



### **General Certificate of Education**

## **Mathematics 6360**

MD02 Decision 2

# **Mark Scheme**

2009 examination - June series

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation meeting attended by all examiners and is the scheme which was used by them in this examination. The standardisation meeting ensures that the mark scheme covers the candidates' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for the standardisation meeting each examiner analyses a number of candidates' scripts: alternative answers not already covered by the mark scheme are discussed at the meeting and legislated for. If, after this meeting, examiners encounter unusual answers which have not been discussed at the meeting they are required to refer these to the Principal Examiner.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of candidates' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

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М	mark is for method						
m or dM	mark is dependent on one or more M marks and is for method						
А	mark is dependent on M or m marks and is for accuracy						
В	mark is independent of M or m marks and is for method and accuracy						
Е	mark is for explanation						
$\sqrt{100}$ or ft or F	follow through from previous						
	incorrect result	MC	mis-copy				
CAO	correct answer only	MR	mis-read				
CSO	correct solution only	RA	required accuracy				
AWFW	anything which falls within	FW	further work				
AWRT	anything which rounds to	ISW	ignore subsequent work				
ACF	any correct form	FIW	from incorrect work				
AG	answer given	BOD	given benefit of doubt				
SC	special case	WR	work replaced by candidate				
OE	or equivalent	FB	formulae book				
A2,1	2 or 1 (or 0) accuracy marks	NOS	not on scheme				
–x EE	deduct x marks for each error	G	graph				
NMS	no method shown	с	candidate				
PI	possibly implied	sf	significant figure(s)				
SCA	substantially correct approach	dp	decimal place(s)				

#### Key to mark scheme and abbreviations used in marking

#### No Method Shown

Where the question specifically requires a particular method to be used, we must usually see evidence of use of this method for any marks to be awarded. However, there are situations in some units where part marks would be appropriate, particularly when similar techniques are involved. Your Principal Examiner will alert you to these and details will be provided on the mark scheme.

Where the answer can be reasonably obtained without showing working and it is very unlikely that the correct answer can be obtained by using an incorrect method, we must award **full marks**. However, the obvious penalty to candidates showing no working is that incorrect answers, however close, earn **no marks**.

Where a question asks the candidate to state or write down a result, no method need be shown for full marks.

Where the permitted calculator has functions which reasonably allow the solution of the question directly, the correct answer without working earns **full marks**, unless it is given to less than the degree of accuracy accepted in the mark scheme, when it gains **no marks**.

#### Otherwise we require evidence of a correct method for any marks to be awarded.

MD02				1
Q	Solution	Marks	Total	Comments
1	$ \begin{array}{c} D \\ 5   4   11 \\ \hline B \\ 0   3   3 \\ \hline E \\ \hline \end{array} $	$     \frac{F}{9 2 13} $ $     \frac{G}{4 9 13} $	13	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
(a)	Network attempted (3 more activities) Up to 2 slips (boxes or connections) Correct network	M1 A1 A1	3	SCA Condone missing arrows if sequence is clear
(b)(i)	Forward pass Correct	M1 A1	2	up to 1 slip ft
( <b>ii</b> )	Backward pass Correct	M1 A1	2	up to 1 slip ft
( <b>c</b> )	Minimum completion time 22 days	B1		Must be stated – not simply in <i>K</i> box
	Critical path <i>B E G H I K</i>	B1	2	and no others
( <b>d</b> )( <b>i</b> )	New start time for <i>H</i> is 15 days New start time for <i>I</i> is 16 days	M1 A1	2	For <i>H</i> , their ( <i>F</i> earliest time 9) + $(2 + 4)$ both correct
( <b>ii</b> )	Minimum delay is 2 days	B1	1	Condone new completion time 24 days
	Total		12	

