

Centre Number						Candidate Number				
Surname										
Other Names										
Candidate Signature										

For Examiner's Use	
Examiner's Initials	
Question	Mark
1	
2	
3	
4	
5	
6	
TOTAL	



General Certificate of Education
Advanced Level Examination
January 2012

Mathematics

MD02

Unit Decision 2

Wednesday 25 January 2012 1.30 pm to 3.00 pm

For this paper you must have:

- the blue AQA booklet of formulae and statistical tables.
- You may use a graphics calculator.

Time allowed

- 1 hour 30 minutes

Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- Write the question part reference (eg (a), (b)(i) etc) in the left-hand margin.
- You must answer the questions in the spaces provided. Do not write outside the box around each page.
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work that you do not want to be marked.
- The **final** answer to questions requiring the use of calculators should be given to three significant figures, unless stated otherwise.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 75.

Advice

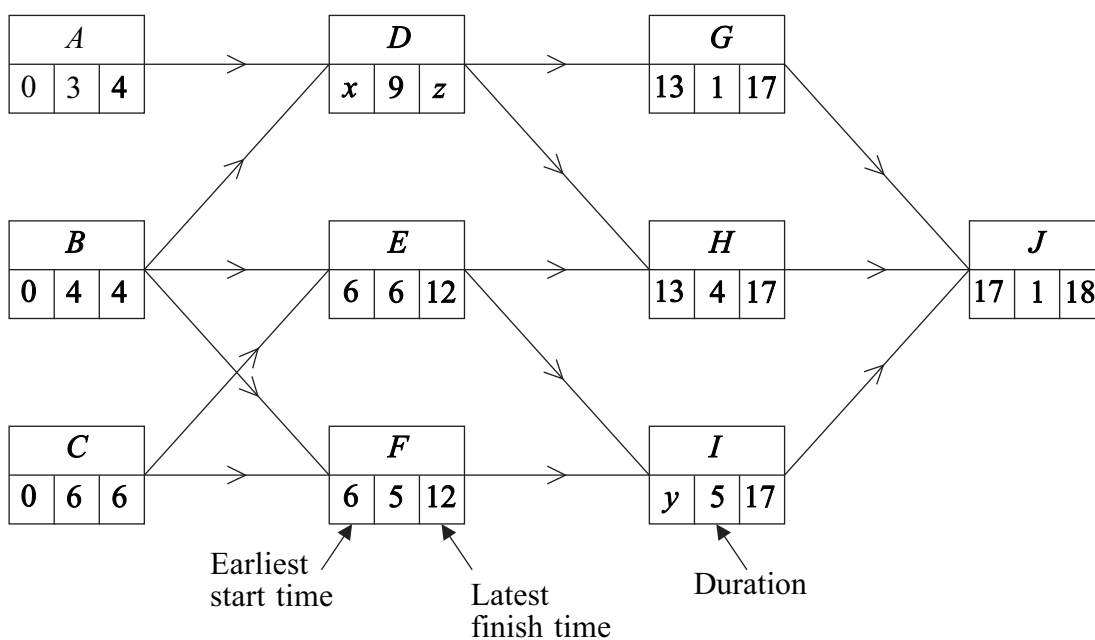
- You do not necessarily need to use all the space provided.



J A N 1 2 M D 0 2 0 1

Answer **all** questions in the spaces provided.

- 1** The diagram shows the activity network and the duration, in days, of each activity for a particular project. Some of the earliest start times and latest finish times are shown on the diagram.



- (a) Find the values of the constants x , y and z . (3 marks)
- (b) Find the critical paths. (2 marks)
- (c) Find the activity with the largest float and state the value of this float. (2 marks)

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(d) The number of workers required for each activity is shown in the table.

