



GCE

# Mathematics

Advanced GCE

Unit 4737: Decision Mathematics 2

## Mark Scheme for January 2011

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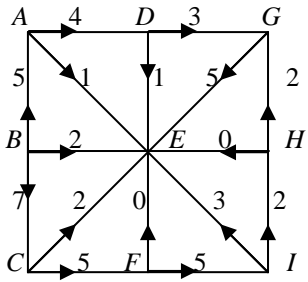
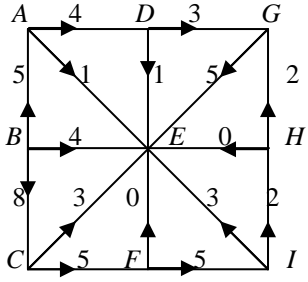
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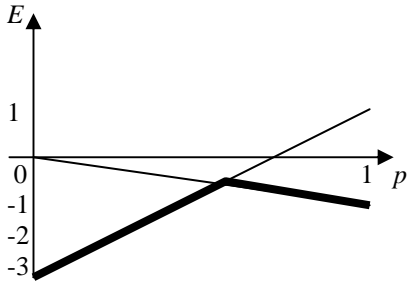
<b>1</b>	<b>(i)</b>		B1	Bipartite graph correct	[1]
	<b>(ii)</b>	$N = A - K = C - O = D$ <p>Amir sponsors the nightjar                  Bex sponsors the lark                  Ceris sponsors the kite                  Duncan sponsors the owl</p>	B1	This alternating path written down, not just read off from labels on graph	[2]
	<b>(iii)</b>	<p>Amir sponsors the nightjar                  Bex sponsors the moorhen                  Ceris sponsors the kite                  Duncan sponsors the lark</p>	B1	This matching written down in words or symbols	[1]
<b>Total = 4</b>					

