrt{25^2 + 54.7^2}$ <p>Resultant is 60.1 N</p>	M1 A1 [2]	<p>Use of Pythagoras. Components must be correct but allow ft from both (ii) and (iii) for this mark only</p> <p>Cao</p>

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6	(i)	Either Both components of initial speed Horiz $31\cos 20^\circ$ (29.1) Vert $31\sin 20^\circ$ (10.6)	B1	No credit if sin-cos interchanged The components may be found anywhere in the question
		Time to goal = $\frac{50}{31\cos 20^\circ}$ = 1.716 ... s	M1 A1	Attempt to use horizontal distance \div horizontal speed
		$h = 31 \times \sin 20^\circ \times 1.716 + 0.5 \times (-9.8) \times (1.716)^2$	M1	Use of one (or more) formula(e) to find the required result(s) relating to vertical motion within a correct complete method. Finding the maximum height is not in itself a complete method.
		$h = 3.76$ (m) So the ball goes over the crossbar	A1 E1	Allow 3.74 or other answers that would round to 3.7 or 3.8 if they result from premature rounding Dependent on both M marks. Allow follow through from previous answer
		Or Both components of initial speed $h = 31\sin 20^\circ \times t - 4.9t^2$ Substitute $h = 2.44 \Rightarrow t = (0.26 \text{ or}) 1.90$ Substitute $t = 1.90$ in $x = 31\cos 20^\circ \times t$ $x = 55.4$ Since $55.4 > 50$ the ball goes over the crossbar	B1 M1 A1 M1 A1 E1	May be found anywhere in the question. No credit if sin-cos interchange If only 0.26 is given, award A0 Allow this mark for substituting $t = 0.26$ Allow $x = 7.6$ following on from $t = 0.26$ Dependent on both M marks. Allow FT from their value for 55.4.
		Or Both components of initial speed $h = 31\sin 20^\circ \times t - 4.9t^2$ Substitute $h = 2.44 \Rightarrow t = (0.26 \text{ or}) 1.90$ Time to goal = $\frac{50}{31\cos 20^\circ}$ = 1.716 ... s Since $1.90 > 1.72$ the ball goes over the crossbar	B1 M1 A1 M1 A1 E1	May be found anywhere in the question. No credit if sin-cos interchanged Attempt to use horizontal distance \div horizontal speed Dependent on both M marks. Allow follow through from previous answer

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		<p>Or</p> <p>Use of the equation of the trajectory</p> $y = x \tan 20^\circ - \frac{9.8x^2}{2 \times 31^2 \times \cos^2 20^\circ}$ <p>Substituting $x = 50$</p> $\Rightarrow y = 3.76$ <p>So the ball goes over the crossbar</p>	<p>M1</p> <p>A1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>E1</p>	<p>Correct substitution of $\alpha = 20^\circ$</p> <p>Fully correct</p> <p>Dependent on both M marks. Follow through from previous answer</p>
6	(ii)	Any one reasonable statement	<p>B1</p> <p>[1]</p>	<p>Accept</p> <p>The ground is horizontal</p> <p>The ball is initially on the ground</p> <p>Air resistance is negligible</p> <p>Horizontal acceleration is zero</p> <p>The ball does not swerve</p> <p>There is no wind</p> <p>The particle model is being used</p> <p>The value of g is 9.8</p> <p>Do not accept</p> <p>g is constant</p>

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Question		Answer	Marks	Guidance
7	(i)	<p>Total mass of train = 800 000 kg</p> <p>Total resistance = $5R + 17R (= 22R)$</p> <p>Newton's 2nd Law in the direction of motion</p> <p>$121\,000 - 22R = 800\,000 \times 0.11$</p> <p>$22R = 121\,000 - 88\,000 \quad R = 1500$</p>	<p>B1</p> <p>B1</p> <p>M1</p> <p>E1</p> <p>[4]</p>	<p>Allow 800 (tonnes)</p> <p>The right elements must be present, consistent with the candidate's answers above for total resistance and mass . No extra forces.</p> <p>Perfect answer required</p>
7	(ii)	(A) <p>Either (Last truck)</p> <p>Resultant force on last truck = $40\,000 \times 0.11$</p> <p>Use of Newton's 2nd Law</p> <p>$T - 1500 = 40\,000 \times 0.11$</p> <p>$T = 5900$ The tension is 5900 N.</p>	<p>B1</p> <p>M1</p> <p>A1</p> <p>A1</p>	<p>Award this mark for $40\,000 \times 0.11 (= 4400)$ or 40×0.11 seen</p> <p>The right elements must be present and consistent with the answer above; no extra forces.</p> <p>Fully correct equation, or equivalent working</p> <p>Cao</p> <p>Special case Award SC2 to a candidate who, instead, provides a perfect argument that the tension in the penultimate coupling is 11 800 N.</p>
		<p>Or (Rest of the train)</p> <p>Resultant force on rest of train = $760\,000 \times 0.11$</p> <p>Use of Newton's 2nd Law</p> <p>$121\,000 - 31\,500 - T = 760\,000 \times 0.11$</p> <p>$T = 5900$ The tension is 5900 N.</p>	<p>B1</p> <p>M1</p> <p>A1</p> <p>A1</p> <p>[4]</p>	<p>Award this mark for $760\,000 \times 0.11 (= 83\,600)$ or 760×0.11 seen</p> <p>The right elements must be present consistent with the answer above; no extra forces.</p> <p>Fully correct equation, or equivalent working</p> <p>Cao</p>