Activity	A	B	C	D	E	F	G	H	I	J
Number of workers required	4	2	3	4	2	4	3	3	5	6

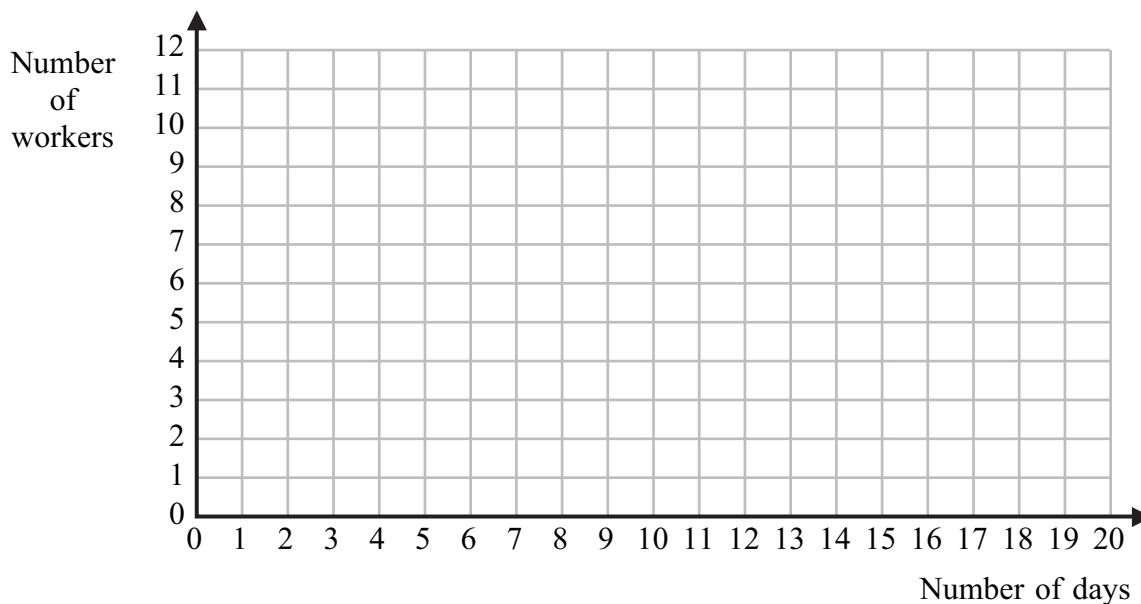
Given that each activity starts as **early** as possible and assuming that there is no limit to the number of workers available, draw a resource histogram for the project on **Figure 1** below, indicating clearly which activities are taking place at any given time. (5 marks)

(e) It is later discovered that there are only 9 workers available at any time. Use resource levelling to find the new earliest start time for activity *J* so that the project can be completed with the minimum extra time. State the minimum extra time required. (2 marks)

QUESTION PART REFERENCE

(d)

Figure 1



Turn over ►



- 2 A team with five members is training to take part in a quiz. The team members, Abby, Bob, Cait, Drew and Ellie, attempted sample questions on each of the five topics and their scores are given in the table.

	Topic 1	Topic 2	Topic 3	Topic 4	Topic 5
Abby	27	29	25	35	31
Bob	33	22	17	29	29
Cait	23	29	25	33	21
Drew	22	29	29	27	31
Ellie	27	27	19	21	27

For the actual quiz, each topic must be allocated to exactly one of the team members. The maximum total score for the sample questions is to be used to allocate the different topics to the team members.

- (a) Explain why the Hungarian algorithm may be used if each number, x , in the table is replaced by $35 - x$. (2 marks)
- (b) Form a new table by subtracting each number in the table above from 35. Hence show that, by reducing **rows first** then columns, the resulting table of values is as below, stating the values of the constants p and q .

8	6	8	0	4
0	11	p	4	4
10	4	6	0	12
q	2	0	4	0
0	0	6	6	0

(3 marks)

- (c) Show that the zeros in the table in part (b) can be covered with two horizontal and two vertical lines. Hence use the Hungarian algorithm to reduce the table to a form where five lines are needed to cover the zeros. (3 marks)
- (d) (i) Hence find the possible allocations of topics to the five team members so that the total score for the sample questions is maximised. (3 marks)
- (ii) State the value of this maximum total score. (1 mark)



3 Two people, Roz and Colum, play a zero-sum game. The game is represented by the following pay-off matrix for Roz.

		Colum		
		C₁	C₂	C₃
Roz	Strategy			
	R₁	−2	−6	−1
	R₂	−5	2	−6
	R₃	−3	3	−4

- (a) Explain what is meant by the term ‘zero-sum game’. (2 marks)

- (b) Determine the play-safe strategy for Colum, giving a reason for your answer. (2 marks)