2	<table border="1" style="width: 100%; border-collapse: collapse; margin-bottom: 10px;"> <thead> <tr> <th></th> <th>A</th> <th>B</th> <th>C</th> <th>D</th> </tr> </thead> <tbody> <tr> <td>Amir</td> <td>25</td> <td>15</td> <td>21</td> <td>19</td> </tr> <tr> <td>Bex</td> <td>20</td> <td>25</td> <td>16</td> <td>14</td> </tr> <tr> <td>Cerys</td> <td>25</td> <td>12</td> <td>25</td> <td>16</td> </tr> <tr> <td>Duncan</td> <td>24</td> <td>10</td> <td>18</td> <td>25</td> </tr> </tbody> </table> <p>Reduce rows</p> <table border="1" style="width: 100%; border-collapse: collapse; margin-bottom: 10px;"> <tbody> <tr> <td>A</td> <td>10</td> <td>0</td> <td>6</td> <td>4</td> </tr> <tr> <td>B</td> <td>6</td> <td>11</td> <td>2</td> <td>0</td> </tr> <tr> <td>C</td> <td>13</td> <td>0</td> <td>13</td> <td>4</td> </tr> <tr> <td>D</td> <td>14</td> <td>0</td> <td>8</td> <td>15</td> </tr> </tbody> </table> <p>Reduce columns</p> <table border="1" style="width: 100%; border-collapse: collapse; margin-bottom: 10px;"> <tbody> <tr> <td>A</td> <td>4</td> <td>0</td> <td>4</td> <td>4</td> </tr> <tr> <td>B</td> <td>0</td> <td>11</td> <td>0</td> <td>0</td> </tr> <tr> <td>C</td> <td>7</td> <td>0</td> <td>11</td> <td>4</td> </tr> <tr> <td>D</td> <td>8</td> <td>0</td> <td>6</td> <td>15</td> </tr> </tbody> </table> <p>Incomplete matching, cross through zeros</p> <table border="1" style="width: 100%; border-collapse: collapse; margin-bottom: 10px;"> <tbody> <tr> <td>A</td> <td>4</td> <td style="background-color: black;">0</td> <td>4</td> <td>4</td> </tr> <tr> <td>B</td> <td style="background-color: black;">0</td> <td>11</td> <td style="background-color: black;">0</td> <td style="background-color: black;">0</td> </tr> <tr> <td>C</td> <td>7</td> <td style="background-color: black;">0</td> <td>11</td> <td>4</td> </tr> <tr> <td>D</td> <td>8</td> <td style="background-color: black;">0</td> <td>6</td> <td>15</td> </tr> </tbody> </table> <p>Augment by 4</p> <table border="1" style="width: 100%; border-collapse: collapse; margin-bottom: 10px;"> <tbody> <tr> <td>A</td> <td>0</td> <td>0</td> <td>0</td> <td>0</td> </tr> <tr> <td>B</td> <td>0</td> <td>15</td> <td>0</td> <td>0</td> </tr> <tr> <td>C</td> <td>3</td> <td>0</td> <td>7</td> <td>0</td> </tr> <tr> <td>D</td> <td>4</td> <td>0</td> <td>2</td> <td>11</td> </tr> </tbody> </table> <p>Cannot match A to A Complete matching</p> <table border="1" style="width: 100%; border-collapse: collapse; margin-bottom: 10px;"> <thead> <tr> <th></th> <th>A</th> <th>B</th> <th>C</th> <th>D</th> </tr> </thead> <tbody> <tr> <td>Amir</td> <td>0</td> <td>0</td> <td style="background-color: black;">0</td> <td>0</td> </tr> <tr> <td>Bex</td> <td style="background-color: black;">0</td> <td>15</td> <td>0</td> <td>0</td> </tr> <tr> <td>Cerys</td> <td>3</td> <td>0</td> <td>7</td> <td style="background-color: black;">0</td> </tr> <tr> <td>Duncan</td> <td>4</td> <td style="background-color: black;">0</td> <td>2</td> <td>11</td> </tr> </tbody> </table> <p>Amir chose Cerys Bex chose Amir Cerys chose Duncan Duncan chose Bex</p>		A	B	C	D	Amir	25	15	21	19	Bex	20	25	16	14	Cerys	25	12	25	16	Duncan	24	10	18	25	A	10	0	6	4	B	6	11	2	0	C	13	0	13	4	D	14	0	8	15	A	4	0	4	4	B	0	11	0	0	C	7	0	11	4	D	8	0	6	15	A	4	0	4	4	B	0	11	0	0	C	7	0	11	4	D	8	0	6	15	A	0	0	0	0	B	0	15	0	0	C	3	0	7	0	D	4	0	2	11		A	B	C	D	Amir	0	0	0	0	Bex	0	15	0	0	Cerys	3	0	7	0	Duncan	4	0	2	11	<p>M1 Reduce rows</p> <p>A1 Correct row reduced matrix (cao) [2]</p> <p>M1 Reduce columns</p> <p>A1 Their correct column reduced matrix (ft) [2]</p> <p>M1 Cross through zeros using minimum number of lines (may be implied) and augment efficiently</p> <p>A1 Correct augmented matrix (cao) [2]</p> <p>B1 This matching (cao) [1]</p>
	A	B	C	D																																																																																																																																
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<b>Total = 7</b>																																																																																																																																				

<p>3</p>	<p>(i)</p>		<p>M1 M1d A1</p>	<p>Durations not necessary Correct structure, even without directions shown Activities must be labelled Exactly five directed dummies used correctly Completely correct, with exactly five dummies used and all arcs directed</p>	<p>[3]</p>
	<p>(ii)</p>	<p>Minimum project completion time = 14 hours Critical activities A, D, F, H</p>	<p>M1 M1 A1ft B1 B1</p>	<p>Follow through their activity network if possible Substantially correct attempt at forward pass (up to 2 independent errors) Substantially correct attempt at backward pass (up to 2 independent errors) Both passes wholly correct 14 cao ADFH cao</p>	<p>[3] [2]</p>
	<p>(iii)</p>	<p>No. of workers</p> <p>hours</p>		<p>Need not be on graph paper Axes scaled appropriately (or implied from lines) and a plausible histogram with no holes or overhangs Axes also labelled and histogram completely correct, cao</p>	<p>[2]</p>
	<p>(iv)</p>	<p>Delay G by 2 hours, so that it starts after E has finished, and delay I by 1 hour.</p>	<p>M1 A1</p>	<p>Delay G (6 to 8 → 8 to 10) Delay I by 1 hour (9 to 13 → 10 to 14) May be shown as a diagram, with activities marked so that shift of G and I can be seen</p>	<p>[2]</p>
<p><b>Total = 12</b></p>					

