



GCE

Mathematics (MEI)

Advanced Subsidiary GCE 4761

Mechanics 1

Mark Scheme for June 2010

Q 1		mark	notes
(i)	$v^2 = 0^2 + 2 \times 9.8 \times 0.75$ $v = \pm 3.8340\dots$ so 3.83 m s^{-1} (3. s. f.)	M1 A1 A1 3	Use of $v^2 = u^2 + 2as$ with $u = 0$ and $a = \pm g$. Accept muddled units and sign errors. Allow wrong or wrongly converted units not sign errors cao [SC2 for 38.3... seen WWW and SC3 for 3.83... seen WWW]
		3	

Q 2		mark	notes
(i)	Resolving $\leftarrow 250 \sin 70 = 234.92\dots$ so 235 N (3 s. f.) $\uparrow 250 \cos 70 = 85.5050\dots$ so 85.5 N (3 s. f.)	M1 A1 A1 3	Resolving in at least 1 of horiz or vert. Accept $\sin \leftrightarrow \cos$. No extra terms. Either both expressions correct (neglect direction) or one correct in correct direction cao Both evaluated and directions correct
(ii)	$250 \div 2 = 125 \text{ N}$	B1 1	Accept $125g$ only if tension taken to be $250g$ in (i)
		4	

Q 3		mark	notes
(i)	$\begin{pmatrix} -1 \\ 14 \\ -8 \end{pmatrix} + \begin{pmatrix} 3 \\ -9 \\ 10 \end{pmatrix} + \mathbf{F} = 4 \begin{pmatrix} -1 \\ 2 \\ 4 \end{pmatrix}$ $\mathbf{F} = \begin{pmatrix} -6 \\ 3 \\ 14 \end{pmatrix}$	M1 M1 A1 A1 4	N2L. Allow sign errors in applying N2L. Do not condone $\mathbf{F} = m\mathbf{g}\mathbf{a}$. Allow one given force omitted. Attempt to add $\begin{pmatrix} -1 \\ 14 \\ -8 \end{pmatrix}$ and $\begin{pmatrix} 3 \\ -9 \\ 10 \end{pmatrix}$ Two components correct cao
(ii)	$\mathbf{v} = \begin{pmatrix} -3 \\ 3 \\ 6 \end{pmatrix} + 3 \begin{pmatrix} -1 \\ 2 \\ 4 \end{pmatrix} = \begin{pmatrix} -6 \\ 9 \\ 18 \end{pmatrix}$ so $\begin{pmatrix} -6 \\ 9 \\ 18 \end{pmatrix} \text{ m s}^{-1}$. speed is $\sqrt{(-6)^2 + 9^2 + 18^2} = 21 \text{ m s}^{-1}$.	M1 A1 M1 F1 4	$\mathbf{v} = \mathbf{u} + t\mathbf{a}$ with given \mathbf{u} and \mathbf{a} . Could go via \mathbf{s} . If integration used, require arbitrary constant (need not be evaluated) cao isw Allow -6^2 even if interpreted as -36 . Only FT their v . FT their \mathbf{v} only. [Award M1 F1 for 21 seen WWW]
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Q 4		mark	notes
(i)	Diagram for P or Q Other diagram	B1 B1 2	Must be properly labelled with arrows Must be properly labelled with arrows consistent with 1 st diagram Accept single diagram if clear.
(ii)	Let tension in rope be T N and accn $\uparrow a \text{ m s}^{-2}$ For box P: N2L \uparrow $1030 - 75g - T = 75a$ For box Q: N2L \uparrow $T - 25g = 25a$	M1 A1 A1 3	N2L applied correctly to either part. Allow $F = mga$ and sign errors. Do not condone missing or extra forces. Direction of a consistent with equation for P. [Condone taking + ve downwards in either equation. +ve direction must be consistent in both equations to receive both A1s]
(iii)	tension is 257.5 N	M1 A1 2	Solving for T their simultaneous equations with 2 variables. cao CWO
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Q 5		mark	notes
(i)	$270 - \arctan\left(\frac{6}{4}\right)$ $= 213.69\dots$ so 214°	M1 A1 2	Award for $\arctan p$ seen where $p = \pm \frac{6}{4}$ or $\frac{4}{6}$, or equivalent cao
