

# Mark Scheme (Results)

June 2011

GCE Further Pure FP2 (6668) Paper 1

Edexcel is one of the leading examining and awarding bodies in the UK and throughout the world. We provide a wide range of qualifications including academic, vocational, occupational and specific programmes for employers.

Through a network of UK and overseas offices, Edexcel's centres receive the support they need to help them deliver their education and training programmes to learners.

For further information, please call our GCE line on 0844 576 0025 or visit our website at [www.edexcel.com](http://www.edexcel.com).

If you have any subject specific questions about the content of this Mark Scheme that require the help of a subject specialist, you may find our **Ask The Expert** email service helpful.

Ask The Expert can be accessed online at the following link:  
<http://www.edexcel.com/Aboutus/contact-us/>

June 2011

Publications Code UA027968

All the material in this publication is copyright

© Edexcel Ltd 2011

## EDEXCEL GCE MATHEMATICS

### General Instructions for Marking

1. The total number of marks for the paper is 75.
2. The Edexcel Mathematics mark schemes use the following types of marks:
  - **M** marks: method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
  - **A** marks: Accuracy marks can only be awarded if the relevant method (M) marks have been earned.
  - **B** marks are unconditional accuracy marks (independent of M marks)
  - Marks should not be subdivided.

### 3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes and can be used if you are using the annotation facility on ePEN.

- bod – benefit of doubt
- ft – follow through
- the symbol  $\checkmark$  will be used for correct ft
- cao – correct answer only
- cso - correct solution only. There must be no errors in this part of the question to obtain this mark
- isw – ignore subsequent working
- awrt – answers which round to
- SC: special case
- oe – or equivalent (and appropriate)
- dep – dependent
- indep – independent
- dp decimal places
- sf significant figures
- \* The answer is printed on the paper
- $\square$  The second mark is dependent on gaining the first mark

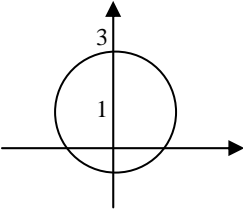
**June 2011**  
**Further Pure Mathematics FP 26668**  
**Mark Scheme**

Question Number	Scheme	Marks
<b>1.</b>	$3x = (x-4)(x+3) \quad x^2 - 4x - 12 = 0$ $x = -2, x = 6$ both Other critical values are $x = -3, x = 0$ $-3 < x < -2, \quad 0 < x < 6$	M1 A1  B1, B1 M1 A1 A1  (7) <b>7</b>
	1 <sup>st</sup> M1 for $\pm(x^2 - 4x - 12) - '=0'$ not required. B marks can be awarded for values appearing in solution e.g. on sketch of graph or in final answer. 2 <sup>nd</sup> M1 for attempt at method using graph sketch or +/- If cvs correct but correct inequalities are not strict award A1A0.	

Question Number	Scheme	Marks
<b>2.</b>  <b>(a)</b>	$\frac{d^3 y}{dx^3} = e^x \left( 2y \frac{d^2 y}{dx^2} + 2 \left( \frac{dy}{dx} \right)^2 + 2y \frac{dy}{dx} \right) + e^x \left( 2y \frac{dy}{dx} + y^2 + 1 \right)$ $\frac{d^3 y}{dx^3} = e^x \left( 2y \frac{d^2 y}{dx^2} + 2 \left( \frac{dy}{dx} \right)^2 + 4y \frac{dy}{dx} + y^2 + 1 \right) \quad (k = 4)$	M1 A1  A1  (3)
<b>(b)</b>	$\left( \frac{d^2 y}{dx^2} \right)_0 = e^0 (4 + 1 + 1) = 6$ $\left( \frac{d^3 y}{dx^3} \right)_0 = e^0 (12 + 8 + 8 + 1 + 1) = 30$ $y = 1 + 2x + \frac{6x^2}{2} + \frac{30x^3}{6} = 1 + 2x + 3x^2 + 5x^3$	B1  B1  M1 A1ft  (4) <b>7</b>
<b>(a)</b>  <b>(b)</b>	1 <sup>st</sup> M1 for evidence of Product Rule 1 <sup>st</sup> A1 for completely correct expression or equivalent 2 <sup>nd</sup> A1 for correct expression or $k = 4$ stated 2 <sup>nd</sup> M1 require four terms and denominators of 2 and 6 (might be implied) A1 follow through from their values in the final answer.	

