



GCE

Mathematics

Advanced GCE

Unit **4736**: Decision Mathematics 1

Mark Scheme for January 2011

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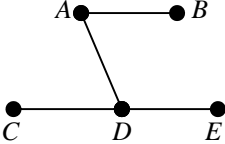
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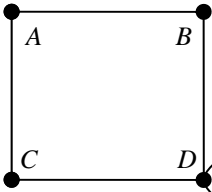
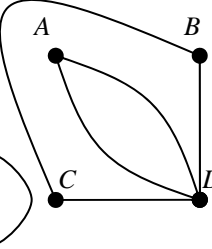
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<p>1 (i)</p>	<p>Route: $A - C - B - E - H$</p>	<p>M1 A1 M1 A1 B1</p>	<p>[5]</p>	<p>Any reasonable presentation of information</p> <p>Updating at B All temporary labels correct (and no extras)</p> <p>All permanent labels correct, cao (condone blank at A)</p> <p>Order of labelling correct, cao</p> <p>cao – or in reverse</p>	<p>Seeing 8 as a temporary label at B and 7 as a permanent label Not follow through</p> <p>Not follow through</p> <p>Not follow through</p> <p>Not follow through</p>
<p>(ii)</p>	<p>Odd nodes: B, E, G, H</p> <p>$BE + GH = 1 + 9 = 10$ $BG + EH = 7 + 7 = 14$ $BH + EG = 8 + 6 = 14$</p> <p>Minimum is 10</p>	<p>B1 M1 A1 B1</p>	<p>[4]</p>	<p>Odd nodes (may be implied from working)</p> <p>At least one correct total (10, 14, 14)</p> <p>All three pairings and correct totals seen</p> <p>10 cao</p>	<p>Using B, E, G, H and no others</p> <p>Correct method and value(s), not follow through</p> <p>Both pairings (eg BE, GH) and totals, all correct</p> <p>Unsupported 10 gets B1</p>
<p>(iii)</p>	<p>Need D and H odd, so need to consider pairings using B, D, E, G</p> <p>The minimum pairing is $BE + DG = 1 + 1 = 2$ (any other pairing must be longer)</p> <p>A possible route is $DCABEHGDGFCBEFH$</p>	<p>B1 B1 B1</p>	<p>[3]</p>	<p>Seen or implied (without having to check route)</p> <p>Repeat BE and DG <u>stated</u> (without having to check route)</p> <p>A possible route</p>	<p>Do not use their route to deduce this, it could, however be seen from their pairings</p> <p>Need to see BE, DG identified, not just $1+1=2$</p> <p>15 letters, starting at D ending at H and repeating BE and DG</p>

2	(i)	<table border="1" style="margin-left: auto; margin-right: auto;"> <thead> <tr> <th></th> <th>A</th> <th>B</th> <th>C</th> <th>D</th> <th>E</th> </tr> </thead> <tbody> <tr> <th>A</th> <td style="text-align: center;">-</td> <td style="text-align: center;">12</td> <td style="text-align: center;">30</td> <td style="text-align: center;">15</td> <td style="text-align: center;">22</td> </tr> <tr> <th>B</th> <td style="text-align: center;">12</td> <td style="text-align: center;">-</td> <td style="text-align: center;">24</td> <td style="text-align: center;">16</td> <td style="text-align: center;">30</td> </tr> <tr> <th>C</th> <td style="text-align: center;">30</td> <td style="text-align: center;">24</td> <td style="text-align: center;">-</td> <td style="text-align: center;">20</td> <td style="text-align: center;">25</td> </tr> <tr> <th>D</th> <td style="text-align: center;">15</td> <td style="text-align: center;">16</td> <td style="text-align: center;">20</td> <td style="text-align: center;">-</td> <td style="text-align: center;">10</td> </tr> <tr> <th>E</th> <td style="text-align: center;">22</td> <td style="text-align: center;">30</td> <td style="text-align: center;">25</td> <td style="text-align: center;">10</td> <td style="text-align: center;">-</td> </tr> </tbody> </table>		A	B	C	D	E	A	-	12	30	15	22	B	12	-	24	16	30	C	30	24	-	20	25	D	15	16	20	-	10	E	22	30	25	10	-	B1		Correct entries chosen on matrix (and no others)	Or with rows and columns interchanged throughout
			A	B	C	D	E																																			
		A	-	12	30	15	22																																			
		B	12	-	24	16	30																																			
C	30	24	-	20	25																																					
D	15	16	20	-	10																																					
E	22	30	25	10	-																																					
$AB = 12$ $AD = 15$ $DE = 10$ $DC = 20$		B1	B1	Arcs chosen in correct order (written down)	Must be arcs not vertices (asked for in question)																																					
57 metres		B1	B1	The correct tree, cao	Not follow through																																					
		B1	[4]	57 cao	Not follow through																																					
(ii)	Two shortest arcs from $F = BF + EF = 29 + 30 = 59$ $57 + 59$ $= 116$	M1		59 + their mst weight from (i)	Method mark may be implied from answer																																					
		A1	[2]	116 cao	Not follow through																																					
	$A - B - D - E - C - F - A$	M1		Applying nn to get $A - B - D - E - C$	Allow even if it stops at C or goes wrong after C																																					
	$12 + 16 + 10 + 25 + 31 + 32 = 126$	A1	[2]	126 cao	Method mark may be implied from 126 Not follow through																																					