4	(i)	<p><math>B</math> is the source (since all flows are out at <math>B</math>)  <math>E</math> is the sink (since all flows are in at <math>E</math>)</p>	B1	<p>Both <math>B</math> and <math>E</math> (assume first answer is source)                  (reasons not needed)</p>	[1]
	(ii)	<p><math>4+4+4+5+5</math>  <math>= 22</math> litres per second</p>	M1 A1	<p>Substantially correct, using upper capacities                  22</p>	[2]
	(iii)	<p>Does not partition source from sink</p>	B1	<p>Source and sink are both in the same set</p>	[1]
	(iv)a	<p>3</p>	B1	<p>3</p>	[1]
	b	<p>At least <math>3+1 = 4</math> must flow out of <math>D</math> and 4 is the most that can flow in, so the flow must be 4</p>	B1	<p>4 must flow out of vertex <math>D</math>  <math>DG = 3</math> and <math>DE = 1</math> (at minimum)</p>	[1]
	c	<p>At least 1 must flow along <math>AE \Rightarrow BA = 5</math></p>	B1	<p>5 cao</p>	[2]
		<p>At least <math>3+2 = 5</math> must flow out of <math>I</math> so 5 must flow along <math>FI</math> and hence at least 5 must flow along <math>CF</math> and so at least <math>2+5 = 7</math> must flow along <math>BC</math></p>	M1	<p>Substantially correct, starting at <math>I</math> and tracing back along <math>IFCB</math></p>	[2]
		<p>Alternatively may use a cuts argument, eg by considering the min through arcs <math>CE, IE, IH</math></p>	A1	<p>Wholly correct reasoning  <math>CF = 5</math> and <math>CE = 2</math>, hence 7 (given)</p>	[2]
	(v)	<p>Minimum flow</p>  <p>Maximum flow</p> 	<p>Answered on insert</p> <p>M1 A1</p> <p>M1 A1</p>	<p><math>BA = 5, BC = 7</math> and <math>BE = 2</math></p> <p>This flow</p> <p>Assume blank means zero</p> <p><math>BA = 5, BC = 8</math> and <math>BE = 4</math></p> <p>This flow</p>	<p>[2]</p> <p>[2]</p>

<p>(vi)a</p>		<p>B1</p>	<p>Answered on insert</p> <p>Flow out of <math>B = 19 =</math> flow into <math>E</math>                  Flow in = flow out at <math>A, C, D, F, G, H</math> and <math>I</math></p> <p>Lower capacity <math>\leq</math> flow <math>\leq</math> upper capacity                  for every arc</p>	<p>[1]</p>
<p>b</p>	<p>Saturated arcs: <math>AD, BA, BE, CE, CF, DG, FI</math>                  Cut <math>\{B, C\}, \{A, D, E, F, G, H, I\}</math></p>	<p>B1 B1</p>	<p>These arcs, written down (and no others)                  This cut, represented in any way                  May be shown on diagram</p>	<p>[2]</p>
<p>(vii)</p>	<p>We have a flow of 19 so <math>\text{max flow} \geq 19</math>                  We have a cut of 19 so <math>\text{min cut} \leq 19</math></p> <p>Max flow = min cut                  Hence 19 is the max flow and the min cut</p> <p>Or, the cut arcs are saturated so no more can                  flow across the cut</p>	<p>B1 B1</p>	<p>Using or referring to the flow of 19 <u>and</u> cut of 19                  that <u>have been found</u></p> <p>Stating or using 'max flow = min cut'                  (eg a false cut with a flow of 19 and correct logic                  given)</p>	<p>[2]</p>
<p><b>Total = 18</b></p>				

