## DIFFERENTIATION

- Given that  $y = x^2 + 3x + 5$ , and that  $x = (t - 4)^3$ , **a** find expressions for **i**  $\frac{dy}{dx}$  in terms of x, **ii**  $\frac{dx}{dt}$  in terms of t, **b** find the value of  $\frac{dy}{dt}$  when **i** t = 5, **ii** x = 8.
- 2 The variables x and y are related by the equation  $y = x\sqrt{2x-3}$ . Given that wie increasing at the rate of 0.2 write per second when

Given that x is increasing at the rate of 0.3 units per second when x = 6, find the rate at which y is increasing at this instant.

- 3 The radius of a circle is increasing at a constant rate of  $0.2 \text{ cm s}^{-1}$ .
  - **a** Show that the perimeter of the circle is increasing at the rate of  $0.4\pi$  cm s<sup>-1</sup>.
  - **b** Find the rate at which the area of the circle is increasing when the radius is 10 cm.
  - **c** Find the radius of the circle when its area is increasing at the rate of  $20 \text{ cm}^2 \text{ s}^{-1}$ .
- 4 The area of a circle is decreasing at a constant rate of  $0.5 \text{ cm}^2 \text{ s}^{-1}$ .
  - **a** Find the rate at which the radius of the circle is decreasing when the radius is 8 cm.
  - **b** Find the rate at which the perimeter of the circle is decreasing when the radius is 8 cm.
- 5 The volume of a cube is increasing at a constant rate of  $3.5 \text{ cm}^3 \text{ s}^{-1}$ . Find
  - **a** the rate at which the length of one side of the cube is increasing when the volume is  $200 \text{ cm}^3$ ,
  - **b** the volume of the cube when the length of one side is increasing at the rate of  $2 \text{ mm s}^{-1}$ .



**C4** 

1



The diagram shows the cross-section of a right-circular paper cone being used as a filter funnel. The volume of liquid in the funnel is  $V \text{ cm}^3$  when the depth of the liquid is *h* cm.

Given that the angle between the sides of the funnel in the cross-section is 60° as shown,

**a** show that  $V = \frac{1}{9}\pi h^3$ .

Given also that at time t seconds after liquid is put in the funnel

 $V = 600 \mathrm{e}^{-0.0005t}$ 

- **b** show that after two minutes, the depth of liquid in the funnel is approximately 11.7 cm,
- c find the rate at which the depth of liquid is decreasing after two minutes.