(ii)	Need $(-4 + 3k)\mathbf{i} + (-6 - 2k)\mathbf{j} = \lambda(7\mathbf{i} - 9\mathbf{j})$ * either so $\frac{-4 + 3k}{-6 - 2k} = \frac{7}{-9}$. or equivalent $k = 6$ or $-4 + 3k = 7\lambda$ $-6 - 2k = -9\lambda$ $k = 6$ trial and error method	M1 M1 A1 A1 M1 A1 A1 4	Attempt to get LHS in the direction of $(7\mathbf{i} - 9\mathbf{j})$. Could be done by finding (tangents of) angles. Accept the use of $\lambda = 1$. Attempt to solve their *. Allow $= \frac{7}{9}, \frac{9}{7}, -\frac{9}{7}$ Expression correct Award full marks for $k = 6$ found WWW Attempt to solve their *. Must have both equations. Correct equations Award full marks for $k = 6$ found WWW M1 any attempt to find the value of k and 'test' M1 Systematic attempt in (the equivalent of) their * Award full marks for $k = 6$ found WWW
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Q6	mark	notes
(i) Vertically $y = 8t - 4.9t^2$ Horizontally $x = 12t$	M1 A1 B1 3	Use of $s = ut + 0.5at^2$ with $g = \pm 9.8, \pm 10$. Accept $u = 0$ or $14.4\dots$ or $14.4 \sin\theta$ or $u \sin\theta$ but not 12 . Allow use of $+3.6$. Accept derivation of -4.9 not clear. cao.
(ii) either Require $y = -3.6$ so $-3.6 = 8t - 4.9t^2$ Use of formula or $4.9(t-2)(t + \frac{18}{49}) = 0$ Roots are 2 and $-\frac{18}{49}$ ($= -0.367346\dots$) Horizontal distance is $12 \times 2 = 24$ so 24 m or Require $y = -3.6$ so $-3.6 = 8t - 4.9t^2$ Eliminate t between $x = 12t$ and $-3.6 = 8t - 4.9t^2$ so $0 = 3.6 + \frac{8x}{12} - \frac{4.9x^2}{144}$ Use of formula or factorise +ve root is 24 so 24m or Methods that divide the motion into sections Projection to highest point (A) Highest point to level of jetty (B) Level of jetty to sea (C) Combination of A, B and C may be used (A) 0.8163.. s; 9.7959.. m: (B) 0.816...s; 9.7959.. m (C): 0.3673... s; 4.4081... m	M1 M1 A1 M1 F1 M1 M1 A1 M1 F1 M1 M1 A1 A1 A1 5	Equating their y to ± 3.6 or equiv. Any form. A method for solving a 3 term quadratic to give at least 1 root. Allow their y and re-arrangement errors. WWW. Accept no reference to 2 nd root [Award SC3 for $t = 2$ seen WWW] FT their x and t . FT only their t (as long as it is +ve and is not obtained with sign error(s) e.g. -ve sign just dropped) Equating their y to ± 3.6 or equiv. Any form. Expressions in any form. Elimination must be complete Accept in any form. May be implied. A method for solving a 3 term quadratic to give at least 1 root. Allow their y and re-arrangement errors. FT from their quadratic after re-arrangement. Must be +ve. Attempt to find times or distances for sections that give the total horizontal distance travelled Correct method for one section to find time or distance Any time or distance for a section correct 2 nd time or distance correct (The two sections must not be A and B) cao
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Q7		mark	notes
(i)			
(A)	4 m	B1	
(B)	$12 - (-4) = 16$ m	M1 A1	Looking for distance. Need evidence of taking account of +ve and -ve displacements.
(C)	$1 < t < 3.5$	B1 B1	The values 1 and 3.5 Strict inequality
(D)	$t = 1, t = 3.5$	B1 6	Do not award if extra values given.
(ii)	$v = -8t + 8$ $a = -8$	M1 A1 F1 3	Differentiating
(iii)	$-8t + 8 = 4$ so $t = 0.5$ so 0.5 s $-8t + 8 = -4$ so $t = 1.5$ so 1.5 s	B1 B1 2	FT their v . FT their v .