3	<p>(i)</p> <p>Cannot have an odd number of odd vertices (nodes)</p> <p>(Note: the question does not say that this graph has to be simply connected)</p>	B1	[1]	<p>Three odd nodes</p> <p>Must have an even number of odd nodes</p> <p>$1+2+3+3=9$ which would mean $4\frac{1}{2}$ arcs</p>	<p>Not from a diagram of a specific case (and not from talking about what the vertices of order 3 connect to, for example)</p> <p>Not just 'sum = 9'</p>
	<p>(ii)</p> <p>Not simple</p> <p>Cannot have a vertex of order 4</p>	B1	[1]	<p>Identifying that the graph cannot be simple and an explanation that involves the vertex of order 4</p> <p>Condone 'not connected ... and not simple ...' with a valid reason for the 'not simple' part</p>	<p>If the term 'simple' is not used the answer must talk about the vertex of order 4 forcing repeated arcs or loops (allow either) or equivalent</p>
	<p>(iii)</p> <p>All nodes are even (and graph is connected)</p> <p>eg </p> <p>eg </p> <p>eg $A-B-D-D-C-A$ eg $A-D-C-B-D-A$</p>	B1	M1 A1	<p>Vertex orders all even</p> <p>A labelled connected graph with four vertices A, B, C, D with orders 2, 2, 2, 4 respectively</p> <p>A valid Eulerian trail for their graph, written down unambiguously (not just indicated on diagram)</p>	<p>2, 2, 2, 4 are all even</p> <p>Must be connected and labelled as well as having orders 2, 2, 2, 4</p> <p>May start at any vertex but must close the tour by finishing at the start vertex. May write as a list of arcs, directions not necessary</p>
	<p>(iv)(a)</p> <p>a, b and c can only take the values 0, 1 or 2</p> <p>(b)</p> <p>None of a, b and c are zero</p> <p>(c)</p> <p>Two must be odd and the other even</p>	B1 B1 B1	[3]	<p>Condone 'must be 1 or 2', condone $0 \leq a, b, c \leq 2$</p> <p>Must be less than 3</p> <p>'Not 0' or 'all positive' or equivalent</p> <p>Accept 'one ≥ 2 and others ≥ 1'</p> <p>Allow 'two odd'</p>	<p>Do not accept < 2 or $1 \leq a, b, c \leq 2$</p> <p>Allow 'must be 1 or 2' (using (a) as well as (b))</p> <p>Condone $1 \leq a, b, c \leq 2$</p> <p>Not specific values ((using (a) and (b) as well as (c) gives 1, 2, 1. This does not get this mark)</p>