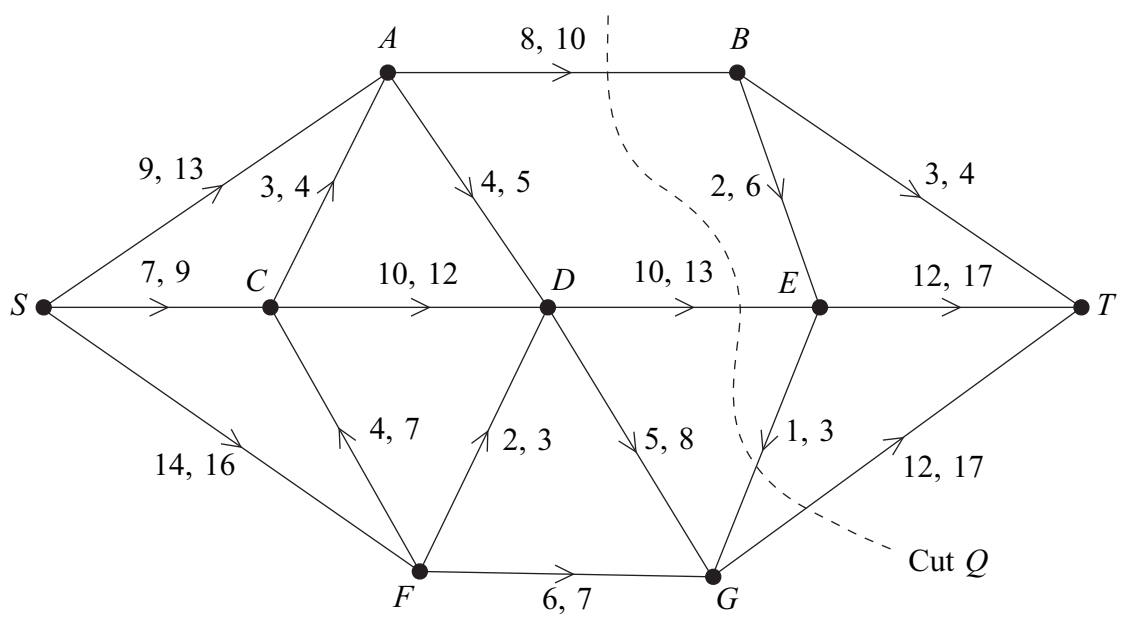
- (c) (i) Show that the matrix can be reduced to a 2 by 3 matrix, giving the reason for deleting one of the rows. (2 marks)

- (ii) Hence find the optimal mixed strategy for Roz. (7 marks)

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6 The network shows a system of pipes with the lower and upper capacities for each pipe in litres per second.



- (a) Find the value of the cut Q . (2 marks)
- (b) **Figure 2** shows most of the values of a feasible flow of 34 litres per second from S to T .
 - (i) Insert the missing values of the flows along DE and FG on **Figure 2**. (2 marks)
 - (ii) Using this feasible flow as the initial flow, indicate potential increases and decreases of the flow along each edge on **Figure 3**. (2 marks)
 - (iii) Use flow augmentation on **Figure 3** to find the maximum flow from S to T . You should indicate any flow-augmenting paths in the table and modify the potential increases and decreases of the flow on the network. (4 marks)
- (c) (i) State the value of the maximum flow. (1 mark)
- (ii) Illustrate your maximum flow on **Figure 4**. (2 marks)
- (d) Find a cut with capacity equal to that of the maximum flow. (1 mark)

