1

	(A)	B	(C)	D	E	(F)	G	(H)
A		9	8	13	17	11	12	10
В	(9)		11	21	15	24	13	7
C	(8)	-11		20	23	17	17	15
-D_	13	21	20	-	15	28	(11)	18
E	17	(15)	-23	15	-	31	23	30
F	(11)-	24	17	28	31	-	13	15
G	(12)	13	17	11	23	13		23
H	10	(7)	15	18	30	15	23	-

The table represents a network that shows the time taken, in minutes, to travel by car between eight villages, A, B, C, D, E, F, G and H.

(a) Use Prim's algorithm, starting at A, to find a minimum spanning tree for this network. You must list the arcs that form your tree in the order in which you select them.

(3)

(b) Draw your minimum spanning tree using the vertices given in Diagram 1 in the answer book and state the weight of the tree.

(2)

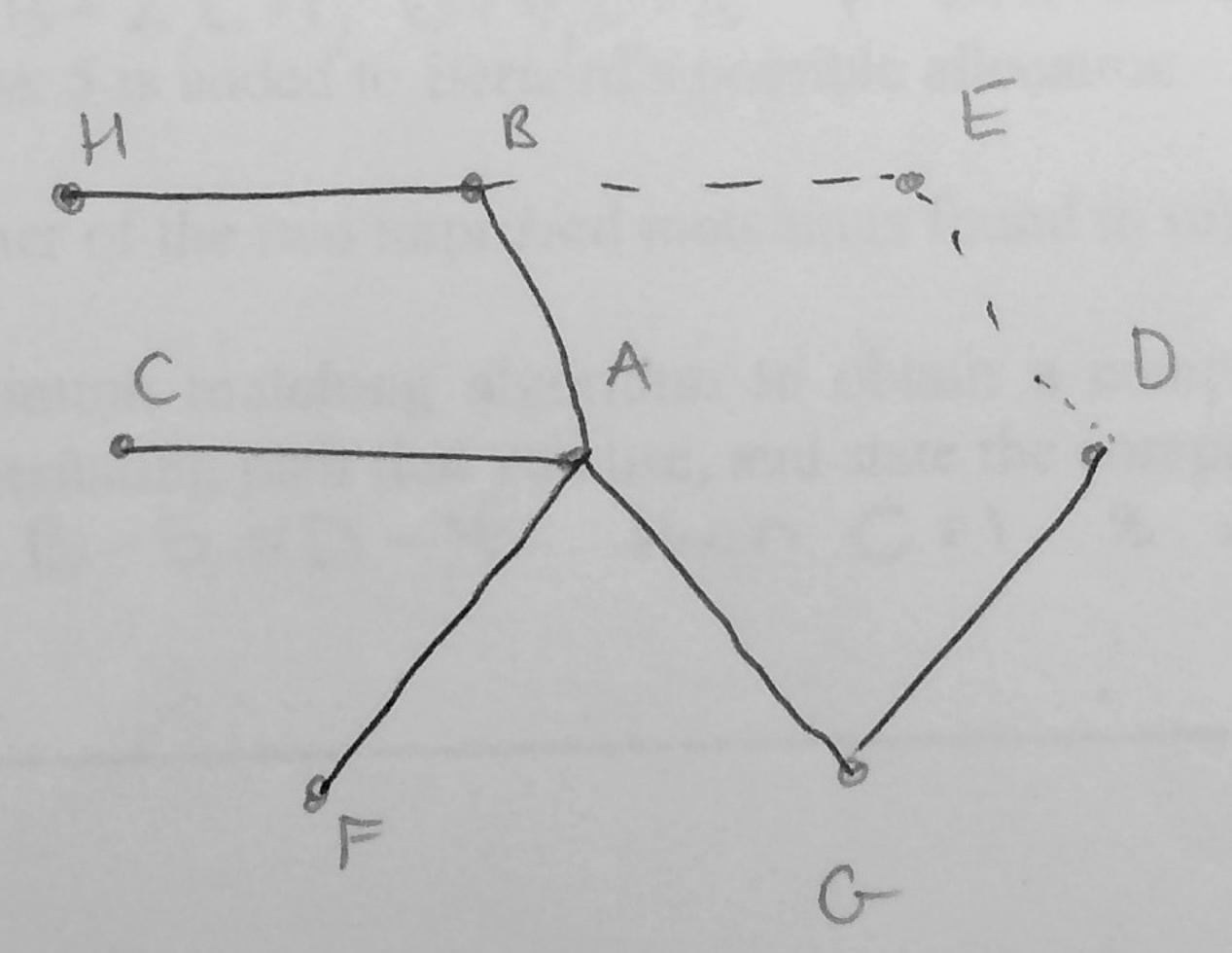
(c) State whether your minimum spanning tree is unique. Justify your answer.

