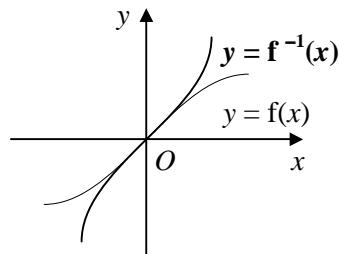


**C3****TRIGONOMETRY****Answers - Worksheet B**

**1**    **a**  $-1 \leq f(x) \leq 1$

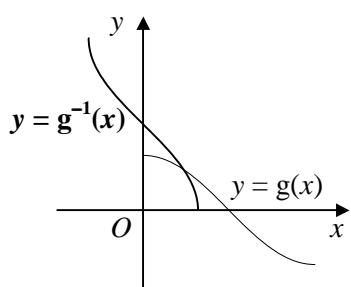
**b**  $f^{-1}(x) \equiv \arcsin x, x \in \mathbb{R}, -1 \leq x \leq 1$

**c**

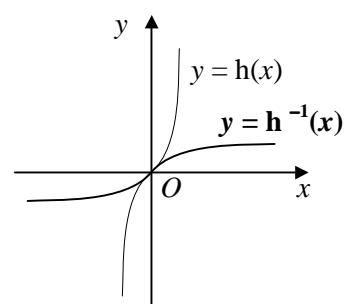


**3**    **a**  $g^{-1}(x) \equiv \arccos x, x \in \mathbb{R}, -1 \leq x \leq 1$

**b**



**2**    **a** 0    **b**  $\frac{\pi}{4}$     **c**  $-\frac{\pi}{2}$     **d**  $-\frac{\pi}{3}$



**5**    **a** 0

**b**  $\frac{\pi}{3}$

**c**  $\frac{\pi}{6}$

**d**  $-\frac{\pi}{6}$

**e**  $-\frac{\pi}{4}$

**f**  $\pi$

**g**  $-\frac{\pi}{6}$

**h**  $\frac{3\pi}{4}$

**6**    **a** 0.64

**b** 1.42

**c** 1.36

**d** -0.39

**e** 0.40

**f** -0.43

**g** -0.53

**h** 2.42

**7**    **a**  $x = \sin \frac{\pi}{4} = \frac{1}{\sqrt{2}}$

**b**  $x = \cos 0 = 1$

**c**  $x = \tan(-\frac{\pi}{3}) = -\sqrt{3}$

**d**  $2x = \cos \frac{\pi}{6} = \frac{\sqrt{3}}{2}$

**e**  $\arctan x = \frac{\pi}{4}$

**f**  $\arcsin x = -\frac{\pi}{6}$

$x = \frac{\sqrt{3}}{4}$

$x = \tan \frac{\pi}{4} = 1$

$x = \sin(-\frac{\pi}{6}) = -\frac{1}{2}$

**8**    **a**  $x = \cos 2 = -0.416$

**b**  $x = \sin(-0.7) = -0.644$

**c**  $3x = \tan 0.96 = 1.42836$   
 $x = 0.476$

**d**  $\arcsin x = 1$

**e**  $\arctan x = -\frac{2}{3}$

**f**  $\arccos 2x = 3$

$x = \sin 1 = 0.841$

$x = \tan(-\frac{2}{3}) = -0.787$

$2x = \cos 3 = -0.98999$

$x = -0.495$

**9**    **a**  $f(-\frac{1}{2}) = \frac{2\pi}{3} - \frac{\pi}{3} = \frac{\pi}{3}$

**b**  $\arccos x = \frac{\pi}{3} \Rightarrow x = \cos \frac{\pi}{3} = \frac{1}{2}$

**c**  $y = \arccos x - \frac{\pi}{3}$     swap     $x = \arccos y - \frac{\pi}{3}$   
 $y = \cos(x + \frac{\pi}{3})$

$f^{-1}(x) \equiv \cos(x + \frac{\pi}{3}), x \in \mathbb{R}, -\frac{\pi}{3} \leq x \leq \frac{2\pi}{3}$