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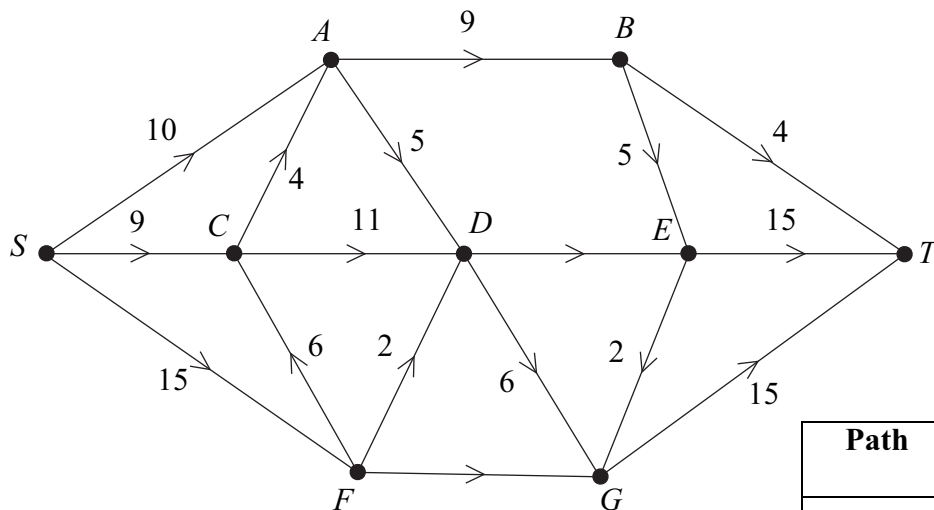
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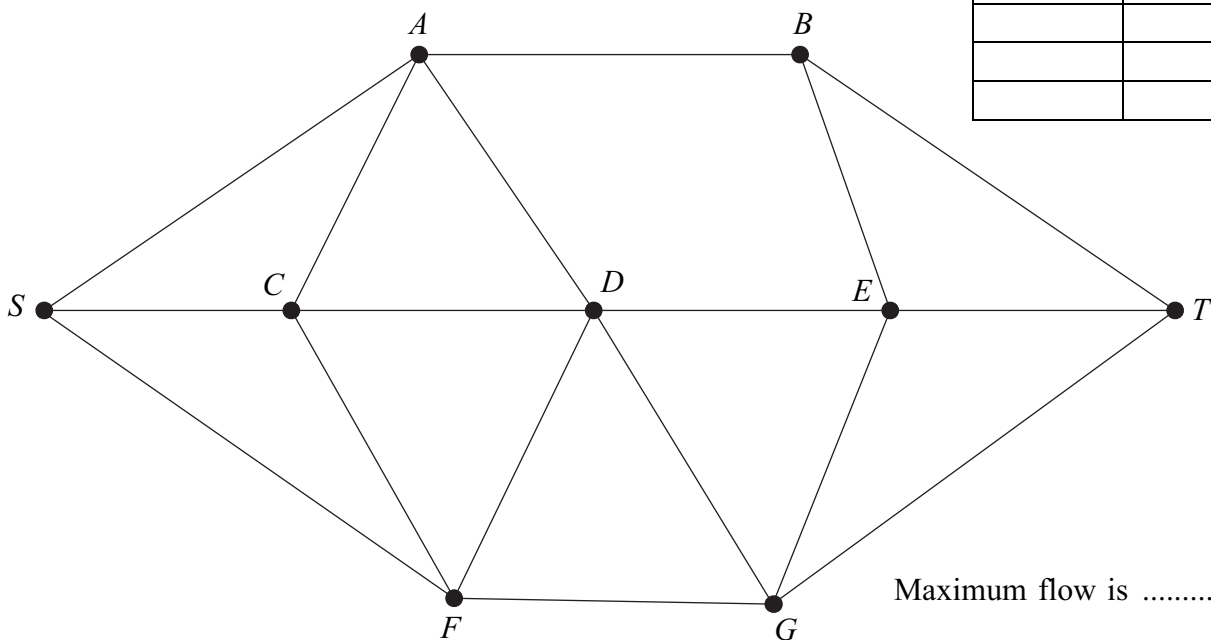


Figure 2



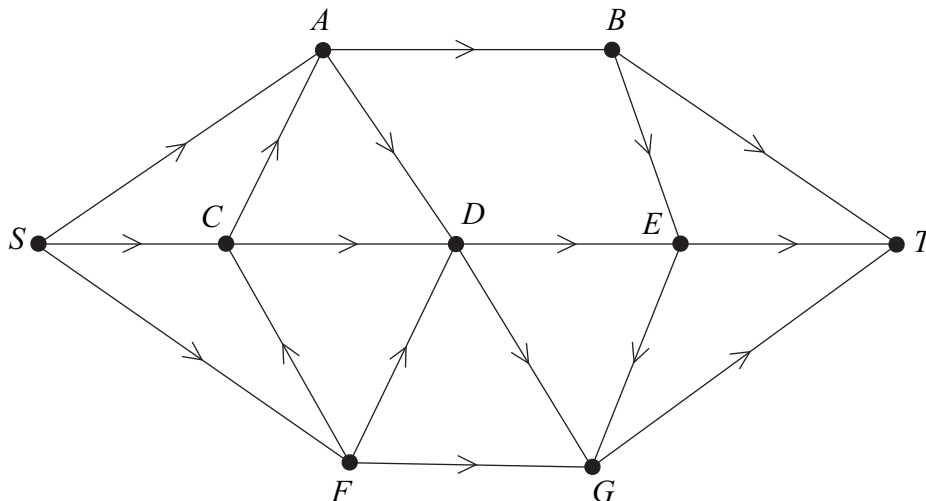
Path	Extra Flow

Figure 3



Maximum flow is

Figure 4



Turn over ►



