

Question Number	Scheme	Marks
1.	$\begin{array}{ccccccccc} 6 & 1 & 18 & 12 & 9 & 0 & 5 & 13 & 14 \\ 18 & 12 & 13 & 14 & 9 & 6 & 1 & 0 & 5 \\ 18 & 14 & 13 & 12 & 9 & 6 & 1 & 5 & 0 \\ 18 & 14 & 13 & 12 & 9 & 6 & 5 & 1 & 0 \\ 18 & 14 & 13 & 12 & 9 & 6 & 5 & 1 & 0 \\ 18 & 14 & 13 & 12 & 9 & 6 & 5 & 1 & 0 \end{array}$ <p>Datchet (18), Wraysbury (14), Staines (13), Feltham (12), Halliford (9), Ashford (6), Poyle (5), Colnbrook (1), Laleham (0).</p>	M1 A1 A1 A1 A1 A1 A1 (5) (5 marks)
2. (a)	No negative elements in the profit row.	B1 (1)
(b)	$P = 11, x = 1, y = \frac{1}{3}, z = 0; r = \frac{2}{3}s = 0, t = 0$	M1 A1; A1 (3)
(c)	$P + z + s + t = 11$ $\Rightarrow P = 11 - z - s - t$ so increasing $z, s$ or $t$ would decrease $P$ .	B1 B1 (2) (6 marks)
3. (a)	$\begin{array}{ll} 1 - C & 1 - C \\ 2 - B & 2 - A \\ 3 - B & \text{and} \quad 3 - D \\ 4 - E & 4 - B \\ 5 - D & 5 - A \end{array}$	B1 B1 (2)
(b)	$2 - B = 4 - C = 1 - E$ $2 - D = 5 - E$	M1 A1 M1 A1 (4) (6 marks)

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4. (a)	<p>Shortest route <math>ABFEHI</math>, length 22 km</p>	M1 A1 A1 (3)
(b)(i)	Odd vertices A and I only, shortest route between them needs to be repeated, hence repeat $AB, BF, FE, EH, HI$	B1 B1 (2) M1 A1
(ii)	e.g. <u><math>AB\overline{FB}\overline{EF}G\overline{IF}E\overline{H}I\overline{HE}C\overline{DA}C\overline{BA}</math></u>	A1 (3)
(ii)	$91 + 22 = 113$ km	M1 A1 (2) (Marks 10)

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5. (a)	$a$	$b$	$c$	$d$	$e$	$f$	$f=0?$	
	645	255	2.53	2	510	135	No	M1 A1
	255	135	1.89	1	135	120	No	M1 A1
	135	120	1.13	1	120	15	No	A1
	120	15	8	8	120	0	Yes	A1
(b)	The answer is 15							A1 (7)
	The first row would be 255 645 0.40 0 0 255 No							M1 A1
	But the second row would then be the same as the first row above, and the solution thereafter would be the same.							A1 (3)
(c)	Finds the H.C.F of $a$ and $b$ .							B1 (1) <b>(11 marks)</b>

Question Number	Scheme	Marks
6. (a)	Critical activities $B, F, J, K, N$ (not $I$ ); length 25 hours	B1; B1 (2)
(b)	$A = 5 - 0 - 3 = 2$ $E = 9 - 3 - 4 = 2$ $L = 22 - 11 - 4 = 7$ $C = 9 - 0 - 6 = 3$ $G = 9 - 4 - 3 = 2$ $M = 22 - 16 - 2 = 4$ $D = 11 - 3 - 3 = 5$ $H = 16 - 7 - 7 = 2$ $P = 25 - 18 - 3 = 4$ $I = 16 - 9 - 5 = 2$	M1 A1 ft A1 (3)
(c)		M1 A1 A1 ft A1 ft A1 ft A1 ft
(d)	 3 workers needed Precedences: 	M1 A1 A1 (3) (12 marks)

ft = follow through mark

Question Number	Scheme	Marks
7. (a)		M1 A1 (2)
(b) (i)	$SF_1 ABR = 6$	B1
(ii)	$SF_3 CR = 8$	B1 (2)
(c)(i)		M1 A1
	e.g. $SF_1 BR = 6$ , $SF_2 BR = 3$ , $SF_2 CR = 3$ , $SF_3 R = 4$	A1 A1
	Total flow = 30	A1 (5)
(ii)	Max flow – min cut theorem	M1
	Cut $BR, F_2C, F_3C, F_3R$	A1 (2)

**(11 marks)**

Question Number	Scheme	Marks
8. (a)	$x + y \geq 380$ $y \geq 125$ $2x + 4y \leq 1200$	B1 B1 B1 (3)
(b)	$c = 3x + 2y$	B1 (1)
(c)		B1 B1 B1 B1 (4)
	Use of profit line or points testing	M1
	Minimum intersection of $x + y = 380$ and $2x + 4y = 1200$	
	$x = 160, y = 120, \text{ cost} = £920$	A1 A1 (3)
(d)	Maximum at intersection of $y = 125$ and $2x + 4y = 1200$	M1
	$x = 350, y = 125, \text{ cost} = £1300$	A1 A1 (3)
		(14 marks)