

Further Pure Mathematics FP1 (6667)

Mock paper mark scheme

Question number	Scheme	Marks
1.	<p>(a) $\mathbf{R}^2 = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$</p> <p>(b) $\mathbf{RS} = \begin{pmatrix} -1 & 0 \\ 0 & -1 \end{pmatrix}$</p> <p>(c) Rotation, 180° about O, or π about O Or enlargement, scale factor -1</p>	<p>B1</p> <p>B1 B1</p> <p>B1 B1</p> <p>(5 marks)</p>
2.	<p>Parabola, or $y^2 = 4ax$ seen</p> <p>$a = 3$ or $a = -3$ seen</p> <p>$y^2 = -12x$</p>	<p>B1</p> <p>B1</p> <p>B1</p> <p>(3 marks)</p>
3.	<p>(a) $1 + 2\sqrt{3}i - 3 + 1 + \sqrt{3}i = -1 + 3\sqrt{3}i$</p> <p>$\frac{(1 + \sqrt{3}i)(2 + \sqrt{3}i)}{(2 - \sqrt{3}i)(2 + \sqrt{3}i)} = \frac{-1 + 3\sqrt{3}i}{7}$</p>	<p>M1 A1 A1</p> <p>(3)</p> <p>M1 A1 A1</p> <p>(3)</p> <p>(6 marks)</p>
4.	<p>(a) $f(2) = -1$, $f(3) = 3$; and so $\alpha = 2 + \frac{1}{1+3} = 2.25$</p> <p>(b) $f'(x) = 3x^2 - 8x + 5$ $f'(2.5) = 3.75$ $f(2.5) = 0.125$</p> <p>(b) $\therefore u_1 = 2.5 - \frac{.125}{3.75} = 2.47$</p>	<p>B1 B1;</p> <p>M1 A1(4)</p> <p>M1</p> <p>A1</p> <p>B1</p> <p>M1 A1 (5)</p> <p>(9 marks)</p>

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5.	<p>(a) Determinant $5ab$</p> $\mathbf{X}^{-1} = \frac{1}{5ab} \begin{pmatrix} 3b & -2b \\ a & a \end{pmatrix}$ <p>(b) $\mathbf{Z} = \mathbf{YX}^{-1}$</p> $= \frac{1}{5ab} \begin{pmatrix} 10ab & -5ab \\ 5ab & 0 \end{pmatrix} = \begin{pmatrix} 2 & -1 \\ 1 & 0 \end{pmatrix}$	<p>B1</p> <p>M1 A1 (3)</p> <p>M1</p> <p>M1 A1 ft</p> <p>A1 cao (4)</p> <p>(7 marks)</p>
6.	<p>(a) $\sum 2r^3 - 6r$</p> $2 \frac{n^2}{4} (n+1)^2 - 6 \frac{n}{2} (n+1)$ $= \frac{n}{2} (n+1) [n(n+1) - 6]$ $= \frac{n}{2} (n+1) [n^2 + n - 6]$ $= \frac{n}{2} (n+1)(n+3)(n-2) \quad (*)$ <p>(b) $f(50) - f(9) = 3243600 - 3780$</p> $= 3239820$	<p>M1</p> <p>A1</p> <p>M1</p> <p>A1 cos (4)</p> <p>M1</p> <p>A1 (2)</p> <p>(6 marks)</p>
7.	<p>(a) Solve quadratic to obtain $z = -5 \pm 12i$</p> <p>(b) $z_1 = z_2 = 13$</p> <p>$\arg z_1 = 1.97$ and $\arg z_2 = -1.97$</p>	<p>M1 A1 A1</p> <p>(3)</p> <p>B1, B1</p> <p>M1 A1 A1</p> <p>(5)</p>

Question number	Scheme	Marks
(c)		B1 B1 (2)
(d)	$ \pm 24i = 24$	M1 A1 (2)
8.	<p>(a) $c^2 = 9$</p> <p>(b) $y = \frac{9}{x} \Rightarrow \frac{dy}{dx} = -\frac{9}{x^2}$</p> <p>Gradient of curve and of tangent is $-\frac{1}{t^2}$</p> <p>Gradient of normal is $-\frac{1}{\text{gradient of tangent}}$</p> <p>Equation is $y - \frac{3}{t} = t^2(x - 3t)$ giving printed answer</p> <p>(c) When $t = 2$, $y = 4x + 1.5 - 24$</p> <p>$\therefore \frac{9}{x} = 4x + 1.5 - 24$</p> <p>Attempt to solve e.g. $4x^2 - 22.5x - 9 = 0$ and formula</p> <p>or factorise $x = -\frac{3}{8}$; $y = -24$</p>	<p>B1 (1)</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>M1 A1 cso (5)</p> <p>M1 A1</p> <p>M1</p> <p>M1 A1;</p> <p>M1 A1 (7)</p> <p>(13 marks)</p>

Question number	Scheme	Marks
9.	(a) $n = 1, u_1 = 3 + 2(1 - 1) = 3$, so result true for $n = 1$ Assume true for k Then $u_{k+1} = 3(3^k + 2(3^{k-1} - 1)) + 4$ So $u_{k+1} = 3^{k+1} + 2(3^k) - 6 + 4$ $u_{k+1} = 3^{k+1} + 2(3^k) - 2 = 3^{k+1} + 2(3^k - 1)$, so result true for $k+1$, so by induction the result is true for all positive integers	B1 M1 M1 A1 A1 (5)
	(b) (i) $\mathbf{A}^1 = \begin{pmatrix} 4 & 0 \\ 3 \times 3 & 1 \end{pmatrix} = \begin{pmatrix} 4 & 0 \\ 9 & 1 \end{pmatrix}$ so result true for $n = 1$ Assume true for k Then $\mathbf{A}^{k+1} = \begin{pmatrix} 4 & 0 \\ 9 & 1 \end{pmatrix} \begin{pmatrix} 4^k & 0 \\ 3(4^k - 1) & 1 \end{pmatrix}$ $= \begin{pmatrix} 4^{k+1} & 0 \\ 9 \cdot 4^k + 3 \cdot 4^k - 3 & 1 \end{pmatrix}$ $= \begin{pmatrix} 4^{k+1} & 0 \\ 3 \cdot 4^k (3 + 1) - 3 & 1 \end{pmatrix} = \begin{pmatrix} 4^{k+1} & 0 \\ 3 \cdot 4^{k+1} - 3 & 1 \end{pmatrix}$ so result true for $k + 1$ So by induction the result is true for all positive integers	B1 B1 M1 M1 A1 M1 A1 (7)
	(ii) For $n = -1, \mathbf{A}^{-1} = \begin{pmatrix} \frac{1}{4} & 0 \\ -9 & 1 \end{pmatrix}$ This is the correct inverse of \mathbf{A} , so result is valid	M1 A1 (2)
	(14 marks)	