4	(i)	<p>In the first pass through bubble sort we compare the first value with the second and swap if the first is larger than the second. We then compare the value that is now second with the third value and swap if the second is larger than the third. We continue like this to the end of the list.</p> <p>At this point the largest value will be in the final position and we can ignore it in subsequent passes. In the second pass we start again by comparing the first and second values, but we now only need to sort the first $n-1$ values.</p> <p>We continue in this way until either we have a list of length 1 to sort or we have a pass in which no swaps were made.</p>	M1 A1 M1 A1 B1	[5]	<p>Must be describing what happens in the general case, not just using a specific numerical example</p> <p>Compare first value with second, swap if first is larger (allow 'compare first and second')</p> <p>Then compare second with third, and so on</p> <p>Final (largest) value is in correct position</p> <p>Start again but only using first $n-1$ values</p> <p>Accept 'until no more passes are possible' or 'stop when whole list has been considered' Allow 'until only one item left' or 'until no swaps' or 'until all have permanent labels' or equivalent</p>	<p>Compare first pair and swap if needed If first is bigger than second swap them</p> <p>Describing moving along list (but not shuttling back), if any ambiguity do not give this mark</p> <p>Last value guaranteed</p> <p>Repeat but with final value already fixed</p> <p>Not just 'stop when list is sorted' Not just 'all numbers are in correct places'</p>
	(ii)	<p>Start with: 3 10 8 2 6 11 After first pass: 3 8 2 6 10 11 After second pass: 3 2 6 8 10 11 After third pass: 2 3 6 8 10 11 After fourth pass: 2 3 6 8 10 11 May label before pass is made, which will look like five passes but is OK</p>	M1 M1 A1	[3]	<p>Result of each pass must be easily found, do not imply from muddled working</p> <p>3 8 2 6 10 11 shown at end of 1st pass 2nd pass correct, follow through their list from 1st pass if possible Final list correct (cao) <u>and</u> exactly <u>four passes</u> used (depends on both method marks)</p>	<p>Misread rule (a single value miscopied or omitted from the list given in the question) will penalise the A mark only, but miscopying from one line of their working to the next could also lose one or both M marks</p>
	(iii)	<p>3 10 2 8 6 11</p>	M1 A1	[2]	<p>3 10 8 and 11 correct</p> <p>All correct, in correct order (cao)</p>	<p>In correct order of planks and cuts (could be vertical or with first at bottom line)</p>
	(iv)	<p>11 8 10 6 3 2</p> <p>Little waste from first two planks and a piece of length 18 feet from the third, which may be more useful than three medium length waste pieces</p>	B1 B1	[2]	<p>All correct, in correct order (cao)</p> <p>Unused piece 18 feet, may be more useful than three shorter pieces (5ft, 6 ft and 9 ft) left over Little waste from first two planks</p>	<p>May also see 11 10 8 6 3 2</p> <p>Referring to the lengths of the pieces left over Not 'it uses fewer cuts' (it doesn't, they both use six cuts), must have all six pieces</p>
	(v)	<p>11 6 3 10 8 2</p> <p>Two planks and four cuts</p>	B1 B1	[2]	<p>This cutting plan, planks in either order, pieces within planks in either order</p> <p>2 planks, 4 cuts or 2 planks each cut twice</p>	<p>Must have all six pieces</p> <p>Do not imply '2 planks', must be stated</p>

5	<p>(i)</p> <p>x = number of parcels per hour from new customers y = number of parcels per hour from occasional customers z = number of parcels per hour from regular customers</p>	B1	[1]	<p>Accept identifying x with new, y with occasional and z with regular with reference to 'number of parcels per hour' and 'customers' missing or wrong Condone x = new, y = occasional, z = regular</p>	<p>Do not accept if x, y and z are not separately identified, unless order is unambiguous So, 'the number if parcels from the three types of customer' or 'number of new, occasional and regular parcels' are not enough, unless supported by words like 'in that order' or 'respectively'</p>
	<p>(ii)</p> <p>Contents: $3x + 5y + 2z \leq 60$ Postage: $4x + 3y + 3z \leq 60$ Address: $3x + 4y + 3z \leq 60$</p> <p>$x \geq 0, y \geq 0, z \geq 0$</p>	B1 B1 B1 B1	[4]	<p>cao need not have identified with contents, not < cao need not have identified with postage, not < cao need not have identified with address, not <</p> <p>cao</p>	<p>Allow use of slack variables (assume slack ≥ 0) and allow scaled versions, provided they are correct</p> <p>If slack variables have been used then these must also be identified as non-negative here</p>
	<p>(iii)</p> <p>Can ignore the z term Objective function becomes $P = 8x + 7y$</p> <p>Constraints become</p> <p>$3x + 5y \leq 60$ $4x + 3y \leq 60$ $3x + 4y \leq 60$ $x \geq 0, y \geq 0$</p>	B1 B1	[2]	<p>Saying that we can ignore z (or equivalent), or writing out the objective with z removed</p> <p>Writing out all their constraints with z removed (must have at least two linear constraints that involve both x and y)</p>	<p>Need not say 'Maximise' and may omit '$P =$'</p> <p>Follow through their constraints Condone omission of non-negativity constraints</p>
	<p>(iv)</p> <p>(20, 0) (0, 12) (15, 0) (0, 20) (20, 0) (0, 15)</p>	B1 M1 A1	[3]	<p>Axes scaled and labelled appropriately</p> <p>Boundaries of all their constraints shown correctly, at least two linear constraints that involve both x and y, extending far enough for feasible region to plausibly be seen</p> <p><u>Correct</u> graph with correct shading or feasible region correct and clearly identified (cao) Need not shade $x < 0$ and $y < 0$ May also show a profit line (eg joining (0,8) to (7,0) or (0, 16) to (14, 0))</p>	<p>x and y labels (and some scale markings on both)</p> <p>Lines joining (20, 0) to (0, 12); (15, 0) to (0, 20) and (20, 0) to (0, 15) or follow through theirs</p> <p>Tolerance ± 1 little square on axes</p> <p>Not follow through for A mark</p>