Q	Solution	Marks	Total	Comments
<b>2(a)</b>	(For each outcome)			
	Rowena's gain + Colin's gain = $0$	E1	1	One player's loss is other's gain
<b>(b)</b>	(Column maxima 2, 5, 4)			Withhold E mark if any value
~ /	$\Rightarrow \min(\operatorname{col}\max)=2$ (OE but strict)	E1		incorrect; accept column minimax = 2
	$\Rightarrow$ Colin's play-safe strategy is $C_1$	B1	2	
(c)	$R_{3}$ is dominated by $R_{1}$	E1	1	-5 < -4; 4 < 5 and 3 < 4
				E0 if $R_2$ mentioned as well
( <b>d</b> )	Let Rowena play $R_1$ with prob $p$			
	and $R_2$ with prob $1-p$			
	Expected gain when Colin plays			
	$C_1: -4p + 2(1-p) = 2 - 6p$			
	$C_2: 5p - 3(1 - p) = -3 + 8p$	M1		attempt at least 2 with one correct
	$C_3: 4p - (1-p) = -1 + 5p$	A1		all 3 correct unsimplified
	Plot expected gains against <i>p</i> for $0 \le p \le 1$	M1		All 3 drawn ft their exp gains
	The expected gams against p for $0 \le p \le 1$	1011		An 5 drawn it then exp gains
	$ \begin{array}{c} 2 \\ 1 \\ 0 \\ -1 \\ -2 \\ -3 \\ \end{array} $	A1		correct
	$\Rightarrow 2-6p = -3+8p$	M1		Using "correct" equation Choosing highest point of region
	$\Rightarrow p = \frac{5}{14}$	A1		
	Therefore Rowena plays $R_1$ with prob $\frac{5}{14}$	E1√	7	ft their p
	and $R_2$ with prob $\frac{9}{14}$			F
	Total		11	

Q	Solution	Marks	Total	Comments
3(a)	Hungarian algorithm minimises. 17-x gives measure of criteria not met	E1		Or changes maximising to minimising problem
	(which need minimising in order to maximise scores)	E1	2	Explanation of what each new entry or 17- <i>x</i> represents (as something which ca be minimised)
(b)	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	B1		array with $17 - x$ values
	0 0 4 3 0 0 0 3 3 0 4 3 5 0 2 4 3 4 0 2	M1		reduce rows first – condone one slip
	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	A1	3	then columns; AG
( <b>c</b> )	Top and bottom rows and 1 <sup>st</sup> & 4 <sup>th</sup> columns covered	B1		Zeros covered with 2 horizontal and 2 vertical lines
	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	M1		augment by subtracting 2 from each uncovered and adding 2 to each double covered – condone one slip (may earn in different lines are drawn)
	5 1 0 4 0	A1CSO	3	
( <b>d</b> )	T1, R2, V3, U4, S5 T1, U2, V3, S4, R5	M1 A1 M1		3 items correctly matched First matching correct 3 items correct in second matching
		A1	4	Second matching correct and no other matches attempted
(e)	Maximum total score = 74	B1	1	
. /	Tot	ıl	13	

Q	t) Solution							Marks	Total	Comments
4(a)										
()	$2x + y + 4z \le 10$					B1	1	Exactly this		
(b)(i)	Pivot is 2 in <i>x</i> -column					~~~~		B1		Must be ringed or clearly indicated or
(U)(I)			s 2 m x-	<i>x</i> -column			DI		stated – <b>not</b> simply implied	
	Р	x	у	Z.	S	t	value	M1		row operations (even with incorrect pivot condone one slip
	1	0	1	8-k	0	2	20	A1		Top or 2 <sup>nd</sup> row correct using correct pivor
	0	0	$1\frac{1}{2}$	1	1	$-\frac{1}{2}$	2	A1	4	All correct (condone multiples of rows)
	0	1	$\frac{1}{2}$	2	0	$\frac{1}{2}$	5			
( <b>ii</b> )	8- <i>k</i> <	<0						M1		Their $f(k) < 0$
	$\Rightarrow k$	>8						A1	2	SC B1 for $k \ge 9$
(c)(i)	New pivot from <i>z</i> -column in second row			nd row	<b>B</b> 1√		Stated or possibly implied from tableau			
	Р	x	у	z	s	t	value	M1		row operations using "their" correct
	1	0	4	0	2	1	24	A 1		pivot condone 1 slip
	0	0	$1\frac{1}{2}$	1	1	$-\frac{1}{2}$	2	A1 A1	4	one row (other than pivotal row) correct all correct (condone multiples of rows)
				0			1			
(ii)	P=24	4						B1√		Provided no negatives in top row
	Optin	num n	low rea	ached				E1		Or $P_{\text{max}} = \dots$
	x = 1,	y = 0	0, <i>z</i> =	2				B1√`		Only ft if no more than 2 slips in final tableau
									3	
							Total		14	