(1)

(Total 6 marks)

Ilal AC AB BH AF AG DG DE BE

6



clno, 2 different trees both with a weight of 73 either with DE or BE

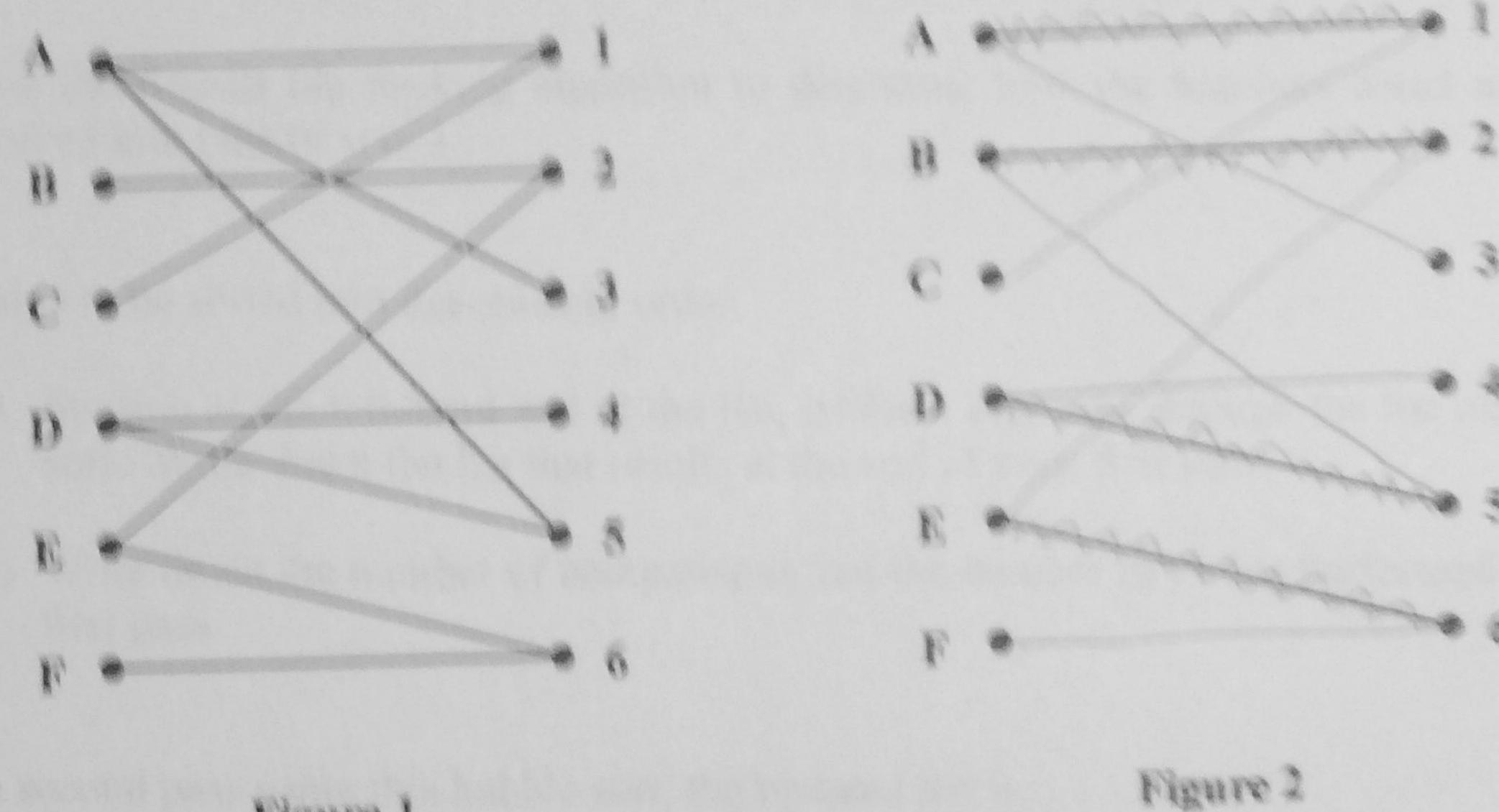


Figure 1

Figure 1 shows the possible allocations of six workers, Amrit (A), Bernard (B), Cameron (C), David (D), Emily (E) and Francis (F), to six tasks, 1, 2, 3, 4, 5 and 6

(a) Explain why it is not possible to find a complete matching.

B can only do 2, F com only do 6, E does 2 36 so no alteration (1)