	<p>Checking P at (one or more of the) vertices of their feasible region (to nearest integer or better) <u>or</u> using a profit line (of negative gradient)</p> <p>(15, 0) gives $P = 120$ (10.9, 5.45) gives $P = 125.45$ (0, 12) gives $P = 84$</p> <p>Check 10.9 parcels from new customers and 5.45 parcels from occasional customers on average each hour.</p>	M1 A1 A1	[3]	<p>May be implied from <u>correct</u> answer (to nearest integer or better)</p> <p>Optimum point correct to nearest integer or better – accept (11, 5) or (11, 6), allow (10, 6)</p> <p>Giving $(\frac{120}{11}, \frac{60}{11})$ or $(10\frac{10}{11}, 5\frac{5}{11})$ or (10.9, 5.5) or (10.9, 5.4), or better, need not be in context</p>	<p>Correct vertex marked or answer 125 (or better) for optimum value or either of (11, 5) or (11, 6) (or better) given as optimum point implies M mark Following through their graph.</p> <p>Do not follow through to a different optimal vertex for the A marks</p> <p>Allow ‘10.9 new and 5.5 occasional’ (or 5.4 or better) Allow ‘$x = 10.9$ and $y = 5.5$’ (or 5.4, or better)</p>
(v)	<p>x and y must now be integers</p> <p>(10, 6) gives $P = 122$ (11, 5) gives $P = 123$ (9, 6) gives $P = 114$ (12, 4) gives $P = 124$ (8, 7) gives $P = 113$ (13, 2) gives $P = 118$ (7, 7) gives $P = 105$ (14, 1) gives $P = 119$ (6, 8) gives $P = 104$ (15, 0) gives $P = 120$ and so on</p> <p>Check 12 parcels from new customers and 4 from occasional customers</p>	B1 M1 A1	[3]	<p>Recognising that x and y must both be integers, or implied from answer – even if this is the same as the answer to part (iv)</p> <p>Testing feasible integer points or using a profit line on <u>integer</u> feasible points, may be implied from answer being given as one of (10, 6), (11, 5) or (12, 4)</p> <p>cao, need not be in context</p>	<p>Sufficient to give <u>any</u> integer point as final solution</p> <p>Sufficient to test one integer point in their feasible region Allow grid point dots on graph</p> <p>Accept ‘12 new and 4 occasional’ or ‘$x = 12, y = 4$’</p>
(vi)	<p>May not have enough parcels of each type Cannot do two checks at the same time on the same parcel</p>	B1	[1]	<p>Any valid reason</p>	<p>Not a criticism of the values for timings or points given in the question</p>