Question Number	Scheme	Marks
3.	$\frac{dy}{dx} + 5\frac{y}{x} = \frac{\ln x}{x^2} \quad \text{Integrating factor } e^{\int \frac{5}{x}}$ $e^{\int \frac{5}{x}} = e^{5 \ln x} = x^5$ $\int x^3 \ln x dx = \frac{x^4 \ln x}{4} - \int \frac{x^3}{4} dx$ $= \frac{x^4 \ln x}{4} - \frac{x^4}{16} (+C)$ $x^5 y = \frac{x^4 \ln x}{4} - \frac{x^4}{16} + C \quad y = \frac{\ln x}{4x} - \frac{1}{16x} + \frac{C}{x^5}$	M1 A1 M1 M1 A1 A1 M1 A1 (8) <b>8</b>
	1 <sup>st</sup> M1 for attempt at correct Integrating Factor 1 <sup>st</sup> A1 for simplified IF 2 <sup>nd</sup> M1 for $\frac{\ln x}{x^2}$ times their IF to give their ' $x^3 \ln x$ ' 3 <sup>rd</sup> M1 for attempt at correct Integration by Parts 2 <sup>nd</sup> A1 for both terms correct 3 <sup>rd</sup> A1 constant not required 4 <sup>th</sup> M1 $x^5 y = \text{their answer} + C$	



Question Number	Scheme	Marks
<p><b>5.</b></p> <p><b>(a)</b></p>	$x^2 + (y-1)^2 = 4$	<p>M1 A1</p> <p>(2)</p>
<p><b>(b)</b></p>	 <p>M1: Sketch of circle A1: Evidence of correct centre and radius</p>	<p>M1 A1</p> <p>(2)</p>
<p><b>(c)</b></p>	$w = \frac{(x+iy)+i}{3+i(x+iy)} = \frac{x+i(y+1)}{(3-y)+ix}$ $= \frac{[x+i(y+1)][(3-y)-ix]}{[(3-y)+ix][(3-y)-ix]}$ <p>On <math>x</math>-axis, so imaginary part = 0: <math>(y+1)(3-y) - x^2 = 0</math>  <math>(y+1)(3-y) - x^2 = 0 \Rightarrow x^2 + (y-1)^2 = 4</math>, so <math>Q</math> is on <math>C</math></p>	<p>M1</p> <p>M1</p> <p>M1 A1 A1cso</p> <p>(5) <b>9</b></p>
<p><b>Alt. (c)</b></p>	<p>Let <math>w = u + iv</math>: <math>u = \frac{z+i}{3+iz}</math> (since <math>v = 0</math>)</p> $z = \frac{3u-i}{1-ui}$ $z-i = \frac{3u-i-i-u}{1-ui} = \frac{2(u-i)}{1-ui}$ $ z-i  = \frac{2\sqrt{u^2+1}}{\sqrt{u^2+1}} = 2, \text{ so } Q \text{ is on } C$	<p>M1</p> <p>dM1</p> <p>M1 A1</p> <p>A1cso</p>
<p><b>(a)</b> <b>(b)</b> <b>(c)</b></p>	<p>M1 Use of <math>z = x + iy</math> and find modulus Award A0 if circle doesn't intersect <math>x</math> - axis twice 1<sup>st</sup> M for subbing <math>z = x + iy</math> and collecting real and imaginary parts 2<sup>nd</sup> M for multiply numerator and denominator by their complex conjugate 3rd M for equating imaginary parts of numerator to 0 Award A1 for equation matching part (a), statement not required.</p>	



