

Question Number	Scheme	Marks
1.	<p>(a) $p = 1.357; q = 1.382$</p> <p>(b) $I \approx \frac{0.5}{2} [1 + 2(1.216 + 1.357 + 1.413) + 1.382]$ $= 2.589$</p>	<p>B1 B1 (2)</p> <p>B1 M1 A1 ft</p> <p>A1 (4)</p> <p>(6 marks)</p>
2.	<p>(a) $\int x \cos 2x dx = \frac{x \sin 2x}{2} - \int \frac{\sin 2x}{2} dx$ (integration in correct direction)</p> <p>$= \frac{x \sin 2x}{2} + \frac{\cos 2x}{4} (+k)$ (second integration)</p> <p>(b) $x \frac{2 \sin x \cos x}{2} + \frac{1 - 2 \sin^2 x}{4} (+k)$ (use of appropriate double angle formulae)</p> <p>$= \frac{1}{2} \sin x (2x \cos x - \sin x) + \frac{1}{4} + k$ for $\frac{1}{4} + k$</p> <p>$= \frac{1}{2} \sin x (2x \cos x - \sin x) + C \star$</p>	<p>M1 A1</p> <p>M1 A1 (4)</p> <p>M1</p> <p>A1</p> <p>A1 cao (3)</p> <p>(7 marks)</p>
3.	<p>(a) $(1+3x)^{-2} = 1 + (-2)(3x) + \frac{(-2)(-3)}{2!}(3x)^2 + \frac{(-2)(-3)(-4)}{3!}(3x)^3 + \dots$</p> <p>$= 1, -6x, +27x^2 \dots (-108x^3)$</p> <p>(b) Using (a) to expand $(x+4)(1+3x)^{-2}$ or complete method to find coefficients</p> <p>[e.g. Maclaurin or $\frac{1}{3}(1+3x)^{-1} + \frac{11}{3}(1+3x)^{-2}$].</p> <p>$= 4 - 23x, +102x^2, -405x^3 = 4, -23x, +102x^2 \dots (-405x^3)$</p>	<p>M1</p> <p>B1 A1 A1 (4)</p> <p>M1</p> <p>A1, A1ft,</p> <p>A1ft (4)</p> <p>(8 marks)</p>

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4.	<p>(a) $\overrightarrow{AB} = 3\mathbf{b} + 6\mathbf{j} + 6\mathbf{k}$</p> <p>(b) $\cos A = \frac{-12 - 48 + 6}{\sqrt{81}\sqrt{81}} = -\frac{2}{3}$</p> <p>(c) $\lambda = 4$ at point A and $\lambda = 7$ at point B. $\mathbf{r} = -9\mathbf{k} + \lambda(\mathbf{i} + 2\mathbf{j} + 2\mathbf{k})$ represents a line</p> <p>(d) $(\lambda\mathbf{i} + 2\lambda\mathbf{j} + (2\lambda - 9)\mathbf{k}) \cdot (\mathbf{i} + 2\mathbf{j} + 2\mathbf{k}) = 0$ $\lambda + 4\lambda + \lambda - 18 = 0$. Therefore $\lambda = 2$</p> <p>(e) The point is (2, 4, -5)</p>	<p>B1 (1)</p> <p>M1 A1 A1 (3)</p> <p>B1 B1</p> <p>B1 (3)</p> <p>M1</p> <p>M1 A1 (3)</p> <p>M1 A1 (2)</p> <p>(12 marks)</p>
5.	<p>(a) $\frac{dy}{dx} = \sqrt{\sin x} + \frac{x}{2}(\sin x)^{-\frac{1}{2}} \cos x$</p> <p>At A $\sqrt{\sin x} + \frac{x}{2}(\sin x)^{-\frac{1}{2}} \cos x = 0$</p> <p>$\therefore \sin x + \frac{x}{2} \cos x = 0$ (essential to see intermediate line before given answer)</p> <p>$\therefore 2 \tan x + x = 0$ *</p> <p>(b) $V = \pi \int y^2 dx = \pi \int x^2 \sin x dx$</p> <p>$= \pi \left[-x^2 \cos x + \int 2x \cos x dx \right]_0^\pi$</p> <p>$= \pi \left[-x^2 \cos x + 2x \sin x - \int 2 \sin x dx \right]_0^\pi$</p> <p>$= \pi \left[-x^2 \cos x + 2x \sin x + 2 \cos x \right]_0^\pi$</p> <p>$= \pi \left[\pi^2 - 2 - 2 \right]$</p> <p>$= \pi \left[\pi^2 - 4 \right]$</p>	<p>M1 A1</p> <p>M1</p> <p>A1 (4)</p> <p>M1</p> <p>M1 A1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>A1 (7)</p> <p>(11 marks)</p>

