## **FUNCTIONS**

(3)

(4)

(4)

**1** The function f is defined by

$$f: x \to 3 + \ln(x+2), x \in \mathbb{R}, x \ge k$$

where k is a constant.

Given that the range of f is 
$$f(x) \ge 3$$
,

- **a** find the value of k,
- **b** find  $f^{-1}(x)$ , stating its domain clearly.

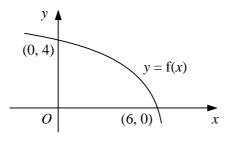
The function g is defined by

$$g: x \to 4 + \ln (x - 1), x \in \mathbb{R}, x > 1.$$

**c** Find, in terms of e, the value of x such that 
$$f(x) = g(x)$$
.

2

**C**3



The diagram shows the curve with equation y = f(x) which crosses the coordinate axes at the points (0, 4) and (6, 0).

Showing the coordinates of any points of intersection with the axes, sketch on separate diagrams the curves

$$\mathbf{a} \quad \mathbf{y} = \mathbf{f}(\mid \mathbf{x} \mid), \tag{2}$$

$$\mathbf{b} \quad y = 4 - \mathbf{f}(x), \tag{2}$$

$$\mathbf{c} \quad \mathbf{y} = 2\mathbf{f}(3\mathbf{x}). \tag{3}$$

**3** The functions f and g are given by

$$f(x) \equiv \frac{x}{x+2}, x \in \mathbb{R}, x \neq -2$$
$$g(x) \equiv \frac{3}{x}, x \in \mathbb{R}, x \neq 0$$

**a** Solve the equation fg(x) = 4. (4)

- **b** Find  $f^{-1}(x)$ , stating its domain clearly. (4)
- **c** Solve the equation  $f(x) = f^{-1}(x)$ . (3)

4 The function f is defined by

$$\mathbf{f}(x) \equiv x^2 - 2x - 9, \ x \in \mathbb{R}, \ x \ge k.$$

<b>a</b> Find the minimum value of the constant k for which $f^{-1}(x)$ exists.	(3)

Given that *k* takes the value found in part **a**,

- **b** solve the equation  $f^{-1}(x) = 4$ , (2)
- **c** sketch the curve y = |f(x)|, (3)
- **d** find the values of x for which |f(x)| = 6. (5)

## **C3** FUNCTIONS

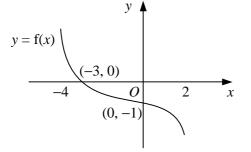
5	The function f is defined by	
	$f: x \to 2 - \frac{3}{x}, x \in \mathbb{R}, x \neq 0.$	
	<b>a</b> Find the value of $ff(1)$ .	(2)
	<b>b</b> Find $f^{-1}(x)$ and state its domain.	(4)
	The function g is defined by	
	$g: x \to x^2, x \in \mathbb{R}.$	
	<b>c</b> Solve the equation $gf(x) = 1$ .	(4)
6	The function f is defined by	
	$f: x \to e^{\frac{1}{2}x} - 2, \ x \in \mathbb{R}.$	
	<b>a</b> Evaluate f(ln 9).	(2)
	<b>b</b> State the range of f.	(1)
	<b>c</b> Find $f^{-1}(x)$ and state its domain.	(4)
	The function g is defined by	

$$g: x \to x^2 + 4x, x \in \mathbb{R}.$$

**d** Find and simplify an expression for gf(x).

e Solve the equation 
$$gf(x) + 1 = 0$$
.





The diagram shows the curve y = f(x). The domain of f is  $-4 \le x \le 2$  and the curve intersects the coordinate axes at the points (-3, 0) and (0, -1).

**a** Explain how the graph shows that f is one-one.

separate diagrams the graphs of

**b** Showing the coordinates of any points of intersection with the axes, sketch on

**i** 
$$y = |\mathbf{f}(x)|,$$
  
**ii**  $y = \mathbf{f}^{-1}(x).$ 
(5)

8

$$f(x) \equiv \frac{5}{(x+1)(2x-3)} + \frac{1}{x+1}, \ x \in \mathbb{R}, \ x \ge 2.$$

**a** Show that 
$$f(x) = \frac{2}{2x-3}$$
. (4)

- **b** Find the range of f.
- **c** Find an expression for  $f^{-1}(x)$ .

$$g(x) \equiv \frac{1}{x-2}, \ x \in \mathbb{R}, \ x \neq 2.$$

**d** Solve the equation  $fg(x) = \frac{2}{3}$ .

(4)

(2)

(3)

(3) (2)

(1)

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