<p>6 (i)</p>	<p>$a = 6-x, b = 8-y, c = 10-z$</p> <p>Minimise $2a - 4b + 5c - 30$ \Rightarrow minimise $12 - 2x - 32 + 4y + 50 - 5z - 30$ \Rightarrow minimise $-2x + 4y - 5z$ \Rightarrow maximise $2x - 4y + 5z$ (given)</p> <p>$3a + 2b - c \geq 10$ $\Rightarrow 3(6-x) + 2(8-y) - (10-z) \geq 10$ $\Rightarrow 3x + 2y - z \leq 14$ (given)</p> <p>$-2a + 4c \leq 35$ $\Rightarrow -2(6-x) + 4(10-z) \leq 35 \Rightarrow 2x - 4z \leq 7$ (given)</p> <p>$4a - b \leq 20$ $\Rightarrow 4(6-x) - (8-y) \leq 20 \Rightarrow -4x + y \leq 4$ (given)</p> <p>$a \leq 6 \Rightarrow x \geq 0, b \leq 8 \Rightarrow y \geq 0, c \leq 10 \Rightarrow z \geq 0$</p>	<p>B1</p> <p>M1</p> <p>A1</p>	<p>[3]</p>	<p>Replacing a, b and c in objective to get $2x - 4y + 5z$</p> <p>Replacing a, b and c in the first <u>three</u> constraints</p> <p>to get the given expressions</p> <p>Not necessary to show how $a \leq 6, b \leq 8, c \leq 10$ give $x \geq 0, y \geq 0, z \geq 0$</p>	<p>Evidence of $2(6-x) - 4(8-y) + 5(10-z)$, with or without -30 and with or without 'minimise'</p> <p>Replacing a by $6-x, b$ by $8-y$ and c by $10-z$ in <u>all three</u> constraints</p> <p>Convincingly achieving the given expressions, including dealing with the inequality signs</p>																																																																																
<p>(ii)</p>	<table border="1" data-bbox="215 815 748 975"> <thead> <tr> <th>P</th> <th>x</th> <th>y</th> <th>z</th> <th>s</th> <th>t</th> <th>u</th> <th>RHS</th> </tr> </thead> <tbody> <tr> <td>1</td> <td>-2</td> <td>4</td> <td>-5</td> <td>0</td> <td>0</td> <td>0</td> <td>0</td> </tr> <tr> <td>0</td> <td>3</td> <td>2</td> <td>-1</td> <td>1</td> <td>0</td> <td>0</td> <td>14</td> </tr> <tr> <td>0</td> <td>2</td> <td>0</td> <td>-4</td> <td>0</td> <td>1</td> <td>0</td> <td>7</td> </tr> <tr> <td>0</td> <td>-4</td> <td>1</td> <td>0</td> <td>0</td> <td>0</td> <td>1</td> <td>4</td> </tr> </tbody> </table> <table border="1" data-bbox="215 1062 748 1222"> <thead> <tr> <th>P</th> <th>x</th> <th>y</th> <th>z</th> <th>s</th> <th>t</th> <th>u</th> <th>RHS</th> </tr> </thead> <tbody> <tr> <td>1</td> <td>0</td> <td>4</td> <td>-9</td> <td>0</td> <td>1</td> <td>0</td> <td>7</td> </tr> <tr> <td>0</td> <td>0</td> <td>2</td> <td>5</td> <td>1</td> <td>-1.5</td> <td>0</td> <td>3.5</td> </tr> <tr> <td>0</td> <td>1</td> <td>0</td> <td>-2</td> <td>0</td> <td>0.5</td> <td>0</td> <td>3.5</td> </tr> <tr> <td>0</td> <td>0</td> <td>1</td> <td>-8</td> <td>0</td> <td>2</td> <td>1</td> <td>18</td> </tr> </tbody> </table> <p>New row 3 = (row 3) \div 2 (even if $-ve$ pivot) New row 1 = row 1 + 2(new row 3) New row 2 = row 2 - 3(new row 3) New row 4 = row 4 + 4(new row 3)</p> <p>Pivot row method may be implied</p>	P	x	y	z	s	t	u	RHS	1	-2	4	-5	0	0	0	0	0	3	2	-1	1	0	0	14	0	2	0	-4	0	1	0	7	0	-4	1	0	0	0	1	4	P	x	y	z	s	t	u	RHS	1	0	4	-9	0	1	0	7	0	0	2	5	1	-1.5	0	3.5	0	1	0	-2	0	0.5	0	3.5	0	0	1	-8	0	2	1	18	<p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>B1 ft</p>	<p>[2]</p> <p>[3]</p>	<p>Constraint rows correct, with three slack variable columns</p> <p>Objective row correct</p> <p>An augmented tableau with four basis columns (or three with P column missing), non-negative values in final column and value of objective having not decreased</p> <p>Correct tableau after one iteration (cao)</p> <p>Method seen and correct, any reasonable form Or: new row 1 = row 1 + original row 3 new row 2 = row 2 - 1.5 (original row 3) new row 3 = row 3 \div 2 new row 4 = row 4 + 2(original row 3)</p>	<p>Condone P column missing</p> <p>Rows and columns may appear in any order</p> <p>Slack variable columns must consist of 0's and a 1</p> <p>Not the negatives of these values (2 -4 5 0 0 0 0)</p> <p>M mark is for any tableau that satisfies these conditions and is different from the original</p> <p>Basis columns must consist of 0's and a 1</p> <p>A mark is not follow through and requires a P col</p> <p>May use 'row 3' to mean original or new row, provided consistent</p> <p>eg for row 1 allow any of + 2r3, r1+2r3, +2pr, etc or +r3, r1+r3, etc</p>
P	x	y	z	s	t	u	RHS																																																																														
1	-2	4	-5	0	0	0	0																																																																														
0	3	2	-1	1	0	0	14																																																																														
0	2	0	-4	0	1	0	7																																																																														
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0	1	0	-2	0	0.5	0	3.5																																																																														
0	0	1	-8	0	2	1	18																																																																														