Figure 2 shows an initial matching. Starting from this initial matching.

(b) find the two alternating paths that start at C.
$$C - 1 = A - 3$$
 $C - 1 = A - 5 = D - 4$ (2)

(c) List the two improved matchings generated by using the two alternating paths found in (b).

A=3, B=2, C=1, D=5, E=6 F correct voct A = 5, B = 2, C = 1, D = 4, E = 6 F connatened

After training, task 5 is added to Bernard's possible allocation.

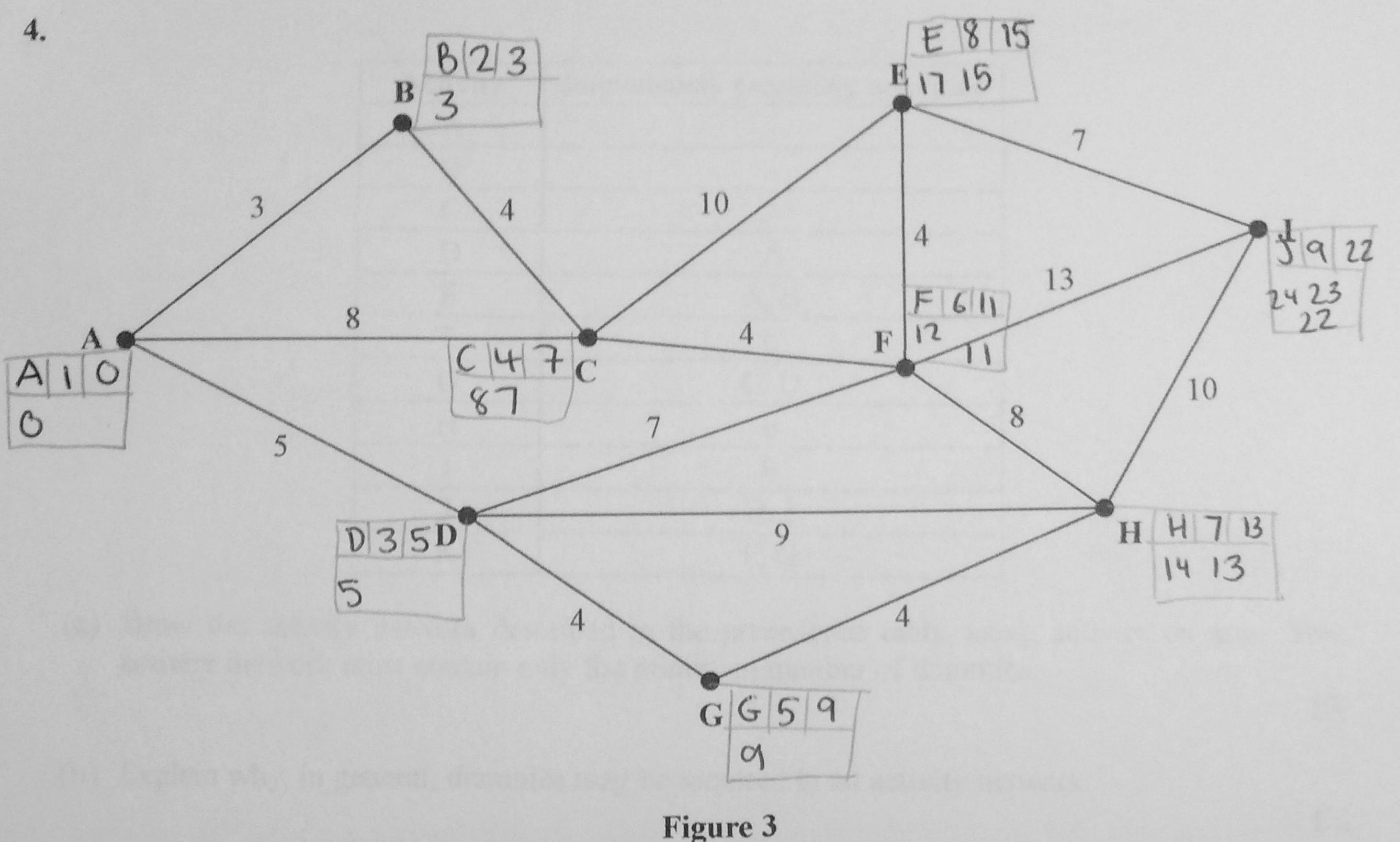
Starting from either of the two improved matchings found in (c).