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6.	<p>(a) $\frac{dN}{dt} = -kN$</p> <p>(b) $\int \frac{dN}{N} = \int -k dt$</p> <p>$\ln N = -kt + c$</p> <p>$N = e^{-kt+c} = Ae^{-kt}$</p> <p>(c) $3 \times 10^{17} = 7 \times 10^{18} e^{-8k}$</p> <p>$e^{-k} = \sqrt[8]{\frac{3}{70}} = 0.6745$ or $k = \frac{1}{8} \ln \frac{70}{3}$</p> <p>$k = 0.3937$</p> <p>(d) $N = 7 \times 10^{18} e^{-0.3937 \times 16}$ or $\frac{3}{70} \times 3 \times 10^{17}$</p> <p>$= 1.286 \times 10^{16}$</p>	<p>M1 A1 (2)</p> <p>B1 ft</p> <p>M1 A1 ft</p> <p>M1 A1 (5)</p> <p>M1</p> <p>M1</p> <p>A1 (3)</p> <p>M1</p> <p>A1 (2)</p> <p>(12 marks)</p>
7.	<p>(a) $A = 2, B = -16$</p> <p>(b) $A(1 - 2x)^{-1} + B(2 + x)^{-1}$ and attempt at expansion</p> <p>$A(1 + 2x + 4x^2 + 8x^3 + \dots) + \frac{B}{2} \left(1 - \frac{x}{2} + \frac{x^2}{4} - \frac{x^3}{8} + \dots\right)$</p> <p>$= 10 + 10x^2 + 15x^3 + \dots$</p>	<p>M1 A1 A1 (3)</p> <p>M1</p> <p>A1 M1 A1</p> <p>A1 (5)</p> <p>(8 marks)</p>

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8.	(a) $\frac{dy}{dx} = \frac{\frac{dy}{d\theta}}{\frac{dx}{d\theta}} = \frac{4 \cos \theta}{-5 \sin \theta}$	M1 A1
	Equation of tangent is $y - 4 \sin \alpha = \frac{4 \cos \alpha}{-5 \sin \alpha} (x - 5 \cos \alpha)$	M1
	$\therefore 5y \sin \alpha + 4x \cos \alpha = 20(\cos^2 \alpha + \sin^2 \alpha) = 20$ (*)	A1 (4)
	(b) $\int y \frac{dx}{d\theta} d\theta = - \int 4 \sin \theta 5 \sin \theta d\theta$	M1
	$= 10 \int (\cos 2\theta - 1) d\theta$	M1
	$= [5 \sin 2\theta - 10\theta]$	M1
	Area = 20π	A1 cso (4)
	(c) When $x = 0, y = \frac{4}{\sin \alpha}$, or when $y = 0, x = \frac{5}{\cos \alpha}$	B1
	Area of parallelogram = $4 \times \frac{10}{\sin \alpha \cos \alpha} = \frac{80}{\sin 2\alpha}$	M1 A1
	$\therefore A = \frac{80}{\sin 2\alpha} - 20\pi$	A1 (4)
(d) $\frac{80}{\sin 2\alpha} - 20\pi = 20\pi$	M1 A1	
$\sin 2\alpha = \frac{2}{\pi}$		
$\alpha = 0.345$	A1 (3)	
		(15 marks)