<b>5</b>	<b>(i)</b>	<p>The number of tokens that the first player gains equals the number that the second player loses. The total number of tokens is unchanged.</p> <p>Collaboration cannot benefit both players No reason to cooperate</p>	B1	Explaining why game is zero-sum Describing a single instance not what happens in the long run	[2]																									
			B1	Describing what zero-sum means for the way in which the players play the game Not just 'one player can only gain by making the other lose'																										
	<b>(ii)</b>	<table border="1" style="margin-bottom: 10px;"> <thead> <tr> <th></th> <th>Square</th> <th>Triangle</th> <th>Circle</th> <th>Row min</th> </tr> </thead> <tbody> <tr> <th>Red</th> <td style="text-align: center;">2</td> <td style="text-align: center;">-1</td> <td style="text-align: center;">1</td> <td style="text-align: center;">-1 *</td> </tr> <tr> <th>Yellow</th> <td style="text-align: center;">-2</td> <td style="text-align: center;">0</td> <td style="text-align: center;">-3</td> <td style="text-align: center;">-3</td> </tr> <tr> <th>Blue</th> <td style="text-align: center;">-5</td> <td style="text-align: center;">1</td> <td style="text-align: center;">3</td> <td style="text-align: center;">-5</td> </tr> <tr> <th>Col max</th> <td style="text-align: center;">2</td> <td style="text-align: center;">1 *</td> <td style="text-align: center;">3</td> <td></td> </tr> </tbody> </table> <p>Col minimax is 1      Row maximin is -1</p> <p>Play-safe strategy for first player is red Play-safe strategy for second player is triangle</p> <p>Game is unstable since <math>1 \neq -1</math> row maximin <math>\neq</math> col minimax</p> <p>In a stable game, playing safe is the best strategy for each player in the long run</p> <p>In an unstable game, playing safe cannot be the best strategy for both players</p>		Square	Triangle	Circle	Row min	Red	2	-1	1	-1 *	Yellow	-2	0	-3	-3	Blue	-5	1	3	-5	Col max	2	1 *	3		M1	Finding row minima and maximin correctly (numerical values must be seen)	[3]
		Square	Triangle	Circle	Row min																									
Red	2	-1	1	-1 *																										
Yellow	-2	0	-3	-3																										
Blue	-5	1	3	-5																										
Col max	2	1 *	3																											
		M1	Finding col maxima and minimax correctly (or negatives of these), (numerical values must be seen)																											
		A1	Finding <u>Red</u> (R) and <u>Triangle</u> (T or $\Delta$ ), following both method marks gained																											
		B1	Unstable and a correct reason (may be explained in words, eg if second chooses triangle then first would do better by choosing blue)																											
		B1	Explaining what play-safe strategies mean for a stable game																											
		B1	Explaining what play-safe strategies mean for the playing of an unstable game																											
<b>(iii)</b>	<p>Red: <math>-2 &lt; -1</math> Yellow: <math>2 &lt; 3</math></p> <p>In each row the entry for square is bigger than the entry for circle, so the second player loses more by choosing square than by choosing circle.</p> <p>The second player should not choose square</p>	B1	<p>Or <math>1 &lt; 2</math> and <math>-3 &lt; -2</math></p> <p>Showing both comparisons (or equivalent) or in words</p> <p>Circle dominates square (given) as the pay-off is better (for the second player) in each row</p>	B1	Do not choose square	[2]																								
<b>(iv)</b>	<p>Triangle: <math>-1(p) + 0(1-p) = -p</math> Circle: <math>1(p) - 3(1-p) = 4p - 3</math></p>  <p><math>-p = 4p - 3 \Rightarrow p = 0.6</math></p>	B1	Both expressions correct (in any form) (may also have square: $2p - 2(1-p) = 4p - 2$ )	B1	<p>Either a <u>correct</u> sketch graph (condone missing scales and/or labels), no ft, except may have <math>4p - 2</math> as well</p> <p><u>or</u> correct reasoning (considering <math>p=0</math>, <math>p=1</math> and intersection <u>or</u> using gradients)</p> <p>Calculating intersection on its own is not enough</p>	B1	0.6 cao	[3]																						
			If circle column was removed in (iii), instead of square then ft for (iv) to $p = 0.4$																											