(iv)	<p>method 1 Need velocity at $t = 3$ $v(3) = -8 \times 3 + 8 = -16$ either $v = \int 32 dt = 32t + C$ $v = -16$ when $t = 3$ gives $v = 32t - 112$ $y = \int (32t - 112) dt = 16t^2 - 112t + D$ $y = 0$ when $t = 3$ gives $y = 16t^2 - 112t + 192$ or $y = -16 \times (t - 3) + \frac{1}{2} \times 32 \times (t - 3)^2$</p> <p>(so $y = 16t^2 - 112t + 192$)</p> <p>method 2 Since accn is constant, the displacement y is a quadratic function. Since we have $y = 0$ at $t = 3$ and $t = 4$ $y = k(t - 3)(t - 4)$</p> <p>When $t = 3.5$, $y = -4$ so $-4 = k \times \frac{1}{2} \times -\frac{1}{2}$ so $k = 16$ (and $y = 16t^2 - 112t + 192$)</p>	B1 M1 A1 M1 A1 M1 A1 M1 A1 M1 A1 M1 A1 M1 A1 5	<p>FT their v from (ii)</p> <p>Accept $32t + C$ or $32t$. SC1 if $\int_3^4 32 dt$ attempted.</p> <p>Use of their -16 from an attempt at v when $t=3$</p> <p>FT their v of the form $pt + q$ with $p \neq 0$ and $q \neq 0$. Accept if at least 1 term correct. Accept no D.</p> <p>cao.</p> <p>Use of $s = ut + \frac{1}{2}at^2$</p> <p>Use of their -16 (not 0) from an attempt at v when $t=3$ and 32. Condone use of just t</p> <p>Use of $t \pm 3$</p> <p>cao</p> <p>Use of a quadratic function (condone no k) Correct use of roots k present</p> <p>Or consider velocity at $t = 3$ cao. Accept k without y simplified.</p>
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Q8		mark	notes
(i)	N2L i direction $150 = 250a$ $a = 0.6$ so 0.6 m s^{-2}	M1 A1 2	Use of N2L. Allow $F = mga$. Accept no reference to direction
(ii)	150 N – i direction	B1 B1 2	Allow correct description or arrow [Accept ‘– 150 in i direction’ for B1 B1]
(iii)	For force only in direction perp to i $300 \sin 40 = 450 \sin \theta$ $\theta = 25.37300\dots$ so 25.4° (3 s. f.) In i direction $300 \cos 40 + 150 + 450 \cos \theta$ $786.4017\dots$ so 786 i N (3 s. f.)	M1 B1 A1 M1 A1 A1 6	Resolution of both terms attempted. Allow $\sin \leftrightarrow \cos$ if in both terms. Allow 250 or $250g$ present. $300 \sin 40$ or $450 \sin \theta$ Accept \pm . Accept answer rounding to 25.5. Allow SC1 if seen in this part. Proper resolution attempted of 450 and 300. Allow $\sin \leftrightarrow \cos$ if in both terms. Accept use of their θ or just θ . Either resolution correct. Accept their θ or just θ . Accept \sin/\cos consistent with use for cpt perpendicular to i . Accept no reference to direction cao. Allow SC1 WW
(iv)	Using $s = ut + 0.5at^2$ $1 = 0.5a \times 2^2$ $a = 0.5$ Using N2L in i direction $786.4017\dots - F = 250 \times 0.5$ $661.4017\dots$ so 661 N (3 s. f.)	M1 A1 M1 A1 E1 5	Appropriate (sequence of) <i>suvat</i> [WW M0 A0] Use of $F = ma$ with their 786.4 and their a . No extra forces. Allow sign errors. All correct using their 786.4 and a Use of N2L clearly shown. (Accept 0.5 used WW)
(v)	Using N2L in i direction either $125 - 200 = 250a_1$ or (starting again) $786.4017\dots - (200 + 661.4017\dots) = 250 a_1$ so $a_1 = -0.3$ Using $v^2 = u^2 + 2 a_1 s$ $v^2 = 1.8^2 + 2 \times (-0.3) \times 1.65$ $v = 1.5$ so 1.5 m s^{-1}	M1 F1 M1 F1 A1 5	Use of $F = ma$ with their values. Allow 1 force missing FT only their 786... and their 661 Appropriate (sequence of) <i>suvat</i> with $u \neq 0$. Must be ‘new’ a obtained by using N2L. Only FT use of \pm their a_1 cao
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