Question Number	Scheme	Marks
6.	$2 + \cos \theta = \frac{5}{2} \Rightarrow \theta = \frac{\pi}{3}$ $\frac{1}{2} \int (2 + \cos \theta)^2 d\theta = \frac{1}{2} \int (4 + 4 \cos \theta + \cos^2 \theta) d\theta$ $= \frac{1}{2} \left[ 4\theta + 4 \sin \theta + \frac{\sin 2\theta}{4} + \frac{\theta}{2} \right]$ <p>Substituting limits <math>\left( \frac{1}{2} \left[ \frac{9\pi}{6} + 4 \frac{\sqrt{3}}{2} + \frac{\sqrt{3}}{8} \right] = \frac{1}{2} \left( \frac{3\pi}{2} + \frac{17\sqrt{3}}{8} \right) \right)</math></p> $\text{Area of triangle} = \frac{1}{2} (r \cos \theta) (r \sin \theta) = \frac{1}{2} \times \frac{25}{4} \times \frac{1}{2} \times \frac{\sqrt{3}}{2} \left( = \frac{25\sqrt{3}}{32} \right)$ $\text{Area of } R = \frac{3\pi}{4} + \frac{17\sqrt{3}}{16} - \frac{25\sqrt{3}}{32} = \frac{3\pi}{4} + \frac{9\sqrt{3}}{32}$	B1 M1 M1 A1 M1 M1 A1 M1 A1  (9) <b>9</b>
	<p>1<sup>st</sup> M1 for use of <math>\frac{1}{2} \int r^2 d\theta</math> and correct attempt to expand</p> <p>2<sup>nd</sup> M1 for use of double angle formula - <math>\sin 2\theta</math> required in square brackets</p> <p>3<sup>rd</sup> M1 for substituting their limits</p> <p>4<sup>th</sup> M1 for use of <math>\frac{1}{2}</math> base x height</p> <p>5<sup>th</sup> M1 area of sector – area of triangle</p> <p>Please note there are no follow through marks on accuracy.</p>	

Question Number	Scheme	Marks
<p><b>7.</b></p> <p><b>(a)</b></p>	$\sin 5\theta = \text{Im}(\cos \theta + i \sin \theta)^5$ $5 \cos^4 \theta (i \sin \theta) + 10 \cos^2 \theta (i^3 \sin^3 \theta) + i^5 \sin^5 \theta$ $= i(5 \cos^4 \theta \sin \theta - 10 \cos^2 \theta \sin^3 \theta + \sin^5 \theta)$ $(\text{Im}(\cos \theta + i \sin \theta)^5) = 5 \sin \theta (1 - \sin^2 \theta)^2 - 10 \sin^3 \theta (1 - \sin^2 \theta) + \sin^5 \theta$ $\sin 5\theta = 16 \sin^5 \theta - 20 \sin^3 \theta + 5 \sin \theta \quad (*)$	<p>B1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>A1cso</p> <p style="text-align: right;">(5)</p>
<p><b>(b)</b></p>	$16 \sin^5 \theta - 20 \sin^3 \theta + 5 \sin \theta = 5(3 \sin \theta - 4 \sin^3 \theta)$ $16 \sin^5 \theta - 10 \sin \theta = 0$ $\sin^4 \theta = \frac{5}{8} \quad \theta = 1.095$ <p>Inclusion of solutions from <math>\sin \theta = -\sqrt[4]{\frac{5}{8}}</math></p> <p>Other solutions: <math>\theta = 2.046, 4.237, 5.188</math></p> <p><math>\sin \theta = 0 \Rightarrow \theta = 0, \theta = \pi (3.142)</math></p>	<p>M1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>B1</p> <p style="text-align: right;">(6)</p>
<p><b>(a)</b></p> <p><b>(b)</b></p>	<p>Award B if solution considers Imaginary parts and equates to <math>\sin 5\theta</math></p> <p>1<sup>st</sup> M1 for correct attempt at expansion and collection of imaginary parts</p> <p>2<sup>nd</sup> M1 for substitution powers of <math>\cos \theta</math></p> <p>1<sup>st</sup> M for substituting correct expressions</p> <p>2<sup>nd</sup> M for attempting to form equation</p> <p>Imply 3<sup>rd</sup> M if 4.237 or 5.188 seen. Award for their negative root.</p> <p>Ignore <math>2\pi</math> but 2<sup>nd</sup> A0 if other extra solutions given.</p>	<p style="text-align: right;"><b>11</b></p>







Further copies of this publication are available from  
Edexcel Publications, Adamsway, Mansfield, Notts, NG18 4FN

Telephone 01623 467467

Fax 01623 450481

Email [publication.orders@edexcel.com](mailto:publication.orders@edexcel.com)

Order Code UA027968 June 2011

For more information on Edexcel qualifications, please visit  
[www.edexcel.com/quals](http://www.edexcel.com/quals)

Pearson Education Limited. Registered company number 872828  
with its registered office at Edinburgh Gate, Harlow, Essex CM20 2JE

Ofqual



Llywodraeth Cynulliad Cymru  
Welsh Assembly Government