<table border="1"> <thead> <tr> <th><i>P</i></th> <th><i>x</i></th> <th><i>y</i></th> <th><i>z</i></th> <th><i>s</i></th> <th><i>t</i></th> <th><i>u</i></th> <th>RHS</th> </tr> </thead> <tbody> <tr> <td>1</td> <td>0</td> <td>7.6</td> <td>0</td> <td>1.8</td> <td>-1.7</td> <td>0</td> <td>13.3</td> </tr> <tr> <td>0</td> <td>0</td> <td>0.4</td> <td>1</td> <td>0.2</td> <td>-0.3</td> <td>0</td> <td>0.7</td> </tr> <tr> <td>0</td> <td>1</td> <td>0.8</td> <td>0</td> <td>0.4</td> <td>-0.1</td> <td>0</td> <td>4.9</td> </tr> <tr> <td>0</td> <td>0</td> <td>4.2</td> <td>0</td> <td>1.6</td> <td>-0.4</td> <td>1</td> <td>23.6</td> </tr> </tbody> </table>	<i>P</i>	<i>x</i>	<i>y</i>	<i>z</i>	<i>s</i>	<i>t</i>	<i>u</i>	RHS	1	0	7.6	0	1.8	-1.7	0	13.3	0	0	0.4	1	0.2	-0.3	0	0.7	0	1	0.8	0	0.4	-0.1	0	4.9	0	0	4.2	0	1.6	-0.4	1	23.6	M1	An augmented tableau with four basis columns (or three with <i>P</i> column missing), non-negative values in final column and value of objective having not decreased from 1 st iteration	M mark is for any tableau that satisfies these conditions and is different from the original Basis columns must consist of 0's and a 1
<i>P</i>	<i>x</i>	<i>y</i>	<i>z</i>	<i>s</i>	<i>t</i>	<i>u</i>	RHS																																				
1	0	7.6	0	1.8	-1.7	0	13.3																																				
0	0	0.4	1	0.2	-0.3	0	0.7																																				
0	1	0.8	0	0.4	-0.1	0	4.9																																				
0	0	4.2	0	1.6	-0.4	1	23.6																																				
<p>New row 2 = (row 2) ÷ 5 (even if -ve pivot) New row 1 = row 1 + 9(new row 2) New row 3 = row 3 + 2(new row 2) New row 4 = row 4 + 8(new row 2)</p>	A1	Correct tableau after two iterations (cao)	A mark is not follow through and requires a <i>P</i> col																																								
Pivot row method may be implied	B1 ft	Method seen and correct, any reasonable forms Or: new row 1 = row 1 + 1.8(original row 2) new row 2 = row 2 ÷ 5 new row 3 = row 3 + 0.4(original row 2) new row 4 = row 4 + 1.6(original row 2)	May use 'row 3' to mean original or new row, provided consistent																																								
$x = 4.9, y = 0, z = 0.7 \Rightarrow a = 1.1, b = 8, c = 9.3$	B1	[3]	Correct values for <i>a</i> , <i>b</i> and <i>c</i> (cao)	Not follow through, not just the <i>x</i> , <i>y</i> and <i>z</i> values																																							
$2a - 4b + 5c - 30 = -13.3$	B1	[2]	-13.3 (cao)	<u>Not</u> +13.3																																							

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