(d) use the maximum matching algorithm to obtain a complete matching. You must hat the additional alternating path that you use, and state the complete matching.

additional alternating path that you use, and state the complete matter
$$E = 6 = E - 2 = B - 5 = D - 4$$
 then $C = 1 + 8 = 3$

(Total S marks)





[The total weight of the network is 100]

Figure 3 represents a network of pipes in a building. The number on each arc represents the length, in metres, of the corresponding pipe. ABCFEJ

Use Dijkstra's algorithm to find the shortest path from A to J. State your path and its length. (6)

On a particular day Kim needs to check each pipe. A route of minimum length, which traverses each pipe at least once and starts and finishes at A, needs to be found.

(b) Use an appropriate algorithm to find the arcs that will need to be traversed twice. You must At + FJ 15+11=26 make your method and working clear.

AF + EJ 11 +7 = 18 AJ + EF 22+ 4 = 26

Write down a possible route, giving its length.

100+18=118 ABADGHDFHJETF(2) ECFCBCA

All the pipes directly attached to B are removed. Kim needs to check all the remaining pipes and may now start at any vertex and finish at any vertex. A route is required that excludes all those pipes directly attached to B.

State all possible combinations of starting and finishing points so that the length of Kim's route is minimised. State the length of Kim's route.

Start at E, Finish at J 100-3-4+4=97m

(Total 16 marks)

5.

Activity	Immediately preceding activities
A	preceding activities
В	
C	
D	A
F	A
E	A, B
F	C
U	C, D
H	E
I	E
J	H, I
K	F, G

