













Leave blank

6. A parabola  $C$  has equation  $y^2 = 4ax$ ,  $a > 0$

The points  $P(ap^2, 2ap)$  and  $Q(aq^2, 2aq)$  lie on  $C$ , where  $p \neq 0$ ,  $q \neq 0$ ,  $p \neq q$ .

(a) Show that an equation of the tangent to the parabola at  $P$  is

$$py - x = ap^2 \tag{4}$$

(b) Write down the equation of the tangent at  $Q$ . (1)

The tangent at  $P$  meets the tangent at  $Q$  at the point  $R$ .

(c) Find, in terms of  $p$  and  $q$ , the coordinates of  $R$ , giving your answers in their simplest form. (4)

Given that  $R$  lies on the directrix of  $C$ ,

(d) find the value of  $pq$ . (2)

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