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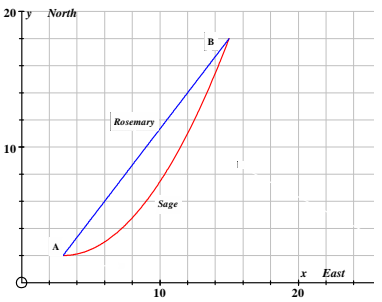
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7	(ii)	(B)	<p>Either (Rest of the train)</p> <p>Newton's 2nd Law is applied to the trucks</p> $S - 25\,500 = 680\,000 \times 0.11$ $S = 100\,300 \quad \text{The tension is } 100\,300 \text{ N.}$	M1 A1 A1	The right elements must be present; no extra forces Cao
			<p>Or (Locomotive)</p> <p>Newton's 2nd Law is applied to the locomotive</p> $121\,000 - S - 5 \times 1500 = 120\,000 \times 0.11$ $S = 100\,300 \quad \text{The tension is } 100\,300 \text{ N.}$	M1 A1 A1	The right elements must be present; no extra forces Cao
			<p>Or (By argument)</p> <p>Each of the 17 trucks has the same mass, resistance and acceleration.</p> <p>So the tension in the first coupling is 17 times that in the last coupling</p> $T = 17 \times 5900 = 100\,300$	M1 A1 A1 [3]	Cao. For this statement on its own with no supporting argument allow SC2
7	(iii)		<p>Resolved component of weight down slope</p> $= 800\,000 \times 9.8 \times \frac{1}{80}$ $= 98\,000 \text{ N}$ <p>Let the acceleration be $a \text{ m s}^{-2}$ up the slope.</p> <p>Newton's 2nd Law to the whole train,</p> $121\,000 - 33\,000 - 98\,000 = 800\,000a$ $a = -0.0125$ <p>Magnitude 0.0125 m s^{-2}, down the slope</p>	B1 M1 A1 A1 [4]	$m \times 9.8 \times \frac{1}{80}$ where m is the mass of the object the candidate is considering. Do not award if g is missing. Evaluation need not be seen The right elements must be present consistent with the candidate's component of the weight down the slope. No extra forces allowed Cao but allow an answer rounding to -0.012 or -0.013 following earlier premature rounding. The negative sign must be interpreted so "Down the slope" or "decelerating" must be seen

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7	(iv)	<p>Taking the train as a whole, Force down the slope = Resistance force</p> $800\,000 \times 9.8 \times \sin \beta = 33\,000$ $\beta = 0.24^\circ$	<p>M1</p> <p>A1</p> <p>A1</p> <p>[3]</p>	<p>Equilibrium of whole train required The evidence for this mark may be obtained from a correct force diagram Allow missing g for this mark only</p>
8	(i)	<p>A: $t = 0$, $\mathbf{r} = \begin{pmatrix} 3 \\ 2 \end{pmatrix}$, B: $t = 2$, $\mathbf{r} = \begin{pmatrix} 15 \\ 18 \end{pmatrix}$</p> $\begin{pmatrix} 15 \\ 18 \end{pmatrix} - \begin{pmatrix} 3 \\ 2 \end{pmatrix} = \begin{pmatrix} 12 \\ 16 \end{pmatrix}$ $\sqrt{12^2 + 16^2} = 20 \text{ The distance AB is 20 km.}$	<p>B1</p> <p>B1</p> <p>B1</p> <p>[3]</p>	<p>Award this mark automatically if the displacement is correct</p> <p>Finding the displacement. Follow through from position vectors for A and B</p> <p>Cao</p>
8	(ii)	$\mathbf{v} = \frac{d\mathbf{r}}{dt} = \begin{pmatrix} 6 \\ 8 \end{pmatrix} \text{ which is constant}$	<p>B1</p> <p>[1]</p>	<p>Any valid argument. Accept $\begin{pmatrix} 6 \\ 8 \end{pmatrix}$ with no comment. Do not accept $a = 0$ without explanation.</p>
8	(iii)		<p>B1</p> <p>B1</p> <p>B1</p> <p>[3]</p>	<p>Points A and B plotted correctly, with no FT from part (i), and the line segment AB for the <i>Rosemary</i>. No extra lines or curves.</p> <p>For the <i>Sage</i>, a curve between A and B. B0 for two line segments. Nothing extra. No FT from part (i).</p> <p>Passes through (9, 6)</p> <p>Condone no labels</p>