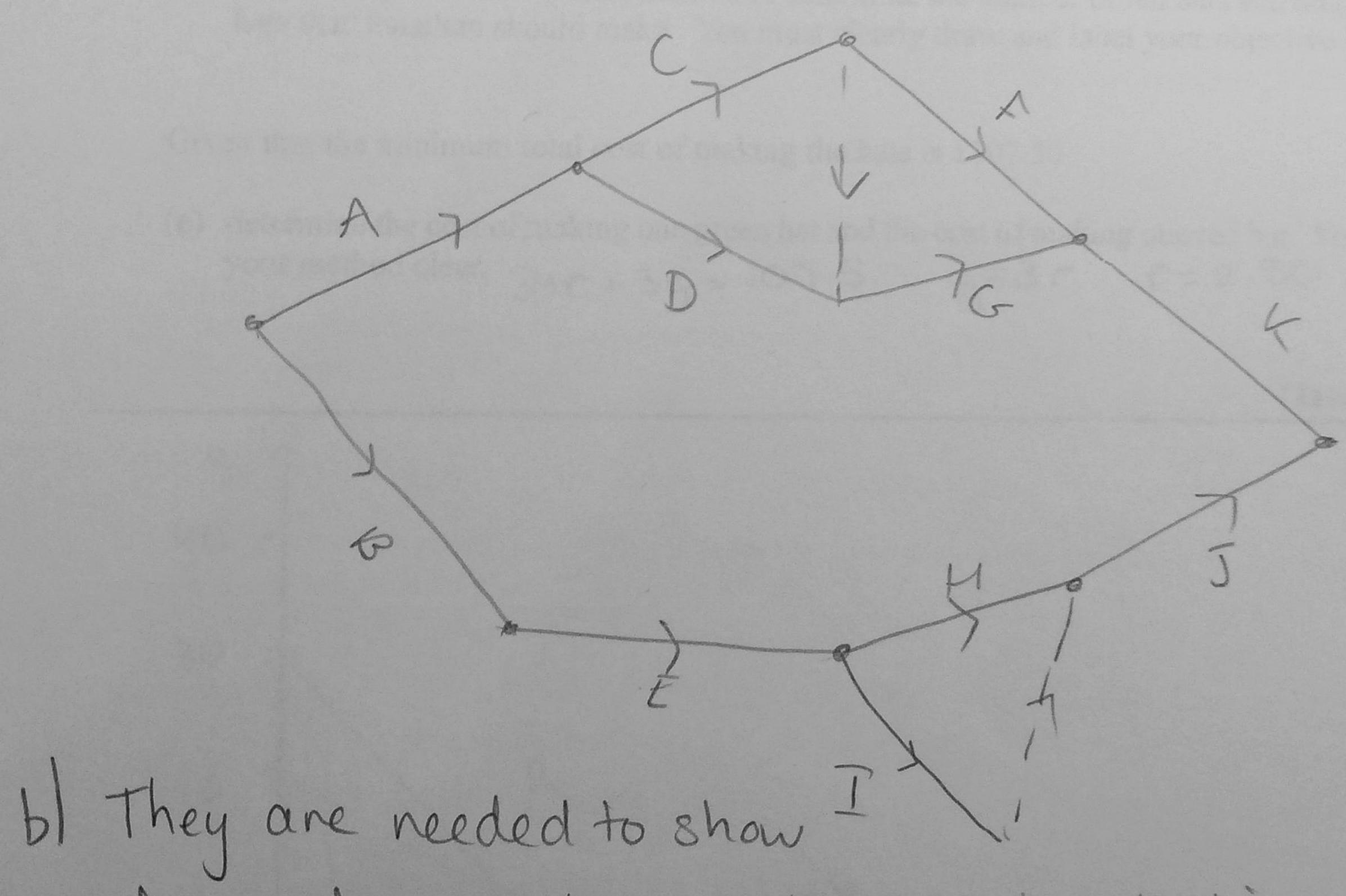
(a) Draw the activity network described in the precedence table, using activity on arc. Your activity network must contain only the minimum number of dummies.

(5)

(b) Explain why, in general, dummies may be required in an activity network.

(2)

(Total 7 marks)



- dependancy where subsequent activities do not depend on the same preceeding activities

- an activity can be uniquely represented in terms of its endevents

P45059A

6. Jonathan is going to make hats to sell at a fete. He can make red hats and green hats. Jonathan can use linear programming to determine the number of each colour of hat that he should make.

Let x be the number of red hats he makes and y be the number of green hats he makes.

One of the constraints is that there must be at least 30 hats.

(a) Write down an inequality, in terms of x and y, to model this constraint.

(1)

Two further constraints are

$$2y + x \ge 40$$

$$2y - x \ge -30$$

(b) Write down two more constraints which apply.

2C+43/30 2C/10 41/0 (1)

(c) Represent all these constraints on Diagram 1 in the answer book. Hence determine, and label, the feasible region R.

(4)