<p>(v)</p>	<p>The new table is</p> <table border="1" data-bbox="228 215 655 349"> <thead> <tr> <th></th> <th>Square</th> <th>Triangle</th> <th>Circle</th> </tr> </thead> <tbody> <tr> <td>Red</td> <td>2</td> <td>-1</td> <td>1</td> </tr> <tr> <td>Yellow</td> <td>-2</td> <td>0</td> <td>-3</td> </tr> <tr> <td>Blue</td> <td>5</td> <td>-1</td> <td>-3</td> </tr> </tbody> </table> <p>We add 3 throughout to make all entries non-negative</p> <table border="1" data-bbox="228 443 655 577"> <thead> <tr> <th></th> <th>Square</th> <th>Triangle</th> <th>Circle</th> </tr> </thead> <tbody> <tr> <td>Red</td> <td>5</td> <td>2</td> <td>4</td> </tr> <tr> <td>Yellow</td> <td>1</td> <td>3</td> <td>0</td> </tr> <tr> <td>Blue</td> <td>8</td> <td>2</td> <td>0</td> </tr> </tbody> </table> <p>When the second player chooses square, the first expects to win <math>5x + y + 8z</math> in this augmented table</p>		Square	Triangle	Circle	Red	2	-1	1	Yellow	-2	0	-3	Blue	5	-1	-3		Square	Triangle	Circle	Red	5	2	4	Yellow	1	3	0	Blue	8	2	0	<p>M1</p> <p>A1</p>	<p>Need not draw whole table, could just explain effect on first column.</p> <p>(Values for Blue being multiplied by -1 was given in question)</p> <p>-5 becomes 5, then add 3 to values</p> <p>This table is sufficient for the M mark</p> <p>Square, or first column, explicitly identified as giving the constraint</p>	<p>[2]</p>
	Square	Triangle	Circle																																	
Red	2	-1	1																																	
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<p>(vi)</p>	<p><math>5x + y + 8z = 3.4</math>  <math>2x + 3y + 2z = 2.4</math>  <math>4x = 2.4</math></p> <p><math>m \leq 3.4, 2.4, 2.4 \Rightarrow m \leq 2.4</math>  <math>M = m - 3 \Rightarrow M \leq -0.6</math>                  Need maximum value of <math>M \Rightarrow M = -0.6</math></p>	<p>M1</p> <p>A1</p> <p>B1</p>	<p>At least one of the values 3.4, 2.4, 2.4 correct</p> <p>All three values</p> <p>-0.6 cao</p>	<p>[3]</p>																																
<p><b>Total = 18</b></p>																																				