Q	Solution	Marks	Total		(	Commen	its	
<b>5</b> (a)	Completing stage 2 values (condone unsimplified)	B1						
	At least 6 values at stage 3 using only "their" max <i>I</i> value from stage	M1 m1		Stage	State	From	Value	Τ
	2 All stage 3 values correct	A1		1	K	Т	7	
	Using only max at <i>D</i> , <i>E</i> , <i>F</i> , <i>G</i> from stage	M1			L	Т	8	
	3 in stage 4 (at least 3 of these values used)			2	Η	K	-2 + 7 = 5	
	All stage 4 values correct	A1			Ι	K L	4 + 7 = 11 -1 + 8 = 7	
	All stage 5 values correct and all other values correct unsimplified	A1CSO	7		J	L	5 + 8 = 13	
				3	D	H I	4 + 5 = 9 2+11 = 13	
					Ε	H I	7 + 5 = 12 -9 + 11 = 2	
					F	I J	-4+11 = 7 9+13 = 22	
					G	I J	-7+11 = 4 -8+13 = 5	
				4	A	D E F	-2+13=11 5+12 = 17 -8+22=14	
					В	E F G	-1+12=11 -7+22=15 -3+5=2	
					С	G	5 + 5 = 10	
				5	S	A B C	1+17 = 18 2+15 = 17 6+10 = 16	
(b)	Maximum profit £18m Sequence of actions SAEHKT	B1 B1	2	condone	18			
	Total		9					

PMT

MD02 (cont)	
Q	Solution

(-) Value of and $20 - 10 + 12 + 20$	nts
<b>6(a)</b> Value of cut = $30 - 10 + 12 + 20$ M1	
= 52 A1 2 Full marks for correct ar working	nswers without
(b) $AE = 9;$ B1	
EF = 5; $B1$	
FG = 4 $B1$ 3	
(c)(i) Attempt at forward and backward flows M1 At least 5 pairs correct SA 2 & 4; AB 1 & 3; BT 1 & 3	
<i>SD</i> 3 & 1 ; <i>DA</i> 0 & 3 ; <i>AE</i> 0 & 3 A1 10 pairs correct	
<i>BE</i> 0 & 7; <i>DE</i> 2 & 0; <i>ET</i> 1 & 3	
FD 2 & 1; EF 5 & 1; EG 1 & 5	
FG 1 & 2; GT 3 & 0A13all correct	
(ii) First flow augmenting path and correct May end up with	
flow on table $M1$	<b>.</b>
Table correct   A1	Γ <sup>A</sup>
Adjusting flows – forward and back M1	
Correct A1 4 $4$	
$S \xrightarrow{2 x 0} A \xrightarrow{A} \xrightarrow{A} x 0$ $S \xrightarrow{2 x 0} A \xrightarrow{A} \xrightarrow{A} x 0$ $S \xrightarrow{4 x 6} \xrightarrow{4 x 6} \xrightarrow{A x 0} B$ $S \xrightarrow{4 x 6} \xrightarrow{7 x 4} \xrightarrow{7 x 4} \xrightarrow{7 x 0} 7 x 0$	ow Or <i>SDET</i>
(d) Max flow of 44 shown on figure 5 M1 up to 2 slips	
A1 2 all correct	
S 36 A 30 B	
May have	
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	A
(e) Cut through their saturated arcs M1	
Cut passes through <i>AB</i> , <i>AE</i> , <i>DE</i> and <i>DF</i> A1 2 Or <i>BT</i> , <i>ET</i> , <i>EG</i> , and <i>FG</i>	
Total 16	
TOTAL 75	