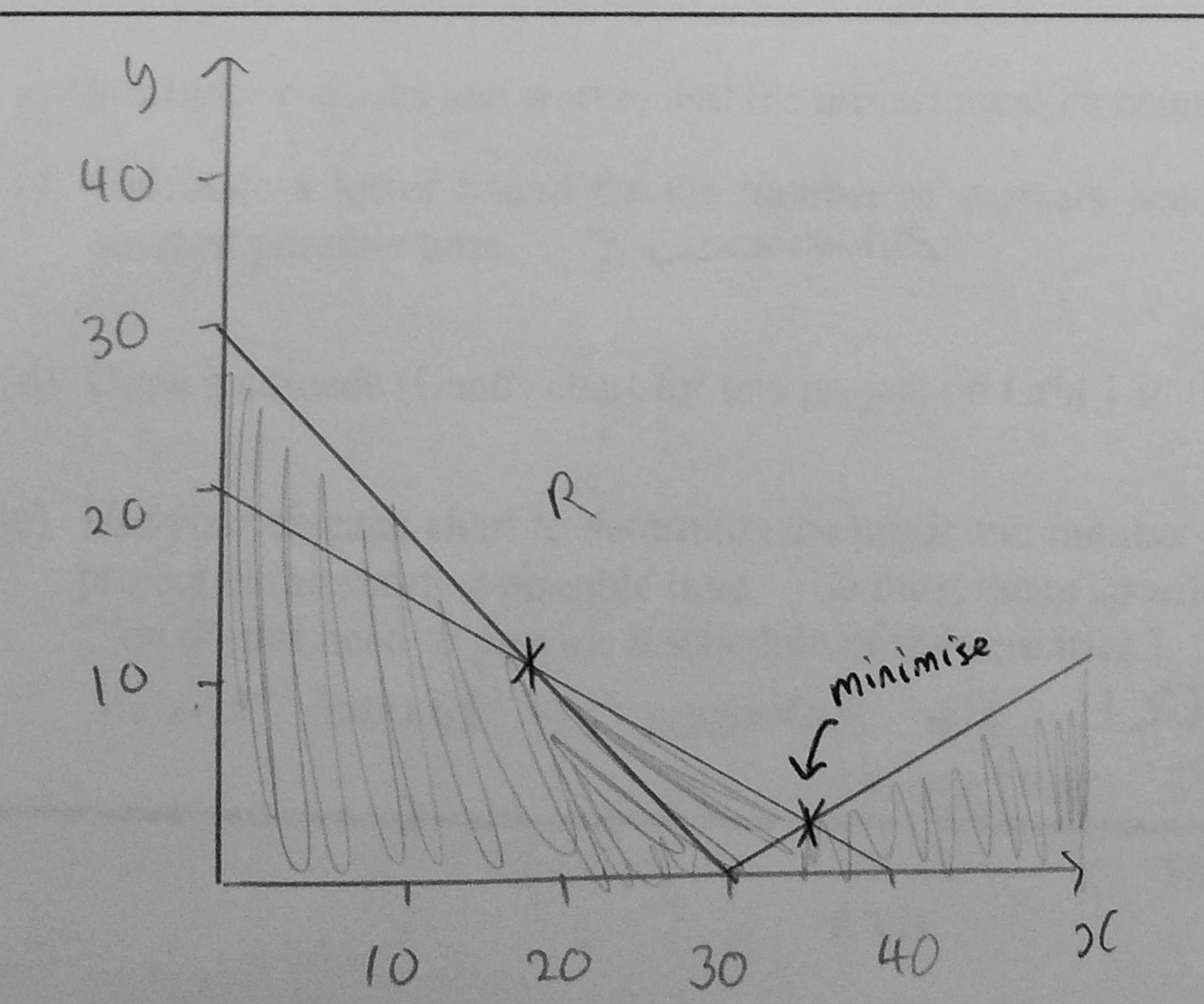
The cost of making a green hat is three times the cost of making a red hat. Jonathan wishes to minimise the total cost.

(d) Use the objective line (ruler) method to determine the number of red hats and number of green hats that Jonathan should make. You must clearly draw and label your objective line. (34,3)

Given that the minimum total cost of making the hats is £107.50

(e) determine the cost of making one green hat and the cost of making one red hat. You must make your method clear. 347 + 39 = 107.5 9 = 37 7 = 2.50 9 = 7.50

(Total 12 marks)