Answered on insert

6	(i)	10+3+2+3+17 = 35			B1	35	[1]																																																														
	(ii)	Visits the kite twice Does not visit the nightjar at all			B1	Does not visit every bird (in context)	[1]																																																														
	(iii)	18 is the suboptimal min from stage 3, state 4(13) 6 is the time taken to travel from bird 1 to bird 4 (kite to nightjar)			B1 B1	Identifying the 18 with coming from state 4(13) Identifying the 6 with kite – nightjar in table, or with 1 to 4 or 1(3) to 4(13)	[2]																																																														
	(iv)	<table border="1" style="width: 100%; border-collapse: collapse;"> <tr> <td rowspan="10" style="text-align: center; vertical-align: middle;">2</td> <td>1(4)</td> <td>2(14) 3(14)</td> <td>14+3=17 16+2=18</td> <td>17</td> </tr> <tr> <td>2(1)</td> <td>3(12) 4(12)</td> <td>20+2=22 15+4=19</td> <td>19</td> </tr> <tr> <td>2(3)</td> <td>1(23) 4(23)</td> <td>23+3=26 16+4=20</td> <td>20</td> </tr> <tr> <td>2(4)</td> <td>1(24) 3(24)</td> <td>14+3=17 12+2=14</td> <td>14</td> </tr> <tr> <td>3(1)</td> <td>2(13) 4(13)</td> <td>21+2=23 18+3=21</td> <td>21</td> </tr> <tr> <td>3(2)</td> <td>1(23) 4(23)</td> <td>23+2=25 16+3=19</td> <td>19</td> </tr> <tr> <td>3(4)</td> <td>1(34) 2(34)</td> <td>17+2=19 13+2=15</td> <td>15</td> </tr> <tr> <td>4(1)</td> <td>2(14) 3(14)</td> <td>14+4=18 16+3=19</td> <td>18</td> </tr> <tr> <td>4(2)</td> <td>1(24) 3(24)</td> <td>14+6=20 12+3=15</td> <td>15</td> </tr> <tr> <td>4(3)</td> <td>1(34) 2(34)</td> <td>17+6=23 13+4=17</td> <td>17</td> </tr> <tr> <td rowspan="4" style="text-align: center; vertical-align: middle;">1</td> <td>1</td> <td>2(1) 3(1) 4(1)</td> <td>19+3=22 21+2=23 18+6=24</td> <td>22</td> </tr> <tr> <td>2</td> <td>1(2) 3(2) 4(2)</td> <td>21+3=24 19+2=21 15+4=19</td> <td>19</td> </tr> <tr> <td>3</td> <td>1(3) 2(3) 4(3)</td> <td>24+2=26 20+2=22 17+3=20</td> <td>20</td> </tr> <tr> <td>4</td> <td>1(4) 2(4) 3(4)</td> <td>17+6=23 14+4=18 15+3=18</td> <td>18</td> </tr> <tr> <td>0</td> <td>0</td> <td>1 2 3 4</td> <td>22+10=32 19+14=33 20+12=32 18+17=35</td> <td>32</td> </tr> </table>			2	1(4)	2(14) 3(14)	14+3=17 16+2=18	17	2(1)	3(12) 4(12)	20+2=22 15+4=19	19	2(3)	1(23) 4(23)	23+3=26 16+4=20	20	2(4)	1(24) 3(24)	14+3=17 12+2=14	14	3(1)	2(13) 4(13)	21+2=23 18+3=21	21	3(2)	1(23) 4(23)	23+2=25 16+3=19	19	3(4)	1(34) 2(34)	17+2=19 13+2=15	15	4(1)	2(14) 3(14)	14+4=18 16+3=19	18	4(2)	1(24) 3(24)	14+6=20 12+3=15	15	4(3)	1(34) 2(34)	17+6=23 13+4=17	17	1	1	2(1) 3(1) 4(1)	19+3=22 21+2=23 18+6=24	22	2	1(2) 3(2) 4(2)	21+3=24 19+2=21 15+4=19	19	3	1(3) 2(3) 4(3)	24+2=26 20+2=22 17+3=20	20	4	1(4) 2(4) 3(4)	17+6=23 14+4=18 15+3=18	18	0	0	1 2 3 4	22+10=32 19+14=33 20+12=32 18+17=35	32	M1 A1 M1 A1	Action column correct for stage 2 (at least 14 of the 20 correct) All suboptimal min values transferred correctly from stage 3 All times transferred correctly from table for stage 2 All suboptimal min column correct for stage 2
2	1(4)	2(14) 3(14)	14+3=17 16+2=18	17																																																																	
	2(1)	3(12) 4(12)	20+2=22 15+4=19	19																																																																	
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	4(1)	2(14) 3(14)	14+4=18 16+3=19	18																																																																	
	4(2)	1(24) 3(24)	14+6=20 12+3=15	15																																																																	
	4(3)	1(34) 2(34)	17+6=23 13+4=17	17																																																																	
1	1	2(1) 3(1) 4(1)	19+3=22 21+2=23 18+6=24	22																																																																	
	2	1(2) 3(2) 4(2)	21+3=24 19+2=21 15+4=19	19																																																																	
	3	1(3) 2(3) 4(3)	24+2=26 20+2=22 17+3=20	20																																																																	
	4	1(4) 2(4) 3(4)	17+6=23 14+4=18 15+3=18	18																																																																	
0	0	1 2 3 4	22+10=32 19+14=33 20+12=32 18+17=35	32																																																																	
		<p>Kite – lark – nightjar – moorhen (or moorhen – nightjar – lark – kite)</p> <p>Minimum journey time = 32 minutes</p>			B1 B1	Follow through their suboptimal min values from stage 2 for the method marks Suboptimal min values transferred correctly from stage 2 Suboptimal min column correct for stage 1 from their stage 2 values Totally correct table (cao) cao (names must be used, allow letters but not numbers)	[3] [2]																																																														
						32 cao	[2]																																																														
<b>Total = 13</b>																																																																					

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