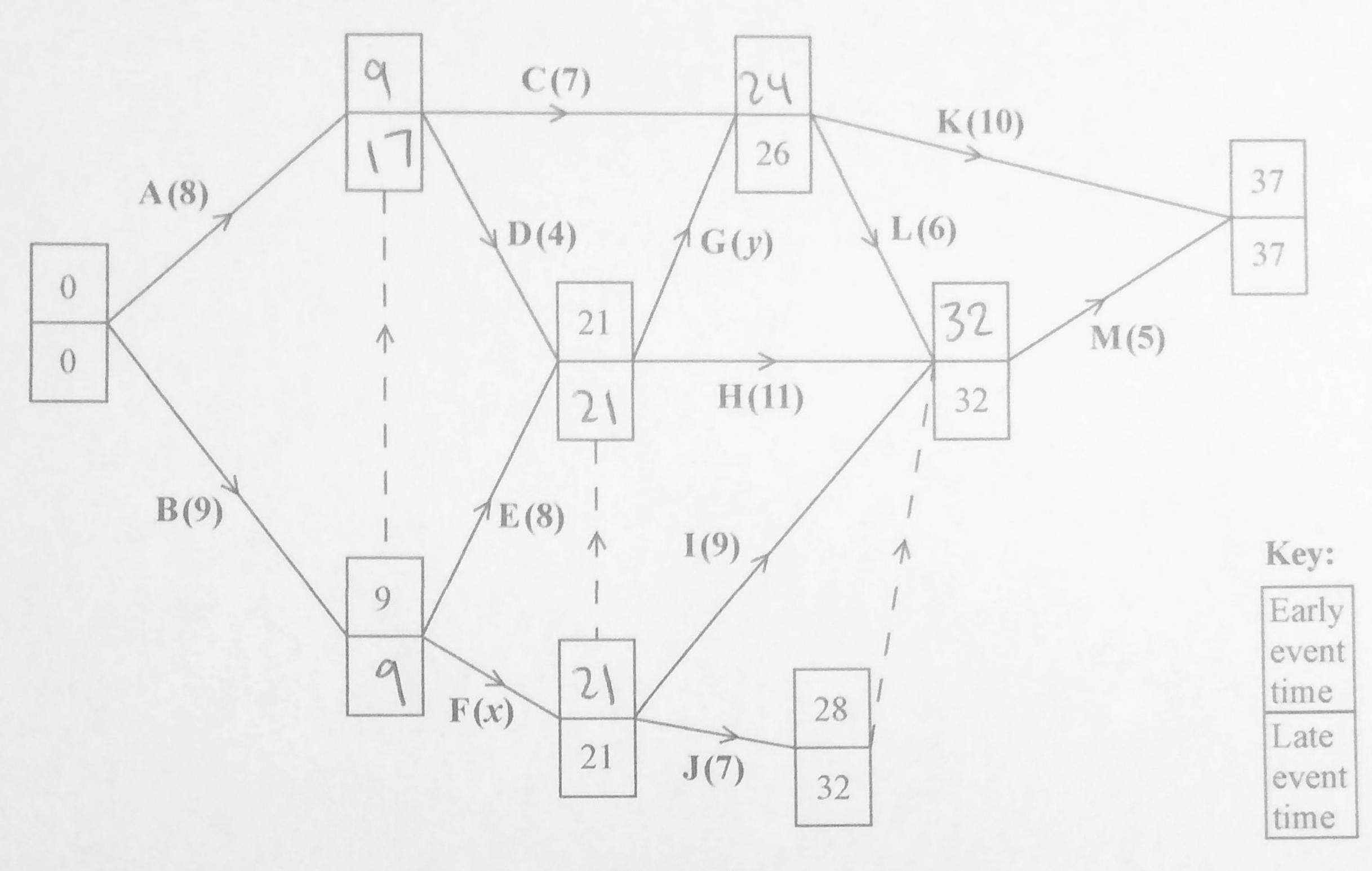


Figure 4

[The sum of all the activity durations is 99 days]

The network in Figure 4 shows the activities that need to be undertaken to complete a project. Each activity is represented by an arc and the duration of the activity, in days, is shown in brackets. The early event times and late event times are to be shown at each vertex and some have been completed for you.

Given that activity F is a critical activity and that the total float on activity G is 2 days,

(a) write down the value of x and the value of y, x=12 y=3

(2)

(b) calculate the missing early event times and late event times and hence complete Diagram 1 in your answer book.

Each activity requires one worker and the project must be completed in the shortest possible time.

- (c) Calculate a lower bound for the number of workers needed to complete the project in the shortest possible time. 3 workers (1)
- (d) Draw a cascade (Gantt) chart for this project on Grid 1 in the answer book. PTO
- (e) Use your cascade chart to determine the minimum number of workers needed to complete the project in the shortest possible time. You must make specific reference to times and activities.

 (You do **not** need to provide a schedule of the activities.)

lower bound 5 workers eg HIJKL (2) together 27 < TZ28 (Total 12 marks)